

Package ‘Matrix’

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Title Sparse and Dense Matrix Classes and Methods

Description A rich hierarchy of sparse and dense matrix classes, including general, symmetric, triangular, and diagonal matrices with numeric, logical, or pattern entries. Efficient methods for operating on such matrices, often wrapping the 'BLAS', 'LAPACK', and 'SuiteSparse' libraries.

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URL <https://Matrix.R-forge.R-project.org>

BugReports https://R-forge.R-project.org/tracker/?atid=294&group_id=61

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Depends R (>= 4.4), methods

Imports grDevices, graphics, grid, lattice, stats, utils

Suggests MASS, datasets, sfsmisc, tools

Enhances SparseM, graph

LazyData no

LazyDataNote not possible, since we use data/*.R and our S4 classes

BuildResaveData no

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 abIndex-class

 Class "abIndex" of Abstract Index Vectors

Description

The "abIndex" class, short for "Abstract Index Vector", is used for dealing with large index vectors more efficiently, than using integer (or `numeric`) vectors of the kind `2:1000000` or `c(0:1e5, 1000:1e6)`.

Note that the current implementation details are subject to change, and if you consider working with these classes, please contact the package maintainers (`packageDescription("Matrix")$Maintainer`).

Objects from the Class

Objects can be created by calls of the form `new("abIndex", ...)`, but more easily and typically either by `as(x, "abIndex")` where `x` is an integer (valued) vector, or directly by `abIseq()` and combination `c(...)` of such.

Slots

`kind`: a `character` string, one of `("int32", "double", "rleDiff")`, denoting the internal structure of the `abIndex` object.

`x`: Object of class "numLike"; is used (i.e., not of length 0) only iff the object is *not* compressed, i.e., currently exactly when `kind != "rleDiff"`.

`rleD`: object of class "rleDiff", used for compression via `rle`.

Methods

as.numeric, as.integer, as.vector signature(`x = "abIndex"`): ...

[signature(`x = "abIndex"`, `i = "index"`, `j = "ANY"`, `drop = "ANY"`): ...

coerce signature(`from = "numeric"`, `to = "abIndex"`): ...

coerce signature(`from = "abIndex"`, `to = "numeric"`): ...

coerce signature(`from = "abIndex"`, `to = "integer"`): ...

length signature(`x = "abIndex"`): ...

Ops signature(`e1 = "numeric"`, `e2 = "abIndex"`): These and the following arithmetic and logic operations are **not yet implemented**; see `Ops` for a list of these (S4) group methods.

Ops signature(`e1 = "abIndex"`, `e2 = "abIndex"`): ...

Ops signature(`e1 = "abIndex"`, `e2 = "numeric"`): ...

Summary signature(`x = "abIndex"`): ...

show ("abIndex"): simple `show` method, building on `show(<rleDiff>)`.

is.na ("abIndex"): works analogously to regular vectors.

is.finite, is.infinite ("abIndex"): ditto.

Note

This is currently experimental and not yet used for our own code. Please contact us (`packageDescription("Matrix")$Maintainer`) if you plan to make use of this class.

Partly builds on ideas and code from Jens Oehlschlaegel, as implemented (around 2008, in the GPL'ed part of) package **ff**.

See Also

[rle \(base\)](#) which is used here; [numeric](#)

Examples

```
showClass("abIndex")
ii <- c(-3:40, 20:70)
str(ai <- as(ii, "abIndex"))# note
ai # -> show() method

stopifnot(identical(-3:20,
                    as(abIseq1(-3,20), "vector")))
```

abIseq

Sequence Generation of "abIndex", Abstract Index Vectors

Description

Generation of abstract index vectors, i.e., objects of class "[abIndex](#)".

`abIseq()` is designed to work entirely like [seq](#), but producing "[abIndex](#)" vectors.

`abIseq1()` is its basic building block, where `abIseq1(n,m)` corresponds to `n:m`.

`c(x, ...)` will return an "[abIndex](#)" vector, when `x` is one.

Usage

```
abIseq1(from = 1, to = 1)
abIseq (from = 1, to = 1, by = ((to - from)/(length.out - 1)),
       length.out = NULL, along.with = NULL)

## S3 method for class 'abIndex'
c(...)
```

Arguments

<code>from, to</code>	the starting and (maximal) end value of the sequence.
<code>by</code>	number: increment of the sequence.
<code>length.out</code>	desired length of the sequence. A non-negative number, which for <code>seq</code> and <code>seq.int</code> will be rounded up if fractional.
<code>along.with</code>	take the length from the length of this argument.
<code>...</code>	in general an arbitrary number of R objects; here, when the first is an " abIndex " vector, these arguments will be concatenated to a new " abIndex " object.

asUniqueT

*Standardize a Sparse Matrix in Triplet Format***Description**

Detect or standardize a [TsparseMatrix](#) with unsorted or duplicated (i, j) pairs.

Usage

```
anyDuplicatedT(x, ...)
isUniqueT(x, byrow = FALSE, isT = is(x, "TsparseMatrix"))
asUniqueT(x, byrow = FALSE, isT = is(x, "TsparseMatrix"))
aggregateT(x)
```

Arguments

x an R object. `anyDuplicatedT` and `aggregateT` require `x` inheriting from [TsparseMatrix](#). `asUniqueT` requires `x` inheriting from [Matrix](#) and coerces `x` to [TsparseMatrix](#) if necessary.

... optional arguments passed to the default method for generic function `anyDuplicated`.

byrow a logical indicating if `x` should be sorted by row then by column.

isT a logical indicating if `x` inherits from virtual class [TsparseMatrix](#).

Value

`anyDuplicatedT(x)` returns the index of the first duplicated (i, j) pair in `x` (0 if there are no duplicated pairs).

`isUniqueT(x)` returns TRUE if `x` is a [TsparseMatrix](#) with sorted, nonduplicated (i, j) pairs and FALSE otherwise.

`asUniqueT(x)` returns the unique [TsparseMatrix](#) representation of `x` with sorted, nonduplicated (i, j) pairs. Values corresponding to identical (i, j) pairs are aggregated by addition, where in the logical case “addition” refers to logical OR.

`aggregateT(x)` aggregates without sorting.

See Also

Virtual class [TsparseMatrix](#).

Examples

```
example("dgTMatrix-class", echo=FALSE)
## -> 'T2' with (i,j,x) slots of length 5 each
T2u <- asUniqueT(T2)
stopifnot(## They "are" the same (and print the same):
           all.equal(T2, T2u, tol=0),
           ## but not internally:
```



```

anyDuplicatedT(T2) == 2,
anyDuplicatedT(T2u) == 0,
length(T2 @x) == 5,
length(T2u@x) == 3)

isUniqueT(T2 ) # FALSE
isUniqueT(T2u) # TRUE

T3 <- T2u
T3[1, c(1,3)] <- 10; T3[2, c(1,5)] <- 20
T3u <- asUniqueT(T3)
str(T3u) # sorted in 'j', and within j, sorted in i
stopifnot(isUniqueT(T3u))

## Logical l.TMatrix and n.TMatrix :
(L2 <- T2 > 0)
validObject(L2u <- asUniqueT(L2))
(N2 <- as(L2, "nMatrix"))
validObject(N2u <- asUniqueT(N2))
stopifnot(N2u@i == L2u@i, L2u@i == T2u@i, N2@i == L2@i, L2@i == T2@i,
          N2u@j == L2u@j, L2u@j == T2u@j, N2@j == L2@j, L2@j == T2@j)
# now with a nasty NA [partly failed in Matrix 1.1-5]:
L.0N <- L.1N <- L2
L.0N@x[1:2] <- c(FALSE, NA)
L.1N@x[1:2] <- c(TRUE, NA)
validObject(L.0N)
validObject(L.1N)
(m.0N <- as.matrix(L.0N))
(m.1N <- as.matrix(L.1N))
stopifnot(identical(10L, which(is.na(m.0N))), !anyNA(m.1N))
symnum(m.0N)
symnum(m.1N)

```

band-methods

Extract bands of a matrix

Description

Return the matrix obtained by setting to zero elements below a diagonal (`triu`), above a diagonal (`tril`), or outside of a general band (`band`).

Usage

```

band(x, k1, k2, ...)
triu(x, k = 0L, ...)
tril(x, k = 0L, ...)

```

Arguments

<code>x</code>	a matrix-like object
<code>k, k1, k2</code>	integers specifying the diagonals that are not set to zero, $k1 \leq k2$. These are interpreted relative to the main diagonal, which is $k = 0$. Positive and negative values of k indicate diagonals above and below the main diagonal, respectively.
<code>...</code>	optional arguments passed to methods, currently unused by package Matrix .

Details

`triu(x, k)` is equivalent to `band(x, k, dim(x)[2])`. Similarly, `tril(x, k)` is equivalent to `band(x, -dim(x)[1], k)`.

Value

An object of a suitable matrix class, inheriting from `triangularMatrix` where appropriate. It inherits from `sparseMatrix` if and only if `x` does.

Methods

`x = "CsparseMatrix"` method for compressed, sparse, column-oriented matrices.

`x = "RsparseMatrix"` method for compressed, sparse, row-oriented matrices.

`x = "TsparseMatrix"` method for sparse matrices in triplet format.

`x = "diagonalMatrix"` method for diagonal matrices.

`x = "denseMatrix"` method for dense matrices in packed or unpacked format.

`x = "matrix"` method for traditional matrices of implicit class `matrix`.

See Also

[bandSparse](#) for the *construction* of a banded sparse matrix directly from its non-zero diagonals.

Examples

```
## A random sparse matrix :
set.seed(7)
m <- matrix(0, 5, 5)
m[sample(length(m), size = 14)] <- rep(1:9, length=14)
(mm <- as(m, "CsparseMatrix"))

tril(mm)      # lower triangle
tril(mm, -1) # strict lower triangle
triu(mm, 1)  # strict upper triangle
band(mm, -1, 2) # general band
(m5 <- Matrix(rnorm(25), ncol = 5))
tril(m5)      # lower triangle
tril(m5, -1) # strict lower triangle
triu(m5, 1)  # strict upper triangle
band(m5, -1, 2) # general band
(m65 <- Matrix(rnorm(30), ncol = 5)) # not square
```

```

triu(m65)      # result not "dtrMatrix" unless square
(sm5 <- crossprod(m65)) # symmetric
  band(sm5, -1, 1)# "dsyMatrix": symmetric band preserves symmetry property
as(band(sm5, -1, 1), "sparseMatrix")# often preferable
(sm <- round(crossprod(triu(mm/2)))) # sparse symmetric ("dsC*")
band(sm, -1,1) # remains "dsC", *however*
band(sm, -2,1) # -> "dgC"

```

bandSparse	<i>Construct Sparse Banded Matrix from (Sup-/Super-) Diagonals</i>
------------	--

Description

Construct a sparse banded matrix by specifying its non-zero sup- and super-diagonals.

Usage

```
bandSparse(n, m = n, k, diagonals, symmetric = FALSE,
           repr = "C", giveCsparse = (repr == "C"))
```

Arguments

n, m	the matrix dimension $(n, m) = (nrow, ncol)$.
k	integer vector of “diagonal numbers”, with identical meaning as in <code>band(*, k)</code> , i.e., relative to the main diagonal, which is $k=0$.
diagonals	optional list of sub-/super- diagonals; if missing, the result will be a pattern matrix, i.e., inheriting from class <code>nMatrix</code> . diagonals can also be $n' \times d$ matrix, where $d <- \text{length}(k)$ and $n' \geq \min(n, m)$. In that case, the sub-/super- diagonals are taken from the columns of diagonals, where only the first several rows will be used (typically) for off-diagonals.
symmetric	logical; if true the result will be symmetric (inheriting from class <code>symmetricMatrix</code>) and only the upper or lower triangle must be specified (via <code>k</code> and <code>diagonals</code>).
repr	<code>character</code> string, one of “C”, “T”, or “R”, specifying the sparse <i>representation</i> to be used for the result, i.e., one from the super classes <code>CsparseMatrix</code> , <code>TsparseMatrix</code> , or <code>RsparseMatrix</code> .
giveCsparse	(deprecated, replaced with repr): logical indicating if the result should be a <code>CsparseMatrix</code> or a <code>TsparseMatrix</code> , where the default was TRUE, and now is determined from <code>repr</code> ; very often <code>Csparse</code> matrices are more efficient subsequently, but not always.

Value

a sparse matrix (of class `CsparseMatrix`) of dimension $n \times m$ with diagonal “bands” as specified.

See Also

[band](#), for *extraction* of matrix bands; [bdiag](#), [diag](#), [sparseMatrix](#), [Matrix](#).

Examples

```
diags <- list(1:30, 10*(1:20), 100*(1:20))
s1 <- bandSparse(13, k = -c(0:2, 6), diag = c(diags, diags[2]), symm=TRUE)
s1
s2 <- bandSparse(13, k = c(0:2, 6), diag = c(diags, diags[2]), symm=TRUE)
stopifnot(identical(s1, t(s2)), is(s1,"dsCMatrix"))

## a pattern Matrix of *full* (sub-)diagonals:
bk <- c(0:4, 7,9)
(s3 <- bandSparse(30, k = bk, symm = TRUE))

## If you want a pattern matrix, but with "sparse"-diagonals,
## you currently need to go via logical sparse:
llis <- lapply(list(rpois(20, 2), rpois(20, 1), rpois(20, 3))[c(1:3, 2:3, 3:2)],
              as.logical)
(s4 <- bandSparse(20, k = bk, symm = TRUE, diag = llis))
(s4. <- as(drop0(s4), "nsparseMatrix"))

n <- 1e4
bk <- c(0:5, 7,11)
bMat <- matrix(1:8, n, 8, byrow=TRUE)
bLis <- as.data.frame(bMat)
B <- bandSparse(n, k = bk, diag = bLis)
Bs <- bandSparse(n, k = bk, diag = bLis, symmetric=TRUE)
B [1:15, 1:30]
Bs[1:15, 1:30]
## can use a list *or* a matrix for specifying the diagonals:
stopifnot(identical(B, bandSparse(n, k = bk, diag = bMat)),
          identical(Bs, bandSparse(n, k = bk, diag = bMat, symmetric=TRUE))
          , inherits(B, "dtCMatrix") # triangular!
)

```

bdiag

Construct a Block Diagonal Matrix

Description

Build a block diagonal matrix given several building block matrices.

Usage

```
bdiag(...)
.bdiag(lst)
```

Arguments

... individual matrices or a [list](#) of matrices.
 lst non-empty [list](#) of matrices.

Details

For non-trivial argument list, `bdiag()` calls `.bdiag()`. The latter maybe useful to programmers.

Value

A *sparse* matrix obtained by combining the arguments into a block diagonal matrix.

The value of `bdiag()` inherits from class `CsparseMatrix`, whereas `.bdiag()` returns a `TsparseMatrix`.

Note

This function has been written and is efficient for the case of relatively few block matrices which are typically sparse themselves.

It is currently *inefficient* for the case of many small dense block matrices. For the case of *many* dense $k \times k$ matrices, the `bdiag_m()` function in the ‘Examples’ is an order of magnitude faster.

Author(s)

Martin Maechler, built on a version posted by Berton Gunter to R-help; earlier versions have been posted by other authors, notably Scott Chasalow to S-news. Doug Bates’s faster implementation builds on `TsparseMatrix` objects.

See Also

[Diagonal](#) for constructing matrices of class `diagonalMatrix`, or [kronecker](#) which also works for “Matrix” inheriting matrices.

[bandSparse](#) constructs a *banded* sparse matrix from its non-zero sub-/super - diagonals.

Note that other CRAN R packages have own versions of `bdiag()` which return traditional matrices.

Examples

```
bdiag(matrix(1:4, 2), diag(3))
## combine "Matrix" class and traditional matrices:
bdiag(Diagonal(2), matrix(1:3, 3,4), diag(3:2))

m1list <- list(1, 2:3, diag(x=5:3), 27, cbind(1,3:6), 100:101)
bdiag(m1list)
stopifnot(identical(bdiag(m1list),
                    bdiag(lapply(m1list, as.matrix))))

m1 <- c(as(matrix((1:24)%% 11 == 0, 6,4), "nMatrix"),
        rep(list(Diagonal(2, x=TRUE)), 3))
m1n <- c(m1, Diagonal(x = 1:3))
stopifnot(is(bdiag(m1), "lsparseMatrix"),
          is(bdiag(m1n), "dsparseMatrix") )
```

```

## random (diagonal-)block-triangular matrices:
rblockTri <- function(nb, max.ni, lambda = 3) {
  .bdiag(replicate(nb, {
    n <- sample.int(max.ni, 1)
    tril(Matrix(rpois(n * n, lambda = lambda), n, n))
  }))
}

(T4 <- rblockTri(4, 10, lambda = 1))
image(T1 <- rblockTri(12, 20))

##' Fast version of Matrix :: .bdiag() -- for the case of *many* (k x k) matrices:
##' @param lmat list(<mat1>, <mat2>, ....., <mat_N>) where each mat_j is a k x k 'matrix'
##' @return a sparse (N*k x N*k) matrix of class \code{"\linkS4class{dgCMatrix}"}.
bdiag_m <- function(lmat) {
  ## Copyright (C) 2016 Martin Maechler, ETH Zurich
  if(!length(lmat)) return(new("dgCMatrix"))
  stopifnot(is.list(lmat), is.matrix(lmat[[1]]),
    (k <- (d <- dim(lmat[[1]]))[1]) == d[2], # k x k
    all(vapply(lmat, dim, integer(2)) == k)) # all of them
  N <- length(lmat)
  if(N * k > .Machine$integer.max)
    stop("resulting matrix too large; would be M x M, with M=", N*k)
  M <- as.integer(N * k)
  ## result: an M x M matrix
  new("dgCMatrix", Dim = c(M,M),
    ## 'i :' maybe there's a faster way (w/o matrix indexing), but elegant?
    i = as.vector(matrix(0L:(M-1L), nrow=k)[, rep(seq_len(N), each=k)]),
    p = k * 0L:M,
    x = as.double(unlist(lmat, recursive=FALSE, use.names=FALSE)))
}

l12 <- replicate(12, matrix(rpois(16, lambda = 6.4), 4, 4),
  simplify=FALSE)
dim(T12 <- bdiag_m(l12))# 48 x 48
T12[1:20, 1:20]

```

boolmatmult-methods *Boolean Arithmetic Matrix Products: %&% and Methods*

Description

For boolean or “pattern” matrices, i.e., R objects of class `nMatrix`, it is natural to allow matrix products using boolean instead of numerical arithmetic.

In package **Matrix**, we use the binary operator `%&%` (aka “infix”) function) for this and provide methods for all our matrices and the traditional R matrices (see `matrix`).

Value

a pattern matrix, i.e., inheriting from “`nMatrix`”, or an “`ldiMatrix`” in case of a diagonal matrix.

Methods

We provide methods for both the “traditional” (R base) matrices and numeric vectors and conceptually all matrices and `sparseVector`s in package **Matrix**.

```
signature(x = "ANY", y = "ANY")
signature(x = "ANY", y = "Matrix")
signature(x = "Matrix", y = "ANY")
signature(x = "nMatrix", y = "nMatrix")
signature(x = "nMatrix", y = "nsparseMatrix")
signature(x = "nsparseMatrix", y = "nMatrix")
signature(x = "nsparseMatrix", y = "nsparseMatrix")
signature(x = "sparseVector", y = "sparseVector")
```

Note

These boolean arithmetic matrix products had been newly introduced for **Matrix** 1.2.0 (March 2015). Its implementation has still not been tested extensively.

Originally, it was left unspecified how non-structural zeros, i.e., 0’s as part of the $M \times$ slot should be treated for numeric (“`dMatrix`”) and logical (“`lMatrix`”) sparse matrices. We now specify that boolean matrix products should behave as if applied to `drop0(M)`, i.e., as if dropping such zeros from the matrix before using it.

Equivalently, for all matrices M , boolean arithmetic should work as if applied to $M \neq 0$ (or $M \neq \text{FALSE}$).

The current implementation ends up coercing both x and y to (virtual) class `nsparseMatrix` which may be quite inefficient for dense matrices. A future implementation may well return a matrix with **different** class, but the “same” content, i.e., the same matrix entries $m_{i,j}$.

See Also

`%*%`, `crossprod()`, or `tcrossprod()`, for (regular) matrix product methods.

Examples

```
set.seed(7)
L <- Matrix(rnorm(20) > 1, 4, 5)
(N <- as(L, "nMatrix"))
L. <- L; L.[1:2,1] <- TRUE; L.@x[1:2] <- FALSE; L. # has "zeros" to drop0()
D <- Matrix(round(rnorm(30)), 5, 6) # -> values in -1:1 (for this seed)
L %%% D
stopifnot(identical(L %%% D, N %%% D),
           all(L %%% D == as((L %%% abs(D)) > 0, "sparseMatrix")))

## cross products , possibly with boolArith = TRUE :
crossprod(N) # -> sparse patter'n' (TRUE/FALSE : boolean arithmetic)
crossprod(N + 0) # -> numeric Matrix (with same "pattern")
stopifnot(all(crossprod(N) == t(N) %%% N),
           identical(crossprod(N), crossprod(N + 0, boolArith=TRUE)),
```

```

        identical(crossprod(L), crossprod(N , boolArith=FALSE)))
crossprod(D, boolArith = TRUE) # pattern: "nsCMatrix"
crossprod(L, boolArith = TRUE) # ditto
crossprod(L, boolArith = FALSE) # numeric: "dsCMatrix"

```

BunchKaufman-class *Dense Bunch-Kaufman Factorizations*

Description

Classes `BunchKaufman` and `pBunchKaufman` represent Bunch-Kaufman factorizations of $n \times n$ real, symmetric matrices A , having the general form

$$A = UD_UU' = LD_LL'$$

where D_U and D_L are symmetric, block diagonal matrices composed of b_U and b_L 1×1 or 2×2 diagonal blocks; $U = \prod_{k=1}^{b_U} P_k U_k$ is the product of b_U row-permuted unit upper triangular matrices, each having nonzero entries above the diagonal in 1 or 2 columns; and $L = \prod_{k=1}^{b_L} P_k L_k$ is the product of b_L row-permuted unit lower triangular matrices, each having nonzero entries below the diagonal in 1 or 2 columns.

These classes store the nonzero entries of the $2b_U + 1$ or $2b_L + 1$ factors, which are individually sparse, in a dense format as a vector of length nn (`BunchKaufman`) or $n(n+1)/2$ (`pBunchKaufman`), the latter giving the “packed” representation.

Slots

`Dim`, `Dimnames` inherited from virtual class `MatrixFactorization`.

`uplo` a string, either “U” or “L”, indicating which triangle (upper or lower) of the factorized symmetric matrix was used to compute the factorization and in turn how the `x` slot is partitioned.

`x` a numeric vector of length $n*n$ (`BunchKaufman`) or $n*(n+1)/2$ (`pBunchKaufman`), where $n=Dim[1]$. The details of the representation are specified by the manual for LAPACK routines `dsytrf` and `dsptrf`.

`perm` an integer vector of length $n=Dim[1]$ specifying row and column interchanges as described in the manual for LAPACK routines `dsytrf` and `dsptrf`.

Extends

Class `BunchKaufmanFactorization`, directly. Class `MatrixFactorization`, by class `BunchKaufmanFactorization`, distance 2.

Instantiation

Objects can be generated directly by calls of the form `new(“BunchKaufman”, ...)` or `new(“pBunchKaufman”, ...)`, but they are more typically obtained as the value of `BunchKaufman(x)` for `x` inheriting from `dsyMatrix` or `dspMatrix`.

Methods

`coerce` signature(`from` = "BunchKaufman", `to` = "dtrMatrix"): returns a `dtrMatrix`, useful for inspecting the internal representation of the factorization; see 'Note'.

`coerce` signature(`from` = "pBunchKaufman", `to` = "dtpMatrix"): returns a `dtpMatrix`, useful for inspecting the internal representation of the factorization; see 'Note'.

`determinant` signature(`from` = "p?BunchKaufman", `logarithm` = "logical"): computes the determinant of the factorized matrix A or its logarithm.

`expand1` signature(`x` = "p?BunchKaufman"): see [expand1-methods](#).

`expand2` signature(`x` = "p?BunchKaufman"): see [expand2-methods](#).

`solve` signature(`a` = "p?BunchKaufman", `b` = .): see [solve-methods](#).

Note

In **Matrix** < 1.6-0, class `BunchKaufman` extended `dtrMatrix` and class `pBunchKaufman` extended `dtpMatrix`, reflecting the fact that the internal representation of the factorization is fundamentally triangular: there are $n(n+1)/2$ "parameters", and these can be arranged systematically to form an $n \times n$ triangular matrix. **Matrix** 1.6-0 removed these extensions so that methods would no longer be inherited from `dtrMatrix` and `dtpMatrix`. The availability of such methods gave the wrong impression that `BunchKaufman` and `pBunchKaufman` represent a (singular) matrix, when in fact they represent an ordered set of matrix factors.

The coercions `as(., "dtrMatrix")` and `as(., "dtpMatrix")` are provided for users who understand the caveats.

References

The LAPACK source code, including documentation; see <https://netlib.org/lapack/double/dsytrf.f> and <https://netlib.org/lapack/double/dsptf.f>.

Golub, G. H., & Van Loan, C. F. (2013). *Matrix computations* (4th ed.). Johns Hopkins University Press. doi:10.56021/9781421407944

See Also

Class `dsyMatrix` and its packed counterpart.

Generic functions `BunchKaufman`, `expand1`, and `expand2`.

Examples

```
showClass("BunchKaufman")
set.seed(1)

n <- 6L
(A <- forceSymmetric(Matrix(rnorm(n * n), n, n)))

## With dimnames, to see that they are propagated :
dimnames(A) <- rep.int(list(paste0("x", seq_len(n))), 2L)

(bk.A <- BunchKaufman(A))
```

```

str(e.bk.A <- expand2(bk.A, complete = FALSE), max.level = 2L)
str(E.bk.A <- expand2(bk.A, complete = TRUE), max.level = 2L)

## Underlying LAPACK representation
(m.bk.A <- as(bk.A, "dtrMatrix"))
stopifnot(identical(as(m.bk.A, "matrix"), `dim<-`(bk.A@x, bk.A@Dim)))

## Number of factors is 2*b+1, b <= n, which can be nontrivial ...
(b <- (length(E.bk.A) - 1L) %% 2L)

ae1 <- function(a, b, ...) all.equal(as(a, "matrix"), as(b, "matrix"), ...)
ae2 <- function(a, b, ...) ae1(unname(a), unname(b), ...)

## A ~ U DU U', U := prod(Pk Uk) in floating point
stopifnot(exprs = {
  identical(names(e.bk.A), c("U", "DU", "U."))
  identical(e.bk.A[["U" ]], Reduce(`%*%`, E.bk.A[seq_len(b)]))
  identical(e.bk.A[["U." ]], t(e.bk.A[["U"]]))
  ae1(A, with(e.bk.A, U %*% DU %*% U.))
})

## Factorization handled as factorized matrix
b <- rnorm(n)
stopifnot(identical(det(A), det(bk.A)),
  identical(solve(A, b), solve(bk.A, b)))

```

BunchKaufman-methods *Methods for Bunch-Kaufman Factorization*

Description

Computes the Bunch-Kaufman factorization of an $n \times n$ real, symmetric matrix A , which has the general form

$$A = UD_UU' = LD_LL'$$

where D_U and D_L are symmetric, block diagonal matrices composed of b_U and b_L 1×1 or 2×2 diagonal blocks; $U = \prod_{k=1}^{b_U} P_k U_k$ is the product of b_U row-permuted unit upper triangular matrices, each having nonzero entries above the diagonal in 1 or 2 columns; and $L = \prod_{k=1}^{b_L} P_k L_k$ is the product of b_L row-permuted unit lower triangular matrices, each having nonzero entries below the diagonal in 1 or 2 columns.

Methods are built on LAPACK routines `dsytrf` and `dsptrf`.

Usage

```

BunchKaufman(x, ...)
## S4 method for signature 'dsyMatrix'
BunchKaufman(x, warnSing = TRUE, ...)
## S4 method for signature 'dspMatrix'
BunchKaufman(x, warnSing = TRUE, ...)

```

```
## S4 method for signature 'matrix'
BunchKaufman(x, uplo = "U", ...)
```

Arguments

x	a finite symmetric matrix or Matrix to be factorized. If x is square but not symmetric, then it will be <i>treated</i> as symmetric; see uplo.
warnSing	a logical indicating if a warning should be signaled for singular x.
uplo	a string, either "U" or "L", indicating which triangle of x should be used to compute the factorization.
...	further arguments passed to or from methods.

Value

An object representing the factorization, inheriting from virtual class [BunchKaufmanFactorization](#). The specific class is [BunchKaufman](#) unless x inherits from virtual class [packedMatrix](#), in which case it is [pBunchKaufman](#).

References

The LAPACK source code, including documentation; see <https://netlib.org/lapack/double/dsytrf.f> and <https://netlib.org/lapack/double/dsptrf.f>.

Golub, G. H., & Van Loan, C. F. (2013). *Matrix computations* (4th ed.). Johns Hopkins University Press. doi:10.56021/9781421407944

See Also

Classes [BunchKaufman](#) and [pBunchKaufman](#) and their methods.

Classes [dsyMatrix](#) and [dspMatrix](#).

Generic functions [expand1](#) and [expand2](#), for constructing matrix factors from the result.

Generic functions [Cholesky](#), [Schur](#), [lu](#), and [qr](#), for computing other factorizations.

Examples

```
showMethods("BunchKaufman", inherited = FALSE)
set.seed(0)

data(CAex, package = "Matrix")
class(CAex) # dgCMatrix
isSymmetric(CAex) # symmetric, but not formally

A <- as(CAex, "symmetricMatrix")
class(A) # dsCMatrix

## Have methods for denseMatrix (unpacked and packed),
## but not yet sparseMatrix ...
## Not run:
(bk.A <- BunchKaufman(A))
```

```
## End(Not run)
(bk.A <- BunchKaufman(as(A, "unpackedMatrix"))))

## A ~ U DU U' in floating point
str(e.bk.A <- expand2(bk.A), max.level = 2L)
stopifnot(all.equal(as(A, "matrix"), as(Reduce(`%%`, e.bk.A), "matrix")))
```

CAex

Albers' example Matrix with "Difficult" Eigen Factorization

Description

An example of a sparse matrix for which `eigen()` seemed to be difficult, an unscaled version of this has been posted to the web, accompanying an E-mail to R-help (<https://stat.ethz.ch/mailman/listinfo/r-help>), by Casper J Albers, Open University, UK.

Usage

```
data(CAex)
```

Format

This is a 72×72 symmetric matrix with 216 non-zero entries in five bands, stored as sparse matrix of class `dgCMatrix`.

Details

Historical note (2006-03-30): In earlier versions of R, `eigen(CAex)` fell into an infinite loop whereas `eigen(CAex, EISPACK=TRUE)` had been okay.

Examples

```
data(CAex, package = "Matrix")
str(CAex) # of class "dgCMatrix"

image(CAex)# -> it's a simple band matrix with 5 bands
## and the eigen values are basically 1 (42 times) and 0 (30 x):
zapsmall(ev <- eigen(CAex, only.values=TRUE)$values)
## i.e., the matrix is symmetric, hence
sCA <- as(CAex, "symmetricMatrix")
## and
stopifnot(class(sCA) == "dsCMatrix",
          as(sCA, "matrix") == as(CAex, "matrix"))
```

cbind2-methods *'cbind()' and 'rbind()' recursively built on cbind2/rbind2*

Description

The base functions `cbind` and `rbind` are defined for an arbitrary number of arguments and hence have the first formal argument `...`. Now, when S4 objects are found among the arguments, base `cbind()` and `rbind()` internally “dispatch” *recursively*, calling `cbind2` or `rbind2` respectively, where these have methods defined and so should dispatch appropriately.

`cbind2()` and `rbind2()` are from the **methods** package, i.e., standard R, and have been provided for binding together *two* matrices, where in **Matrix**, we have defined methods for these and the 'Matrix' matrices.

Usage

```
## cbind(..., deparse.level = 1)
## rbind(..., deparse.level = 1)

## S4 method for signature 'Matrix,Matrix'
cbind2(x, y, ...)
## S4 method for signature 'Matrix,Matrix'
rbind2(x, y, ...)
```

Arguments

<code>...</code>	for <code>[cr]bind</code> , vector- or matrix-like R objects to be bound together; for <code>[cr]bind2</code> , further arguments passed to or from methods; see <code>cbind</code> and <code>cbind2</code> .
<code>deparse.level</code>	integer controlling the construction of labels in the case of non-matrix-like arguments; see <code>cbind</code> .
<code>x, y</code>	vector- or matrix-like R objects to be bound together.

Value

typically a ‘matrix-like’ object of a similar `class` as the first argument in `...`

Note that sometimes by default, the result is a `sparseMatrix` if one of the arguments is (even in the case where this is not efficient). In other cases, the result is chosen to be sparse when there are more zero entries than non-zero ones (as the default sparse in `Matrix()`).

Author(s)

Martin Maechler

See Also

`cbind`, `cbind2`.

Our class definition help pages mentioning `cbind2()` and `rbind2()` methods: `"denseMatrix"`, `"diagonalMatrix"`, `"indMatrix"`.

Examples

```
(a <- matrix(c(2:1,1:2), 2,2))

(M1 <- cbind(0, rbind(a, 7))) # a traditional matrix

D <- Diagonal(2)
(M2 <- cbind(4, a, D, -1, D, 0)) # a sparse Matrix

stopifnot(validObject(M2), inherits(M2, "sparseMatrix"),
           dim(M2) == c(2,9))
```

CHMfactor-class

*Sparse Cholesky Factorizations***Description**

CHMfactor is the virtual class of sparse Cholesky factorizations of $n \times n$ real, symmetric matrices A , having the general form

$$P_1 A P_1' = L_1 D L_1' \stackrel{D_{jj} \geq 0}{=} LL'$$

or (equivalently)

$$A = P_1' L_1 D L_1' P_1 \stackrel{D_{jj} \geq 0}{=} P_1' L L' P_1$$

where P_1 is a permutation matrix, L_1 is a unit lower triangular matrix, D is a diagonal matrix, and $L = L_1 \sqrt{D}$. The second equalities hold only for positive semidefinite A , for which the diagonal entries of D are non-negative and \sqrt{D} is well-defined.

The implementation of class CHMfactor is based on CHOLMOD's C-level cholmod_factor_struct. Virtual subclasses CHMsimpl and CHMsuper separate the simplicial and supernodal variants. These have nonvirtual subclasses [dn]CHMsimpl and [dn]CHMsuper, where prefix 'd' and prefix 'n' are reserved for numeric and symbolic factorizations, respectively.

Usage

```
isLDL(x)
```

Arguments

x an object inheriting from virtual class CHMfactor, almost always the result of a call to generic function [Cholesky](#).

Value

isLDL(x) returns TRUE or FALSE: TRUE if x stores the lower triangular entries of $L_1 - I + D$, FALSE if x stores the lower triangular entries of L .

Slots

Of CHMfactor:

`Dim`, `Dimnames` inherited from virtual class [MatrixFactorization](#).

`colcount` an integer vector of length `Dim[1]` giving an *estimate* of the number of nonzero entries in each column of the lower triangular Cholesky factor. If symbolic analysis was performed prior to factorization, then the estimate is exact.

`perm` a 0-based integer vector of length `Dim[1]` specifying the permutation applied to the rows and columns of the factorized matrix. `perm` of length 0 is valid and equivalent to the identity permutation, implying no pivoting.

`type` an integer vector of length 6 specifying details of the factorization. The elements correspond to members `ordering`, `is_ll`, `is_super`, `is_monotonic`, `maxcsize`, and `maxesize` of the original `cholmod_factor_struct`. Simplicial and supernodal factorizations are distinguished by `is_super`. Simplicial factorizations do not use `maxcsize` or `maxesize`. Supernodal factorizations do not use `is_ll` or `is_monotonic`.

Of CHMsimpl (all unused by nCHMsimpl):

`nz` an integer vector of length `Dim[1]` giving the number of nonzero entries in each column of the lower triangular Cholesky factor. There is at least one nonzero entry in each column, because the diagonal elements of the factor are stored explicitly.

`p` an integer vector of length `Dim[1]+1`. Row indices of nonzero entries in column `j` of the lower triangular Cholesky factor are obtained as `i[p[j]+seq_len(nz[j])+1]`.

`i` an integer vector of length greater than or equal to `sum(nz)` containing the row indices of nonzero entries in the lower triangular Cholesky factor. These are grouped by column and sorted within columns, but the columns themselves need not be ordered monotonically. Columns may be overallocated, i.e., the number of elements of `i` reserved for column `j` may exceed `nz[j]`.

`prv`, `nxt` integer vectors of length `Dim[1]+2` indicating the order in which the columns of the lower triangular Cholesky factor are stored in `i` and `x`. Starting from `j <- Dim[1]+2`, the recursion `j <- nxt[j+1]+1` traverses the columns in forward order and terminates when `nxt[j+1] = -1`. Starting from `j <- Dim[1]+1`, the recursion `j <- prv[j+1]+1` traverses the columns in backward order and terminates when `prv[j+1] = -1`.

Of dCHMsimpl:

`x` a numeric vector parallel to `i` containing the corresponding nonzero entries of the lower triangular Cholesky factor L or (if and only if `type[2]` is 0) of the lower triangular matrix $L_1 - I + D$.

Of CHMsuper:

`super`, `pi`, `px` integer vectors of length `nsuper+1`, where `nsuper` is the number of supernodes. `super[j]+1` is the index of the leftmost column of supernode `j`. The row indices of supernode `j` are obtained as `s[pi[j]+seq_len(pi[j+1]-pi[j])+1]`. The numeric entries of supernode `j` are obtained as `x[px[j]+seq_len(px[j+1]-px[j])+1]` (if slot `x` is available).

`s` an integer vector of length greater than or equal to `Dim[1]` containing the row indices of the supernodes. `s` may contain duplicates, but not within a supernode, where the row indices must be increasing.

Of dCHMsuper:

`x` a numeric vector of length less than or equal to `prod(Dim)` containing the numeric entries of the supernodes.

Extends

Class `MatrixFactorization`, directly.

Instantiation

Objects can be generated directly by calls of the form `new("dCHMsimpl", ...)`, etc., but `dCHMsimpl` and `dCHMsuper` are more typically obtained as the value of `Cholesky(x, ...)` for `x` inheriting from `sparseMatrix` (often `dsCMatrix`).

There is currently no API outside of calls to `new` for generating `nCHMsimpl` and `nCHMsuper`. These classes are vestigial and may be formally deprecated in a future version of **Matrix**.

Methods

`coerce` signature(`from` = "CHMsimpl", `to` = "dtCMatrix"): returns a `dtCMatrix` representing the lower triangular Cholesky factor L or the lower triangular matrix $L_1 - I + D$, the latter if and only if `from@type[2]` is 0.

`coerce` signature(`from` = "CHMsuper", `to` = "dgCMatrix"): returns a `dgCMatrix` representing the lower triangular Cholesky factor L . Note that, for supernodes spanning two or more columns, the supernodal algorithm by design stores non-structural zeros above the main diagonal, hence `dgCMatrix` is indeed more appropriate than `dtCMatrix` as a coercion target.

`determinant` signature(`from` = "CHMfactor", `logarithm` = "logical"): behaves according to an optional argument `sqrt`. If `sqrt` = FALSE, then this method computes the determinant of the factorized matrix A or its logarithm. If `sqrt` = TRUE, then this method computes the determinant of the factor $L = L_1 \text{sqrt}(D)$ or its logarithm, giving NaN for the modulus when D has negative diagonal elements. For backwards compatibility, the default value of `sqrt` is TRUE, but that can be expected change in a future version of **Matrix**, hence defensive code will always set `sqrt` (to TRUE, if the code must remain backwards compatible with **Matrix** < 1.6-0). Calls to this method not setting `sqrt` may warn about the pending change. The warnings can be disabled with `options(Matrix.warnSqrtDefault = 0)`.

`diag` signature(`x` = "CHMfactor"): returns a numeric vector of length n containing the diagonal elements of D , which (if they are all non-negative) are the squared diagonal elements of L .

`expand` signature(`x` = "CHMfactor"): see [expand-methods](#).

`expand1` signature(`x` = "CHMsimpl"): see [expand1-methods](#).

`expand1` signature(`x` = "CHMsuper"): see [expand1-methods](#).

`expand2` signature(`x` = "CHMsimpl"): see [expand2-methods](#).

`expand2` signature(`x` = "CHMsuper"): see [expand2-methods](#).

`image` signature(`x` = "CHMfactor"): see [image-methods](#).

`nnzero` signature(`x` = "CHMfactor"): see [nnzero-methods](#).

`solve` signature(`a` = "CHMfactor", `b` = .): see [solve-methods](#).

update signature(object = "CHMfactor"): returns a copy of object with the same nonzero pattern but with numeric entries updated according to additional arguments parent and mult, where parent is (coercible to) a `dsCMatrix` or a `dgCMatrix` and mult is a numeric vector of positive length.

The numeric entries are updated with those of the Cholesky factor of $F(\text{parent}) + \text{mult}[1] * I$, i.e., $F(\text{parent})$ plus $\text{mult}[1]$ times the identity matrix, where $F = \text{identity}$ for symmetric parent and $F = \text{tcrossprod}$ for other parent. The nonzero pattern of $F(\text{parent})$ must match that of S if $\text{object} = \text{Cholesky}(S, \dots)$.

updown signature(update = ., C = ., object = "CHMfactor"): see [updown-methods](#).

References

The CHOLMOD source code; see <https://github.com/DrTimothyAldenDavis/SuiteSparse>, notably the header file 'CHOLMOD/Include/cholmod.h' defining cholmod_factor_struct.

Chen, Y., Davis, T. A., Hager, W. W., & Rajamanickam, S. (2008). Algorithm 887: CHOLMOD, supernodal sparse Cholesky factorization and update/downdate. *ACM Transactions on Mathematical Software*, 35(3), Article 22, 1-14. doi:10.1145/1391989.1391995

Amestoy, P. R., Davis, T. A., & Duff, I. S. (2004). Algorithm 837: AMD, an approximate minimum degree ordering algorithm. *ACM Transactions on Mathematical Software*, 17(4), 886-905. doi:10.1145/1024074.1024081

Golub, G. H., & Van Loan, C. F. (2013). *Matrix computations* (4th ed.). Johns Hopkins University Press. doi:10.56021/9781421407944

See Also

Class [dsCMatrix](#).

Generic functions [Cholesky](#), [updown](#), [expand1](#) and [expand2](#).

Examples

```
showClass("dCHMsimpl")
showClass("dCHMsuper")
set.seed(2)

m <- 1000L
n <- 200L
M <- rsparsematrix(m, n, 0.01)
A <- crossprod(M)

## With dimnames, to see that they are propagated :
dimnames(A) <- dn <- rep.int(list(paste0("x", seq_len(n))), 2L)

(ch.A <- Cholesky(A)) # pivoted, by default
str(e.ch.A <- expand2(ch.A, LDL = TRUE), max.level = 2L)
str(E.ch.A <- expand2(ch.A, LDL = FALSE), max.level = 2L)

ae1 <- function(a, b, ...) all.equal(as(a, "matrix"), as(b, "matrix"), ...)
ae2 <- function(a, b, ...) ae1(unname(a), unname(b), ...)
```

```

## A ~ P1' L1 D L1' P1 ~ P1' L L' P1 in floating point
stopifnot(exprs = {
  identical(names(e.ch.A), c("P1.", "L1", "D", "L1.", "P1"))
  identical(names(E.ch.A), c("P1.", "L", "L.", "P1"))
  identical(e.ch.A[["P1"]],
    new("pMatrix", Dim = c(n, n), Dimnames = c(list(NULL), dn[2L]),
      margin = 2L, perm = invertPerm(ch.A@perm, 0L, 1L))
  identical(e.ch.A[["P1."]], t(e.ch.A[["P1"]]))
  identical(e.ch.A[["L1."]], t(e.ch.A[["L1"]]))
  identical(E.ch.A[["L." ]], t(E.ch.A[["L" ]]))
  identical(e.ch.A[["D"]], Diagonal(x = diag(ch.A)))
  all.equal(E.ch.A[["L"]], with(e.ch.A, L1 %%% sqrt(D)))
  ae1(A, with(e.ch.A, P1. %%% L1 %%% D %%% L1. %%% P1))
  ae1(A, with(E.ch.A, P1. %%% L %%% L. %%% P1))
  ae2(A[ch.A@perm + 1L, ch.A@perm + 1L], with(e.ch.A, L1 %%% D %%% L1.))
  ae2(A[ch.A@perm + 1L, ch.A@perm + 1L], with(E.ch.A, L %%% L. ))
})

## Factorization handled as factorized matrix
## (in some cases only optionally, depending on arguments)
b <- rnorm(n)
stopifnot(identical(det(A), det(ch.A, sqrt = FALSE)),
  identical(solve(A, b), solve(ch.A, b, system = "A")))

u1 <- update(ch.A, A, mult = sqrt(2))
u2 <- update(ch.A, t(M), mult = sqrt(2)) # updating with crossprod(M), not M
stopifnot(all.equal(u1, u2, tolerance = 1e-14))

```

chol-methods

Compute the Cholesky Factor of a Matrix

Description

Computes the upper triangular Cholesky factor of an $n \times n$ real, symmetric, positive semidefinite matrix A , optionally after pivoting. That is the factor L' in

$$P_1 A P_1' = L L'$$

or (equivalently)

$$A = P_1' L L' P_1$$

where P_1 is a permutation matrix.

Methods for [denseMatrix](#) are built on LAPACK routines `dpstrf`, `dpotrf`, and `dpptrf`. The latter two do not permute rows or columns, so that P_1 is an identity matrix.

Methods for [sparseMatrix](#) are built on CHOLMOD routines `cholmod_analyze` and `cholmod_factorize_p`.

Usage

```
chol(x, ...)
## S4 method for signature 'dsyMatrix'
chol(x, pivot = FALSE, tol = -1, ...)
## S4 method for signature 'dspMatrix'
chol(x, ...)
## S4 method for signature 'dsCMatrix'
chol(x, pivot = FALSE, ...)
## S4 method for signature 'ddiMatrix'
chol(x, ...)
## S4 method for signature 'generalMatrix'
chol(x, uplo = "U", ...)
## S4 method for signature 'triangularMatrix'
chol(x, uplo = "U", ...)
```

Arguments

<code>x</code>	a finite , symmetric, positive semidefinite matrix or Matrix to be factorized. If <code>x</code> is square but not symmetric, then it will be <i>treated</i> as symmetric; see <code>uplo</code> . Methods for dense <code>x</code> require positive definiteness when <code>pivot = FALSE</code> . Methods for sparse (but not diagonal) <code>x</code> require positive definiteness unconditionally.
<code>pivot</code>	a logical indicating if the rows and columns of <code>x</code> should be pivoted. Methods for sparse <code>x</code> employ the approximate minimum degree (AMD) algorithm in order to reduce fill-in, i.e., without regard for numerical stability.
<code>tol</code>	a finite numeric tolerance, used only if <code>pivot = TRUE</code> . The factorization algorithm stops if the pivot is less than or equal to <code>tol</code> . Negative <code>tol</code> is equivalent to <code>nrow(x) * .Machine\$double.eps * max(diag(x))</code> .
<code>uplo</code>	a string, either "U" or "L", indicating which triangle of <code>x</code> should be used to compute the factorization. The default is "U", even for lower triangular <code>x</code> , to be consistent with <code>chol</code> from base .
<code>...</code>	further arguments passed to or from methods.

Details

For `x` inheriting from [diagonalMatrix](#), the diagonal result is computed directly and without pivoting, i.e., bypassing `CHOLMOD`.

For all other `x`, `chol(x, pivot = value)` calls `Cholesky(x, perm = value, ...)` under the hood. If you must know the permutation P_1 in addition to the Cholesky factor L' , then call [Cholesky](#) directly, as the result of `chol(x, pivot = TRUE)` specifies L' but not P_1 .

Value

A matrix, [triangularMatrix](#), or [diagonalMatrix](#) representing the upper triangular Cholesky factor L' . The result is a traditional matrix if `x` is a traditional matrix, dense if `x` is dense, and sparse if `x` is sparse.

References

The LAPACK source code, including documentation; see <https://netlib.org/lapack/double/dpstrf.f>, <https://netlib.org/lapack/double/dpotrf.f>, and <https://netlib.org/lapack/double/dpptrf.f>.

The CHOLMOD source code; see <https://github.com/DrTimothyAldenDavis/SuiteSparse>, notably the header file 'CHOLMOD/Include/cholmod.h' defining cholmod_factor_struct.

Chen, Y., Davis, T. A., Hager, W. W., & Rajamanickam, S. (2008). Algorithm 887: CHOLMOD, supernodal sparse Cholesky factorization and update/downdate. *ACM Transactions on Mathematical Software*, 35(3), Article 22, 1-14. doi:10.1145/1391989.1391995

Amestoy, P. R., Davis, T. A., & Duff, I. S. (2004). Algorithm 837: AMD, an approximate minimum degree ordering algorithm. *ACM Transactions on Mathematical Software*, 17(4), 886-905. doi:10.1145/1024074.1024081

Golub, G. H., & Van Loan, C. F. (2013). *Matrix computations* (4th ed.). Johns Hopkins University Press. doi:10.56021/9781421407944

See Also

The default method from **base**, `chol`, called for traditional matrices x .

Generic function `Cholesky`, for more flexibility notably when computing the Cholesky *factorization* and not only the *factor* L' .

Examples

```
showMethods("chol", inherited = FALSE)
set.seed(0)

## ---- Dense -----

## chol(x, pivot = value) wrapping Cholesky(x, perm = value)
selectMethod("chol", "dsyMatrix")

## Except in packed cases where pivoting is not yet available
selectMethod("chol", "dspMatrix")

## .... Positive definite .....

(A1 <- new("dsyMatrix", Dim = c(2L, 2L), x = c(1, 2, 2, 5)))
(R1.nopivot <- chol(A1))
(R1 <- chol(A1, pivot = TRUE))

## In 2-by-2 cases, we know that the permutation is 1:2 or 2:1,
## even if in general 'chol' does not say ...

stopifnot(exprs = {
  all.equal( A1 , as(crossprod(R1.nopivot), "dsyMatrix"))
  all.equal(t(A1[2:1, 2:1]), as(crossprod(R1 , ), "dsyMatrix"))
  identical(Cholesky(A1)@perm, 2:1) # because 5 > 1
})
```

```

## .... Positive semidefinite but not positive definite .....

(A2 <- new("dpoMatrix", Dim = c(2L, 2L), x = c(1, 2, 2, 4)))
try(R2.nopivot <- chol(A2)) # fails as not positive definite
(R2 <- chol(A2, pivot = TRUE)) # returns, with a warning and ...

stopifnot(exprs = {
  all.equal(t(A2[2:1, 2:1]), as(crossprod(R2), "dsyMatrix"))
  identical(Cholesky(A2)@perm, 2:1) # because 4 > 1
})

## .... Not positive semidefinite .....

(A3 <- new("dsyMatrix", Dim = c(2L, 2L), x = c(1, 2, 2, 3)))
try(R3.nopivot <- chol(A3)) # fails as not positive definite
(R3 <- chol(A3, pivot = TRUE)) # returns, with a warning and ...

## _Not_ equal: see details and examples in help("Cholesky")
all.equal(t(A3[2:1, 2:1]), as(crossprod(R3), "dsyMatrix"))

## ---- Sparse -----

## chol(x, pivot = value) wrapping
## Cholesky(x, perm = value, LDL = FALSE, super = FALSE)
selectMethod("chol", "dsCMatrix")

## Except in diagonal cases which are handled "directly"
selectMethod("chol", "ddiMatrix")

(A4 <- toeplitz(as(c(10, 0, 1, 0, 3), "sparseVector")))
(ch.A4.nopivot <- Cholesky(A4, perm = FALSE, LDL = FALSE, super = FALSE))
(ch.A4 <- Cholesky(A4, perm = TRUE, LDL = FALSE, super = FALSE))
(R4.nopivot <- chol(A4))
(R4 <- chol(A4, pivot = TRUE))

det4 <- det(A4)
b4 <- rnorm(5L)
x4 <- solve(A4, b4)

stopifnot(exprs = {
  identical(R4.nopivot, expand1(ch.A4.nopivot, "L."))
  identical(R4, expand1(ch.A4, "L."))
  all.equal(A4, crossprod(R4.nopivot))
  all.equal(A4[ch.A4@perm + 1L, ch.A4@perm + 1L], crossprod(R4))
  all.equal(diag(R4.nopivot), sqrt(diag(ch.A4.nopivot)))
  all.equal(diag(R4), sqrt(diag(ch.A4)))
  all.equal(sqrt(det4), det(R4.nopivot))
  all.equal(sqrt(det4), det(R4))
  all.equal(det4, det(ch.A4.nopivot, sqrt = FALSE))
  all.equal(det4, det(ch.A4, sqrt = FALSE))
  all.equal(x4, solve(R4.nopivot, solve(t(R4.nopivot), b4)))
  all.equal(x4, solve(ch.A4.nopivot, b4))
  all.equal(x4, solve(ch.A4, b4))
})

```

})

chol2inv-methods *Inverse from Cholesky Factor*

Description

Given *formally* upper and lower triangular matrices U and L , compute $(U'U)^{-1}$ and $(LL')^{-1}$, respectively.

This function can be seen as way to compute the inverse of a symmetric positive definite matrix given its Cholesky factor. Equivalently, it can be seen as a way to compute $(X'X)^{-1}$ given the R part of the QR factorization of X , if R is constrained to have positive diagonal entries.

Usage

```
chol2inv(x, ...)
## S4 method for signature 'dtrMatrix'
chol2inv(x, ...)
## S4 method for signature 'dtCMatrix'
chol2inv(x, ...)
## S4 method for signature 'generalMatrix'
chol2inv(x, uplo = "U", ...)
```

Arguments

<code>x</code>	a square matrix or Matrix , typically the result of a call to chol . If <code>x</code> is square but not (formally) triangular, then only the upper or lower triangle is considered, depending on optional argument <code>uplo</code> if <code>x</code> is a Matrix .
<code>uplo</code>	a string, either "U" or "L", indicating which triangle of <code>x</code> contains the Cholesky factor. The default is "U", to be consistent with chol2inv from base .
<code>...</code>	further arguments passed to or from methods.

Value

A matrix, [symmetricMatrix](#), or [diagonalMatrix](#) representing the inverse of the positive definite matrix whose Cholesky factor is `x`. The result is a traditional matrix if `x` is a traditional matrix, dense if `x` is dense, and sparse if `x` is sparse.

See Also

The default method from **base**, [chol2inv](#), called for traditional matrices `x`.

Generic function [chol](#), for computing the upper triangular Cholesky factor L' of a symmetric positive semidefinite matrix.

Generic function [solve](#), for solving linear systems and (as a corollary) for computing inverses more generally.

Examples

```
(A <- Matrix(cbind(c(1, 1, 1), c(1, 2, 4), c(1, 4, 16))))
(R <- chol(A))
(L <- t(R))
(R2i <- chol2inv(R))
(L2i <- chol2inv(R))
stopifnot(exprs = {
  all.equal(R2i, tcrossprod(solve(R)))
  all.equal(L2i, crossprod(solve(L)))
  all.equal(as(R2i %% A, "matrix"), diag(3L)) # the identity
  all.equal(as(L2i %% A, "matrix"), diag(3L)) # ditto
})
```

Cholesky-class

*Dense Cholesky Factorizations***Description**

Classes `Cholesky` and `pCholesky` represent dense, pivoted Cholesky factorizations of $n \times n$ real, symmetric, positive semidefinite matrices A , having the general form

$$P_1 A P_1' = L_1 D L_1' = L L'$$

or (equivalently)

$$A = P_1' L_1 D L_1' P_1 = P_1' L L' P_1$$

where P_1 is a permutation matrix, L_1 is a unit lower triangular matrix, D is a non-negative diagonal matrix, and $L = L_1 \sqrt{D}$.

These classes store the entries of the Cholesky factor L or its transpose L' in a dense format as a vector of length nn (`Cholesky`) or $n(n+1)/2$ (`pCholesky`), the latter giving the “packed” representation.

Slots

`Dim`, `Dimnames` inherited from virtual class `MatrixFactorization`.

`uplo` a string, either “U” or “L”, indicating which triangle (upper or lower) of the factorized symmetric matrix was used to compute the factorization and in turn whether `x` stores L' or L .

`x` a numeric vector of length $n*n$ (`Cholesky`) or $n*(n+1)/2$ (`pCholesky`), where $n=Dim[1]$, listing the entries of the Cholesky factor L or its transpose L' in column-major order.

`perm` a 1-based integer vector of length `Dim[1]` specifying the permutation applied to the rows and columns of the factorized matrix. `perm` of length 0 is valid and equivalent to the identity permutation, implying no pivoting.

Extends

Class `CholeskyFactorization`, directly. Class `MatrixFactorization`, by class `CholeskyFactorization`, distance 2.

Instantiation

Objects can be generated directly by calls of the form `new("Cholesky", ...)` or `new("pCholesky", ...)`, but they are more typically obtained as the value of `Cholesky(x)` for `x` inheriting from `dsyMatrix` or `dspMatrix` (often the subclasses of those reserved for positive semidefinite matrices, namely `dpoMatrix` and `dppMatrix`).

Methods

`coerce` signature(`from = "Cholesky"`, `to = "dtrMatrix"`): returns a `dtrMatrix` representing the Cholesky factor L or its transpose L' ; see ‘Note’.

`coerce` signature(`from = "pCholesky"`, `to = "dtpMatrix"`): returns a `dtpMatrix` representing the Cholesky factor L or its transpose L' ; see ‘Note’.

`determinant` signature(`from = "p?Cholesky"`, `logarithm = "logical"`): computes the determinant of the factorized matrix A or its logarithm.

`diag` signature(`x = "p?Cholesky"`): returns a numeric vector of length n containing the diagonal elements of D , which are the squared diagonal elements of L .

`expand1` signature(`x = "p?Cholesky"`): see [expand1-methods](#).

`expand2` signature(`x = "p?Cholesky"`): see [expand2-methods](#).

`solve` signature(`a = "p?Cholesky"`, `b = .`): see [solve-methods](#).

Note

In **Matrix** < 1.6-0, class `Cholesky` extended `dtrMatrix` and class `pCholesky` extended `dtpMatrix`, reflecting the fact that the factor L is indeed a triangular matrix. **Matrix** 1.6-0 removed these extensions so that methods would no longer be inherited from `dtrMatrix` and `dtpMatrix`. The availability of such methods gave the wrong impression that `Cholesky` and `pCholesky` represent a (singular) matrix, when in fact they represent an ordered set of matrix factors.

The coercions `as(., "dtrMatrix")` and `as(., "dtpMatrix")` are provided for users who understand the caveats.

References

The LAPACK source code, including documentation; see <https://netlib.org/lapack/double/dpstrf.f>, <https://netlib.org/lapack/double/dpotrf.f>, and <https://netlib.org/lapack/double/dpptrf.f>.

Lucas, C. (2004). *LAPACK-style codes for level 2 and 3 pivoted Cholesky factorizations*. LAPACK Working Note, Number 161. <https://www.netlib.org/lapack/lawnpdf/lawn161.pdf>

Golub, G. H., & Van Loan, C. F. (2013). *Matrix computations* (4th ed.). Johns Hopkins University Press. doi:10.56021/9781421407944

See Also

Class `CHMfactor` for sparse Cholesky factorizations.

Classes `dpoMatrix` and `dppMatrix`.

Generic functions `Cholesky`, `expand1` and `expand2`.

Examples

```

showClass("Cholesky")
set.seed(1)

m <- 30L
n <- 6L
(A <- crossprod(Matrix(rnorm(m * n), m, n)))

## With dimnames, to see that they are propagated :
dimnames(A) <- dn <- rep.int(list(paste0("x", seq_len(n))), 2L)

(ch.A <- Cholesky(A)) # pivoted, by default
str(e.ch.A <- expand2(ch.A, LDL = TRUE), max.level = 2L)
str(E.ch.A <- expand2(ch.A, LDL = FALSE), max.level = 2L)

## Underlying LAPACK representation
(m.ch.A <- as(ch.A, "dtrMatrix")) # which is L', not L, because
A@uplo == "U"
stopifnot(identical(as(m.ch.A, "matrix"), `dim<-`(ch.A@x, ch.A@Dim)))

ae1 <- function(a, b, ...) all.equal(as(a, "matrix"), as(b, "matrix"), ...)
ae2 <- function(a, b, ...) ae1(unname(a), unname(b), ...)

##  $A \sim P1' L1 D L1' P1 \sim P1' L L' P1$  in floating point
stopifnot(exprs = {
  identical(names(e.ch.A), c("P1.", "L1", "D", "L1.", "P1"))
  identical(names(E.ch.A), c("P1.", "L", "L.", "P1"))
  identical(e.ch.A[["P1"]],
    new("pMatrix", Dim = c(n, n), Dimnames = c(list(NULL), dn[2L]),
      margin = 2L, perm = invertPerm(ch.A@perm)))
  identical(e.ch.A[["P1."]], t(e.ch.A[["P1"]]))
  identical(e.ch.A[["L1."]], t(e.ch.A[["L1"]]))
  identical(E.ch.A[["L." ]], t(E.ch.A[["L" ]]))
  identical(e.ch.A[["D"]], Diagonal(x = diag(ch.A)))
  all.equal(E.ch.A[["L"]], with(e.ch.A, L1 %*% sqrt(D)))
  ae1(A, with(e.ch.A, P1. %*% L1 %*% D %*% L1. %*% P1))
  ae1(A, with(E.ch.A, P1. %*% L %*% L. %*% P1))
  ae2(A[ch.A@perm, ch.A@perm], with(e.ch.A, L1 %*% D %*% L1.))
  ae2(A[ch.A@perm, ch.A@perm], with(E.ch.A, L %*% L. ))
})

## Factorization handled as factorized matrix
b <- rnorm(n)
all.equal(det(A), det(ch.A), tolerance = 0)
all.equal(solve(A, b), solve(ch.A, b), tolerance = 0)

## For identical results, we need the _unpivoted_ factorization
## computed by det(A) and solve(A, b)
(ch.A.nopivot <- Cholesky(A, perm = FALSE))
stopifnot(identical(det(A), det(ch.A.nopivot)),
  identical(solve(A, b), solve(ch.A.nopivot, b)))

```

Description

Computes the pivoted Cholesky factorization of an $n \times n$ real, symmetric matrix A , which has the general form

$$P_1 A P_1' = L_1 D L_1' \stackrel{D_{jj} \geq 0}{=} L L'$$

or (equivalently)

$$A = P_1' L_1 D L_1' P_1 \stackrel{D_{jj} \geq 0}{=} P_1' L L' P_1$$

where P_1 is a permutation matrix, L_1 is a unit lower triangular matrix, D is a diagonal matrix, and $L = L_1 \sqrt{D}$. The second equalities hold only for positive semidefinite A , for which the diagonal entries of D are non-negative and \sqrt{D} is well-defined.

Methods for [denseMatrix](#) are built on LAPACK routines `dpstrf`, `dpotrf`, and `dpptrf`. The latter two do not permute rows or columns, so that P_1 is an identity matrix.

Methods for [sparseMatrix](#) are built on CHOLMOD routines `cholmod_analyze` and `cholmod_factorize_p`.

Usage

```
Cholesky(A, ...)
## S4 method for signature 'dsyMatrix'
Cholesky(A, perm = TRUE, tol = -1, ...)
## S4 method for signature 'dspMatrix'
Cholesky(A, ...)
## S4 method for signature 'dsCMatrix'
Cholesky(A, perm = TRUE, LDL = !super, super = FALSE,
  Imult = 0, ...)
## S4 method for signature 'ddiMatrix'
Cholesky(A, ...)
## S4 method for signature 'generalMatrix'
Cholesky(A, uplo = "U", ...)
## S4 method for signature 'triangularMatrix'
Cholesky(A, uplo = "U", ...)
## S4 method for signature 'matrix'
Cholesky(A, uplo = "U", ...)
```

Arguments

A a [finite](#), symmetric matrix or [Matrix](#) to be factorized. If A is square but not symmetric, then it will be *treated* as symmetric; see `uplo`. Methods for dense A require positive definiteness when `perm = FALSE` and positive semidefiniteness when `perm = TRUE`. Methods for sparse A require positive definiteness when `LDL = TRUE` and nonzero leading principal minors (after pivoting) when `LDL = FALSE`. Methods for sparse, *diagonal* A are an exception, requiring positive semidefiniteness unconditionally.

perm	a logical indicating if the rows and columns of A should be pivoted. Methods for sparse A employ the approximate minimum degree (AMD) algorithm in order to reduce fill-in, i.e., without regard for numerical stability. Pivoting for sparsity may introduce nonpositive leading principal minors, causing the factorization to fail, in which case it may be necessary to set perm = FALSE.
tol	a finite numeric tolerance, used only if perm = TRUE. The factorization algorithm stops if the pivot is less than or equal to tol. Negative tol is equivalent to $\text{nrow}(A) * \text{.Machine}\$double.eps * \max(\text{diag}(A))$.
LDL	a logical indicating if the simplicial factorization should be computed as $P_1' L_1 D L_1' P_1$, such that the result stores the lower triangular entries of $L_1 - I + D$. The alternative is $P_1' L L' P_1$, such that the result stores the lower triangular entries of $L = L_1 \sqrt{D}$. This argument is ignored if super = TRUE (or if super = NA and the supernodal algorithm is chosen), as the supernodal code does not yet support the LDL = TRUE variant.
super	a logical indicating if the factorization should use the supernodal algorithm. The alternative is the simplicial algorithm. Setting super = NA leaves the choice to a CHOLMOD-internal heuristic.
Imult	a finite number. The matrix that is factorized is $A + \text{Imult} * \text{diag}(\text{nrow}(A))$, i.e., A plus Imult times the identity matrix. This argument is useful for symmetric, indefinite A , as $\text{Imult} > \max(\text{rowSums}(\text{abs}(A)) - \text{diag}(\text{abs}(A)))$ ensures that $A + \text{Imult} * \text{diag}(\text{nrow}(A))$ is diagonally dominant. (Symmetric, diagonally dominant matrices are positive definite.)
uplo	a string, either "U" or "L", indicating which triangle of A should be used to compute the factorization. The default is "U", even for lower triangular A , to be consistent with chol from base.
...	further arguments passed to or from methods.

Details

Note that the result of a call to Cholesky inherits from [CholeskyFactorization](#) but not [Matrix](#). Users who just want a matrix should consider using [chol](#), whose methods are simple wrappers around Cholesky returning just the upper triangular Cholesky factor L' , typically as a [triangularMatrix](#). However, a more principled approach would be to construct factors as needed from the [CholeskyFactorization](#) object, e.g., with [expand1](#)(x, "L"), if x is the object.

The behaviour of `Cholesky(A, perm = TRUE)` for dense A is somewhat exceptional, in that it expects *without* checking that A is positive semidefinite. By construction, if A is positive semidefinite and the exact algorithm encounters a zero pivot, then the unfactorized trailing submatrix is the zero matrix, and there is nothing left to do. Hence when the finite precision algorithm encounters a pivot less than tol, it signals a warning instead of an error and zeros the trailing submatrix in order to guarantee that $P'LL'P$ is positive semidefinite even if A is not. It follows that one way to test for positive semidefiniteness of A in the event of a warning is to analyze the error

$$\frac{\|A - P'LL'P\|}{\|A\|}.$$

See the examples and LAPACK Working Note ("LAWN") 161 for details.

Value

An object representing the factorization, inheriting from virtual class `CholeskyFactorization`. For a traditional matrix A , the specific class is `Cholesky`. For A inheriting from `unpackedMatrix`, `packedMatrix`, and `sparseMatrix`, the specific class is `Cholesky`, `pCholesky`, and `dCHMsimpl` or `dCHMsuper`, respectively.

References

The LAPACK source code, including documentation; see <https://netlib.org/lapack/double/dpstrf.f>, <https://netlib.org/lapack/double/dpotrf.f>, and <https://netlib.org/lapack/double/dpptrf.f>.

The CHOLMOD source code; see <https://github.com/DrTimothyAldenDavis/SuiteSparse>, notably the header file `CHOLMOD/Include/cholmod.h` defining `cholmod_factor_struct`.

Lucas, C. (2004). *LAPACK-style codes for level 2 and 3 pivoted Cholesky factorizations*. LAPACK Working Note, Number 161. <https://www.netlib.org/lapack/lawnspdf/lawn161.pdf>

Chen, Y., Davis, T. A., Hager, W. W., & Rajamanickam, S. (2008). Algorithm 887: CHOLMOD, supernodal sparse Cholesky factorization and update/downdate. *ACM Transactions on Mathematical Software*, 35(3), Article 22, 1-14. doi:10.1145/1391989.1391995

Amestoy, P. R., Davis, T. A., & Duff, I. S. (2004). Algorithm 837: AMD, an approximate minimum degree ordering algorithm. *ACM Transactions on Mathematical Software*, 17(4), 886-905. doi:10.1145/1024074.1024081

Golub, G. H., & Van Loan, C. F. (2013). *Matrix computations* (4th ed.). Johns Hopkins University Press. doi:10.56021/9781421407944

See Also

Classes `Cholesky`, `pCholesky`, `dCHMsimpl` and `dCHMsuper` and their methods.

Classes `dpoMatrix`, `dppMatrix`, and `dsCMatrix`.

Generic function `chol`, for obtaining the upper triangular Cholesky factor L' as a matrix or `Matrix`.

Generic functions `expand1` and `expand2`, for constructing matrix factors from the result.

Generic functions `BunchKaufman`, `Schur`, `lu`, and `qr`, for computing other factorizations.

Examples

```
showMethods("Cholesky", inherited = FALSE)
set.seed(0)

## ---- Dense -----
## .... Positive definite .....

n <- 6L
(A1 <- crossprod(Matrix(rnorm(n * n), n, n)))
(ch.A1.nopivot <- Cholesky(A1, perm = FALSE))
(ch.A1 <- Cholesky(A1))
stopifnot(exprs = {
  length(ch.A1@perm) == ncol(A1)
```

```

    isPerm(ch.A1@perm)
    is.unsorted(ch.A1@perm) # typically not the identity permutation
    length(ch.A1.nopivot@perm) == 0L
  })

## A ~ P1' L D L' P1 ~ P1' L L' P1 in floating point
str(e.ch.A1 <- expand2(ch.A1, LDL = TRUE), max.level = 2L)
str(E.ch.A1 <- expand2(ch.A1, LDL = FALSE), max.level = 2L)
stopifnot(exprs = {
  all.equal(as(A1, "matrix"), as(Reduce(`%*%`, e.ch.A1), "matrix"))
  all.equal(as(A1, "matrix"), as(Reduce(`%*%`, E.ch.A1), "matrix"))
})

## .... Positive semidefinite but not positive definite .....

A2 <- A1
A2[1L, ] <- A2[, 1L] <- 0
A2
try(Cholesky(A2, perm = FALSE)) # fails as not positive definite
ch.A2 <- Cholesky(A2) # returns, with a warning and ...
A2.hat <- Reduce(`%*%`, expand2(ch.A2, LDL = FALSE))
norm(A2 - A2.hat, "2") / norm(A2, "2") # 7.670858e-17

## .... Not positive semidefinite .....

A3 <- A1
A3[1L, ] <- A3[, 1L] <- -1
A3
try(Cholesky(A3, perm = FALSE)) # fails as not positive definite
ch.A3 <- Cholesky(A3) # returns, with a warning and ...
A3.hat <- Reduce(`%*%`, expand2(ch.A3, LDL = FALSE))
norm(A3 - A3.hat, "2") / norm(A3, "2") # 1.781568

## Indeed, 'A3' is not positive semidefinite, but 'A3.hat' _is_
ch.A3.hat <- Cholesky(A3.hat)
A3.hat.hat <- Reduce(`%*%`, expand2(ch.A3.hat, LDL = FALSE))
norm(A3.hat - A3.hat.hat, "2") / norm(A3.hat, "2") # 1.777944e-16

## ---- Sparse -----

## Really just three cases modulo permutation :
##
##           type           factorization  minors of P1 A P1'
##  1 simplicial P1 A P1' = L1 D L1'      nonzero
##  2 simplicial P1 A P1' = L   L  '      positive
##  3 supernodal P1 A P2' = L   L  '      positive

data(KNex, package = "Matrix")
A4 <- crossprod(KNex[["mm"]])

ch.A4 <-
list(pivoted =
  list(simp11 = Cholesky(A4, perm = TRUE, super = FALSE, LDL = TRUE),

```

```

        simpl0 = Cholesky(A4, perm = TRUE, super = FALSE, LDL = FALSE),
        super0 = Cholesky(A4, perm = TRUE, super = TRUE
                           )),
    unpivoted =
    list(simpl1 = Cholesky(A4, perm = FALSE, super = FALSE, LDL = TRUE),
         simpl0 = Cholesky(A4, perm = FALSE, super = FALSE, LDL = FALSE),
         super0 = Cholesky(A4, perm = FALSE, super = TRUE
                           )))
ch.A4

s <- simplify2array
rapply2 <- function(object, f, ...) rapply(object, f, , , how = "list", ...)

s(rapply2(ch.A4, isLDL))
s(m.ch.A4 <- rapply2(ch.A4, expand1, "L")) # giving L = L1 sqrt(D)

## By design, the pivoted and simplicial factorizations
## are more sparse than the unpivoted and supernodal ones ...
s(rapply2(m.ch.A4, object.size))

## Which is nicely visualized by lattice-based methods for 'image'
inm <- c("pivoted", "unpivoted")
jnm <- c("simpl1", "simpl0", "super0")
for(i in 1:2)
  for(j in 1:3)
    print(image(m.ch.A4[[c(i, j)]], main = paste(inm[i], jnm[j])),
           split = c(j, i, 3L, 2L), more = i * j < 6L)

simpl1 <- ch.A4[[c("pivoted", "simpl1")]]
stopifnot(exprs = {
  length(simpl1@perm) == ncol(A4)
  isPerm(simpl1@perm, 0L)
  is.unsorted(simpl1@perm) # typically not the identity permutation
})

## One can expand with and without D regardless of isLDL(.),
## but "without" requires L = L1 sqrt(D), which is conditional
## on min(diag(D)) >= 0, hence "with" is the default
isLDL(simpl1)
stopifnot(min(diag(simpl1)) >= 0)
str(e.ch.A4 <- expand2(simpl1, LDL = TRUE), max.level = 2L) # default
str(E.ch.A4 <- expand2(simpl1, LDL = FALSE), max.level = 2L)
stopifnot(exprs = {
  all.equal(E.ch.A4[["L" ]], e.ch.A4[["L1" ]] %% sqrt(e.ch.A4[["D"]]))
  all.equal(E.ch.A4[["L." ]], sqrt(e.ch.A4[["D"]]) %% e.ch.A4[["L1." ]])
  all.equal(A4, as(Reduce(~%*~, e.ch.A4), "symmetricMatrix"))
  all.equal(A4, as(Reduce(~%*~, E.ch.A4), "symmetricMatrix"))
})

## The "same" permutation matrix with "alternate" representation
## [i, perm[i]] {margin=1} <-> [invertPerm(perm)[j], j] {margin=2}
alt <- function(P) {
  P@margin <- 1L + !(P@margin - 1L) # 1 <-> 2
  P@perm <- invertPerm(P@perm)
  P
}

```

```

}

## Expansions are elegant but inefficient (transposes are redundant)
## hence programmers should consider methods for 'expand1' and 'diag'
stopifnot(exprs = {
  identical(expand1(simpl1, "P1"), alt(e.ch.A4[["P1"]]))
  identical(expand1(simpl1, "L"), E.ch.A4[["L"]])
  identical(Diagonal(x = diag(simpl1)), e.ch.A4[["D"]])
})

## chol(A, pivot = value) is a simple wrapper around
## Cholesky(A, perm = value, LDL = FALSE, super = FALSE),
## returning L' = sqrt(D) L1' _but_ giving no information
## about the permutation P1
selectMethod("chol", "dsCMatrix")
stopifnot(all.equal(chol(A4, pivot = TRUE), E.ch.A4[["L."]]))

## Now a symmetric matrix with positive _and_ negative eigenvalues,
## hence _not_ positive semidefinite
A5 <- new("dsCMatrix",
  Dim = c(7L, 7L),
  p = c(0:1, 3L, 6:7, 10:11, 15L),
  i = c(0L, 0:1, 0:3, 2:5, 3:6),
  x = c(1, 6, 38, 10, 60, 103, -4, 6, -32, -247, -2, -16, -128, -2, -67))
(ev <- eigen(A5, only.values = TRUE)$values)
(t.ev <- table(factor(sign(ev), -1:1))) # the matrix "inertia"

ch.A5 <- Cholesky(A5)
isLDL(ch.A5)
(d.A5 <- diag(ch.A5)) # diag(D) is partly negative

## Sylvester's law of inertia holds here, but not in general
## in finite precision arithmetic
stopifnot(identical(table(factor(sign(d.A5), -1:1)), t.ev))

try(expand1(ch.A5, "L")) # unable to compute L = L1 sqrt(D)
try(expand2(ch.A5, LDL = FALSE)) # ditto
try(chol(A5, pivot = TRUE)) # ditto

## The default expansion is "square root free" and still works here
str(e.ch.A5 <- expand2(ch.A5, LDL = TRUE), max.level = 2L)
stopifnot(all.equal(A5, as(Reduce(~%*%~, e.ch.A5), "symmetricMatrix")))

## Version of the SuiteSparse library, which includes CHOLMOD
Mv <- Matrix.Version()
Mv[["suitsparse"]]

```

Description

Since 2005, package **Matrix** has supported coercions to and from class `graph` from package **igraph**. Since 2013, this functionality has been exposed via functions `T2graph` and `graph2T`, which, unlike methods for `as(from, "<Class>")`, support optional arguments.

Usage

```
graph2T(from, use.weights = )
T2graph(from, need.uniq = !isUniqueT(from), edgemode = NULL)
```

Arguments

<code>from</code>	for <code>graph2T()</code> , an R object of class "graph"; for <code>T2graph()</code> , a sparse matrix inheriting from " <code>TsparseMatrix</code> ".
<code>use.weights</code>	logical indicating if weights should be used, i.e., equivalently the result will be numeric, i.e. of class <code>dgMatrix</code> ; otherwise the result will be <code>ngMatrix</code> or <code>nsMatrix</code> , the latter if the graph is undirected. The default looks if there are weights in the graph, and if any differ from 1, weights are used.
<code>need.uniq</code>	a logical indicating if <code>from</code> may need to be internally "uniqified"; do not set this and hence rather use the default, unless you know what you are doing!
<code>edgemode</code>	one of <code>NULL</code> , "directed", or "undirected". The default <code>NULL</code> looks if the matrix is symmetric and assumes "undirected" in that case.

Value

For `graph2T()`, a sparse matrix inheriting from "`TsparseMatrix`".

For `T2graph()` an R object of class "graph".

See Also

Package **igraph**, which provides similar coercions to and from its class `igraph` via functions `graph_from_adjacency_matrix` and `as_adjacency_matrix`.

Examples

```
if(requireNamespace("igraph")) {
  n4 <- LETTERS[1:4]; dns <- list(n4,n4)
  show(a1 <- sparseMatrix(i= c(1:4), j=c(2:4,1), x = 2, dimnames=dns))
  show(g1 <- as(a1, "igraph")) # directed
  unlist(igraph::edgeWeights(g1)) # all '2'

  show(a2 <- sparseMatrix(i= c(1:4,4), j=c(2:4,1:2), x = TRUE, dimnames=dns))
  show(g2 <- as(a2, "igraph")) # directed
  # now if you want it undirected:
  show(g3 <- T2graph(as(a2,"TsparseMatrix"), edgemode="undirected"))
  show(m3 <- as(g3,"Matrix"))
  show( graph2T(g3) ) # a "pattern Matrix" (nsMatrix)

  a. <- sparseMatrix(i=4:1, j=1:4, dimnames=list(n4, n4), repr="T") # no 'x'
```



```

show(a.) # "ngTMatrix"
show(g. <- as(a., "graph"))

}

```

coerce-methods-SparseM

*Sparse Matrix Coercion from and to those from package **SparseM***

Description

Methods for coercion from and to sparse matrices from package **SparseM** are provided here, for ease of porting functionality to the **Matrix** package, and comparing functionality of the two packages. All these work via the usual `as(., "<class>")` coercion,

```
as(from, Class)
```

Methods

```

from = "matrix.csr", to = "dgRMatrix" ...
from = "matrix.csc", to = "dgCMatrix" ...
from = "matrix.coo", to = "dgTMatrix" ...
from = "dgRMatrix", to = "matrix.csr" ...
from = "dgCMatrix", to = "matrix.csc" ...
from = "dgTMatrix", to = "matrix.coo" ...
from = "Matrix", to = "matrix.csr" ...
from = "matrix.csr", to = "dgCMatrix" ...
from = "matrix.coo", to = "dgCMatrix" ...
from = "matrix.csr", to = "Matrix" ...
from = "matrix.csc", to = "Matrix" ...
from = "matrix.coo", to = "Matrix" ...

```

See Also

The documentation in CRAN package **SparseM**, such as [SparseM.ontology](#), and one important class, [matrix.csr](#).

Description

Form row and column sums and means for objects, for [sparseMatrix](#) the result may optionally be sparse ([sparseVector](#)), too. Row or column names are kept respectively as for **base** matrices and [colSums](#) methods, when the result is [numeric](#) vector.

Usage

```
colSums(x, na.rm = FALSE, dims = 1L, ...)
rowSums(x, na.rm = FALSE, dims = 1L, ...)
colMeans(x, na.rm = FALSE, dims = 1L, ...)
rowMeans(x, na.rm = FALSE, dims = 1L, ...)

## S4 method for signature 'CsparseMatrix'
colSums(x, na.rm = FALSE, dims = 1L,
        sparseResult = FALSE, ...)
## S4 method for signature 'CsparseMatrix'
rowSums(x, na.rm = FALSE, dims = 1L,
        sparseResult = FALSE, ...)
## S4 method for signature 'CsparseMatrix'
colMeans(x, na.rm = FALSE, dims = 1L,
         sparseResult = FALSE, ...)
## S4 method for signature 'CsparseMatrix'
rowMeans(x, na.rm = FALSE, dims = 1L,
         sparseResult = FALSE, ...)
```

Arguments

<code>x</code>	a Matrix , i.e., inheriting from Matrix .
<code>na.rm</code>	logical. Should missing values (including NaN) be omitted from the calculations?
<code>dims</code>	completely ignored by the Matrix methods.
<code>...</code>	potentially further arguments, for method <code><-></code> generic compatibility.
<code>sparseResult</code>	logical indicating if the result should be sparse, i.e., inheriting from class sparseVector . Only applicable when <code>x</code> is inheriting from a sparseMatrix class.

Value

returns a numeric vector if `sparseResult` is `FALSE` as per default. Otherwise, returns a [sparseVector](#). `dimnames(x)` are only kept (as `names(v)`) when the resulting `v` is [numeric](#), since [sparseVectors](#) do not have names.

See Also

[colSums](#) and the [sparseVector](#) classes.

Examples

```

(M <- bdiag(Diagonal(2), matrix(1:3, 3,4), diag(3:2))) # 7 x 8
colSums(M)
d <- Diagonal(10, c(0,0,10,0,2,rep(0,5)))
MM <- kronecker(d, M)
dim(MM) # 70 80
length(MM@x) # 160, but many are '0' ; drop those:
MM <- drop0(MM)
length(MM@x) # 32
cm <- colSums(MM)
(scm <- colSums(MM, sparseResult = TRUE))
stopifnot(is(scm, "sparseVector"),
           identical(cm, as.numeric(scm)))
rowSums (MM, sparseResult = TRUE) # 14 of 70 are not zero
colMeans(MM, sparseResult = TRUE) # 16 of 80 are not zero
## Since we have no 'NA's, these two are equivalent :
stopifnot(identical(rowMeans(MM, sparseResult = TRUE),
                    rowMeans(MM, sparseResult = TRUE, na.rm = TRUE)),
           rowMeans(Diagonal(16)) == 1/16,
           colSums(Diagonal(7)) == 1)

## dimnames(x) --> names( <value> ) :
dimnames(M) <- list(paste0("r", 1:7), paste0("v",1:8))
M
colSums(M)
rowMeans(M)
## Assertions :
stopifnot(exprs = {
  all.equal(colSums(M),
            structure(c(1,1,6,6,6,6,3,2), names = colnames(M)))
  all.equal(rowMeans(M),
            structure(c(1,1,4,8,12,3,2)/8, names = paste0("r", 1:7)))
})

```

condest

Compute Approximate CONDITION number and 1-Norm of (Large) Matrices

Description

“Estimate”, i.e. compute approximately the CONDITION number of a (potentially large, often sparse) matrix A. It works by apply a fast *randomized* approximation of the 1-norm, $\text{norm}(A, "1")$, through `onenormest(.)`.

Usage

```

condest(A, t = min(n, 5), normA = norm(A, "1"),
        silent = FALSE, quiet = TRUE)

```

```
onenormest(A, t = min(n, 5), A.x, At.x, n,
           silent = FALSE, quiet = silent,
           iter.max = 10, eps = 4 * .Machine$double.eps)
```

Arguments

A	a square matrix, optional for <code>onenormest()</code> , where instead of A, A.x and At.x can be specified, see there.
t	number of columns to use in the iterations.
normA	number; (an estimate of) the 1-norm of A, by default <code>norm(A, "1")</code> ; may be replaced by an estimate.
silent	logical indicating if warning and (by default) convergence messages should be displayed.
quiet	logical indicating if convergence messages should be displayed.
A.x, At.x	when A is missing, these two must be given as functions which compute <code>A %% x</code> , or <code>t(A) %% x</code> , respectively.
n	<code>== nrow(A)</code> , only needed when A is not specified.
iter.max	maximal number of iterations for the 1-norm estimator.
eps	the relative change that is deemed irrelevant.

Details

`condest()` calls `lu(A)`, and subsequently `onenormest(A.x = , At.x =)` to compute an approximate norm of the *inverse* of A, A^{-1} , in a way which keeps using sparse matrices efficiently when A is sparse.

Note that `onenormest()` uses random vectors and hence *both* functions' results are random, i.e., depend on the random seed, see, e.g., `set.seed()`.

Value

Both functions return a **list**; `condest()` with components,

est	a number > 0 , the estimated (1-norm) condition number $\hat{\kappa}$; when $r := rcond(A)$, $1/\hat{\kappa} \approx r$.
v	the maximal Ax column, scaled to $norm(v) = 1$. Consequently, $norm(Av) = norm(A)/est$; when est is large, v is an approximate null vector.

The function `onenormest()` returns a list with components,

est	a number > 0 , the estimated <code>norm(A, "1")</code> .
v	0-1 integer vector length n, with an 1 at the index j with maximal column <code>A[, j]</code> in A.
w	numeric vector, the largest Ax found.
iter	the number of iterations used.

Author(s)

This is based on octave's `condest()` and `onenormest()` implementations with original author Jason Riedy, U Berkeley; translation to R and adaption by Martin Maechler.

References

Nicholas J. Higham and Françoise Tisseur (2000). A Block Algorithm for Matrix 1-Norm Estimation, with an Application to 1-Norm Pseudospectra. *SIAM J. Matrix Anal. Appl.* **21**, 4, 1185–1201.

William W. Hager (1984). Condition Estimates. *SIAM J. Sci. Stat. Comput.* **5**, 311–316.

See Also

[norm](#), [rcond](#).

Examples

```
data(KNex, package = "Matrix")
mtm <- with(KNex, crossprod(mm))
system.time(ce <- condest(mtm))
sum(abs(ce$v)) ## || v ||_1 == 1
## Prove that || A v || = || A || / est (as ||v|| = 1):
stopifnot(all.equal(norm(mtm %*% ce$v),
                    norm(mtm) / ce$est))

## reciprocal
1 / ce$est
system.time(rc <- rcond(mtm)) # takes ca 3 x longer
rc
all.equal(rc, 1/ce$est) # TRUE -- the approximation was good

one <- onenormest(mtm)
str(one) ## est = 12.3
## the maximal column:
which(one$v == 1) # mostly 4, rarely 1, depending on random seed
```

CsparseMatrix-class *Class "CsparseMatrix" of Sparse Matrices in Column-compressed Form*

Description

The "CsparseMatrix" class is the virtual class of all sparse matrices coded in sorted compressed column-oriented form. Since it is a virtual class, no objects may be created from it. See `showClass("CsparseMatrix")` for its subclasses.

Slots

- i**: Object of class "integer" of length nnzero (number of non-zero elements). These are the 0-based row numbers for each non-zero element in the matrix, i.e., i must be in 0:(nrow(.)-1).
- p**: integer vector for providing pointers, one for each column, to the initial (zero-based) index of elements in the column. .@p is of length ncol(.) + 1, with p[1] == 0 and p[length(p)] == nnzero, such that in fact, diff(.@p) are the number of non-zero elements for each column. In other words, m@p[1:ncol(m)] contains the indices of those elements in m@x that are the first elements in the respective column of m.
- Dim, Dimnames: inherited from the superclass, see the `sparseMatrix` class.

Extends

Class "sparseMatrix", directly. Class "Matrix", by class "sparseMatrix".

Methods

matrix products `%*%`, `crossprod()` and `tcrossprod()`, several `solve` methods, and other matrix methods available:

`signature(e1 = "CsparseMatrix", e2 = "numeric"): ...`

Arith `signature(e1 = "numeric", e2 = "CsparseMatrix"): ...`

Math `signature(x = "CsparseMatrix"): ...`

band `signature(x = "CsparseMatrix"): ...`

- `signature(e1 = "CsparseMatrix", e2 = "numeric"): ...`

- `signature(e1 = "numeric", e2 = "CsparseMatrix"): ...`

+ `signature(e1 = "CsparseMatrix", e2 = "numeric"): ...`

+ `signature(e1 = "numeric", e2 = "CsparseMatrix"): ...`

coerce `signature(from = "CsparseMatrix", to = "TsparseMatrix"): ...`

coerce `signature(from = "CsparseMatrix", to = "denseMatrix"): ...`

coerce `signature(from = "CsparseMatrix", to = "matrix"): ...`

coerce `signature(from = "TsparseMatrix", to = "CsparseMatrix"): ...`

coerce `signature(from = "denseMatrix", to = "CsparseMatrix"): ...`

diag `signature(x = "CsparseMatrix"): ...`

gamma `signature(x = "CsparseMatrix"): ...`

lgamma `signature(x = "CsparseMatrix"): ...`

log `signature(x = "CsparseMatrix"): ...`

t `signature(x = "CsparseMatrix"): ...`

tril `signature(x = "CsparseMatrix"): ...`

triu `signature(x = "CsparseMatrix"): ...`

Note

All classes extending `CsparseMatrix` have a common validity (see `validObject`) check function. That function additionally checks the `i` slot for each column to contain increasing row numbers. In earlier versions of **Matrix** ($\leq 0.999375-16$), `validObject` automatically re-sorted the entries when necessary, and hence `new()` calls with somewhat permuted `i` and `x` slots worked, as `new(...)` (*with* slot arguments) automatically checks the validity.

Now, you have to use `sparseMatrix` to achieve the same functionality or know how to use `.validateCsparse()` to do so.

See Also

`colSums`, `kronecker`, and other such methods with own help pages.

Further, the super class of `CsparseMatrix`, `sparseMatrix`, and, e.g., class `dgCMatrix` for the links to other classes.

Examples

```
getClass("CsparseMatrix")

## The common validity check function (based on C code):
getValidity(getClass("CsparseMatrix"))
```

ddenseMatrix-class *Virtual Class "ddenseMatrix" of Numeric Dense Matrices*

Description

This is the virtual class of all dense numeric (i.e., `double`, hence “*ddense*”) S4 matrices.

Its most important subclass is the `dgeMatrix` class.

Extends

Class “`dMatrix`” directly; class “`Matrix`”, by the above.

Slots

the same slots at its subclass `dgeMatrix`, see there.

Methods

Most methods are implemented via `as(*, "generalMatrix")` and are mainly used as “fallbacks” when the subclass doesn’t need its own specialized method.

Use `showMethods(class = "ddenseMatrix", where = "package:Matrix")` for an overview.

See Also

The virtual classes `Matrix`, `dMatrix`, and `dsparseMatrix`.

Examples

```
showClass("ddenseMatrix")

showMethods(class = "ddenseMatrix", where = "package:Matrix")
```

```
ddiMatrix-class      Class "ddiMatrix" of Diagonal Numeric Matrices
```

Description

The class "ddiMatrix" of numerical diagonal matrices. Note that diagonal matrices now extend `sparseMatrix`, whereas they did extend dense matrices earlier.

Objects from the Class

Objects can be created by calls of the form `new("ddiMatrix", ...)` but typically rather via [Diagonal](#).

Slots

x: numeric vector. For an $n \times n$ matrix, the x slot is of length n or \emptyset , depending on the `diag` slot:
diag: "character" string, either "U" or "N" where "U" denotes unit-diagonal, i.e., identity matrices.
Dim,Dimnames: matrix dimension and `dimnames`, see the [Matrix](#) class description.

Extends

Class "[diagonalMatrix](#)", directly. Class "[dMatrix](#)", directly. Class "[sparseMatrix](#)", indirectly, see `showClass("ddiMatrix")`.

Methods

```
%*% signature(x = "ddiMatrix", y = "ddiMatrix"): ...
```

See Also

Class [diagonalMatrix](#) and function [Diagonal](#).

Examples

```
(d2 <- Diagonal(x = c(10,1)))
str(d2)
## slightly larger in internal size:
str(as(d2, "sparseMatrix"))

M <- Matrix(cbind(1,2:4))
M %*% d2 #> `fast' multiplication

chol(d2) # trivial
```



```
stopifnot(is(cd2 <- chol(d2), "ddiMatrix"),
          all.equal(cd2@x, c(sqrt(10),1)))
```

denseLU-class *Dense LU Factorizations*

Description

denseLU is the class of dense, row-pivoted LU factorizations of $m \times n$ real matrices A , having the general form

$$P_1 A = LU$$

or (equivalently)

$$A = P_1' LU$$

where P_1 is an $m \times m$ permutation matrix, L is an $m \times \min(m, n)$ unit lower trapezoidal matrix, and U is a $\min(m, n) \times n$ upper trapezoidal matrix. If $m = n$, then the factors L and U are triangular.

Slots

Dim, Dimnames inherited from virtual class [MatrixFactorization](#).

x a numeric vector of length `prod(Dim)` storing the triangular L and U factors together in a packed format. The details of the representation are specified by the manual for LAPACK routine `dgetrf`.

perm an integer vector of length `min(Dim)` specifying the permutation P_1 as a product of transpositions. The corresponding permutation vector can be obtained as `asPerm(perm)`.

Extends

Class [LU](#), directly. Class [MatrixFactorization](#), by class [LU](#), distance 2.

Instantiation

Objects can be generated directly by calls of the form `new("denseLU", ...)`, but they are more typically obtained as the value of `lu(x)` for x inheriting from [denseMatrix](#) (often [dgeMatrix](#)).

Methods

`coerce` signature(`from = "denseLU"`, `to = "dgeMatrix"`): returns a [dgeMatrix](#) with the dimensions of the factorized matrix A , equal to L below the diagonal and equal to U on and above the diagonal.

`determinant` signature(`from = "denseLU"`, `logarithm = "logical"`): computes the determinant of the factorized matrix A or its logarithm.

`expand` signature(`x = "denseLU"`): see [expand-methods](#).

`expand1` signature(`x = "denseLU"`): see [expand1-methods](#).

`expand2` signature(`x = "denseLU"`): see [expand2-methods](#).

`solve` signature(`a = "denseLU"`, `b = "missing"`): see [solve-methods](#).

References

The LAPACK source code, including documentation; see <https://netlib.org/lapack/double/dgetrf.f>.

Golub, G. H., & Van Loan, C. F. (2013). *Matrix computations* (4th ed.). Johns Hopkins University Press. doi:10.56021/9781421407944

See Also

Class [sparseLU](#) for sparse LU factorizations.

Class [dgeMatrix](#).

Generic functions [lu](#), [expand1](#) and [expand2](#).

Examples

```
showClass("denseLU")
set.seed(1)

n <- 3L
(A <- Matrix(round(rnorm(n * n), 2L), n, n))

## With dimnames, to see that they are propagated :
dimnames(A) <- dn <- list(paste0("r", seq_len(n)),
                        paste0("c", seq_len(n)))

(lu.A <- lu(A))
str(e.lu.A <- expand2(lu.A), max.level = 2L)

## Underlying LAPACK representation
(m.lu.A <- as(lu.A, "dgeMatrix")) # which is L and U interlaced
stopifnot(identical(as(m.lu.A, "matrix"), `dim<-`(lu.A@x, lu.A@Dim)))

ae1 <- function(a, b, ...) all.equal(as(a, "matrix"), as(b, "matrix"), ...)
ae2 <- function(a, b, ...) ae1(unname(a), unname(b), ...)

## A ~ P1' L U in floating point
stopifnot(exprs = {
  identical(names(e.lu.A), c("P1.", "L", "U"))
  identical(e.lu.A[["P1."],
            new("pMatrix", Dim = c(n, n), Dimnames = c(dn[1L], list(NULL)),
              margin = 1L, perm = invertPerm(asPerm(lu.A@perm))))
  identical(e.lu.A[["L"]],
            new("dtrMatrix", Dim = c(n, n), Dimnames = list(NULL, NULL),
              uplo = "L", diag = "U", x = lu.A@x))
  identical(e.lu.A[["U"]],
            new("dtrMatrix", Dim = c(n, n), Dimnames = c(list(NULL), dn[2L]),
              uplo = "U", diag = "N", x = lu.A@x))
  ae1(A, with(e.lu.A, P1. %%% L %%% U))
  ae2(A[asPerm(lu.A@perm), ], with(e.lu.A, L %%% U))
})
```

```
## Factorization handled as factorized matrix
b <- rnorm(n)
stopifnot(identical(det(A), det(lu.A)),
           identical(solve(A, b), solve(lu.A, b)))
```

denseMatrix-class *Virtual Class "denseMatrix" of All Dense Matrices*

Description

This is the virtual class of all dense (S4) matrices. It partitions into two subclasses [packedMatrix](#) and [unpackedMatrix](#). Alternatively into the (currently) three subclasses [ddenseMatrix](#), [ldenseMatrix](#), and [ndenseMatrix](#).

`denseMatrix` is (hence) the direct superclass of these (2 + 3 = 5) classes.

Extends

class "Matrix" directly.

Slots

exactly those of its superclass "[Matrix](#)", i.e., "Dim" and "Dimnames".

Methods

Use [showMethods](#)(class = "denseMatrix", where = "package:Matrix") for an overview of methods.

Extraction ("[\[](#)") methods, see [\[](#)-methods.

See Also

[colSums](#), [kronecker](#), and other such methods with own help pages.

Its superclass [Matrix](#), and main subclasses, [ddenseMatrix](#) and [sparseMatrix](#).

Examples

```
showClass("denseMatrix")
```

dgCMatrix-class *Compressed, sparse, column-oriented numeric matrices*

Description

The dgCMatrix class is a class of sparse numeric matrices in the compressed, sparse, column-oriented format. In this implementation the non-zero elements in the columns are sorted into increasing row order. dgCMatrix is the “*standard*” class for sparse numeric matrices in the **Matrix** package.

Objects from the Class

Objects can be created by calls of the form `new("dgCMatrix", ...)`, more typically via `as(*, "CsparseMatrix")` or similar. Often however, more easily via `Matrix(*, sparse = TRUE)`, or most efficiently via `sparseMatrix()`.

Slots

x: Object of class "numeric" - the non-zero elements of the matrix.
 ... all other slots are inherited from the superclass "CsparseMatrix".

Methods

Matrix products (e.g., [crossprod-methods](#)), and (among other)

coerce signature(from = "matrix", to = "dgCMatrix")

diag signature(x = "dgCMatrix"): returns the diagonal of x

dim signature(x = "dgCMatrix"): returns the dimensions of x

image signature(x = "dgCMatrix"): plots an image of x using the [levelplot](#) function

solve signature(a = "dgCMatrix", b = "..."): see [solve-methods](#), notably the extra argument `sparse`.

lu signature(x = "dgCMatrix"): computes the LU decomposition of a square dgCMatrix object

See Also

Classes [dsCMatrix](#), [dtCMatrix](#), [lu](#)

Examples

```
(m <- Matrix(c(0,0,2:0), 3,5))
str(m)
m[,1]
```

dgeMatrix-class *Class "dgeMatrix" of Dense Numeric (S4 Class) Matrices*

Description

A general numeric dense matrix in the S4 Matrix representation. `dgeMatrix` is the “*standard*” class for dense numeric matrices in the **Matrix** package.

Objects from the Class

Objects can be created by calls of the form `new("dgeMatrix", ...)` or, more commonly, by coercion from the `Matrix` class (see [Matrix](#)) or by `Matrix(...)`.

Slots

x: Object of class "numeric" - the numeric values contained in the matrix, in column-major order.

Dim: Object of class "integer" - the dimensions of the matrix - must be an integer vector with exactly two non-negative values.

Dimnames: a list of length two - inherited from class [Matrix](#).

factors: Object of class "list" - a list of factorizations of the matrix.

Methods

The are group methods (see, e.g., [Arith](#))

Arith signature(e1 = "dgeMatrix", e2 = "dgeMatrix"): ...

Arith signature(e1 = "dgeMatrix", e2 = "numeric"): ...

Arith signature(e1 = "numeric", e2 = "dgeMatrix"): ...

Math signature(x = "dgeMatrix"): ...

Math2 signature(x = "dgeMatrix", digits = "numeric"): ...

matrix products `%*%`, [crossprod\(\)](#) and [tcrossprod\(\)](#), several [solve](#) methods, and other matrix methods available:

Schur signature(x = "dgeMatrix", vectors = "logical"): ...

Schur signature(x = "dgeMatrix", vectors = "missing"): ...

chol signature(x = "dgeMatrix"): see [chol](#).

colMeans signature(x = "dgeMatrix"): columnwise means (averages)

colSums signature(x = "dgeMatrix"): columnwise sums

diag signature(x = "dgeMatrix"): ...

dim signature(x = "dgeMatrix"): ...

dimnames signature(x = "dgeMatrix"): ...

eigen signature(x = "dgeMatrix", only.values = "logical"): ...

eigen signature(x = "dgeMatrix", only.values= "missing"): ...
norm signature(x = "dgeMatrix", type = "character"): ...
norm signature(x = "dgeMatrix", type = "missing"): ...
rcond signature(x = "dgeMatrix", norm = "character") or norm = "missing": the reciprocal condition number, [rcond\(\)](#).
rowMeans signature(x = "dgeMatrix"): rowwise means (averages)
rowSums signature(x = "dgeMatrix"): rowwise sums
t signature(x = "dgeMatrix"): matrix transpose

See Also

Classes [Matrix](#), [dtrMatrix](#), and [dsyMatrix](#).

dgRMatrix-class

Sparse Compressed, Row-oriented Numeric Matrices

Description

The `dgRMatrix` class is a class of sparse numeric matrices in the compressed, sparse, row-oriented format. In this implementation the non-zero elements in the rows are sorted into increasing column order.

Note: The column-oriented sparse classes, e.g., [dgCMatrix](#), are preferred and better supported in the **Matrix** package.

Objects from the Class

Objects can be created by calls of the form `new("dgRMatrix", ...)`.

Slots

j: Object of class "integer" of length `nnzero` (number of non-zero elements). These are the column numbers for each non-zero element in the matrix.
p: Object of class "integer" of pointers, one for each row, to the initial (zero-based) index of elements in the row.
x: Object of class "numeric" - the non-zero elements of the matrix.
Dim: Object of class "integer" - the dimensions of the matrix.

Methods

diag signature(x = "dgRMatrix"): returns the diagonal of x
dim signature(x = "dgRMatrix"): returns the dimensions of x
image signature(x = "dgRMatrix"): plots an image of x using the [levelplot](#) function

See Also

the [RsparseMatrix](#) class, the virtual class of all sparse compressed row-oriented matrices, with its methods. The [dgCMatrix](#) class (column compressed sparse) is really preferred.

 dgTMatrix-class *Sparse matrices in triplet form*

Description

The "dgTMatrix" class is the class of sparse matrices stored as (possibly redundant) triplets. The internal representation is not at all unique, contrary to the one for class [dgCMatrix](#).

Objects from the Class

Objects can be created by calls of the form `new("dgTMatrix", ...)`, but more typically via [spMatrix\(\)](#) or [sparseMatrix\(*, repr = "T"\)](#).

Slots

- i**: [integer](#) row indices of non-zero entries *in 0-base*, i.e., must be in $0:(nrow(.)-1)$.
- j**: [integer](#) column indices of non-zero entries. Must be the same length as slot **i** and *0-based* as well, i.e., in $0:(ncol(.)-1)$.
- x**: [numeric](#) vector - the (non-zero) entry at position (i, j) . Must be the same length as slot **i**. If an index pair occurs more than once, the corresponding values of slot **x** are added to form the element of the matrix.
- Dim**: Object of class "integer" of length 2 - the dimensions of the matrix.

Methods

- +** `signature(e1 = "dgTMatrix", e2 = "dgTMatrix")`
- image** `signature(x = "dgTMatrix")`: plots an image of **x** using the [levelplot](#) function
- t** `signature(x = "dgTMatrix")`: returns the transpose of **x**

Note

Triplet matrices are a convenient form in which to construct sparse matrices after which they can be coerced to [dgCMatrix](#) objects.

Note that both `new(.)` and `spMatrix` constructors for "dgTMatrix" (and other "TsparseMatrix" classes) implicitly add x_k 's that belong to identical (i_k, j_k) pairs.

However this means that a matrix typically can be stored in more than one possible "TsparseMatrix" representations. Use [asUniqueT\(\)](#) in order to ensure uniqueness of the internal representation of such a matrix.

See Also

Class [dgCMatrix](#) or the superclasses [dsparseMatrix](#) and [TsparseMatrix](#); [asUniqueT](#).

Examples

```

m <- Matrix(0+1:28, nrow = 4)
m[-3,c(2,4:5,7)] <- m[ 3, 1:4] <- m[1:3, 6] <- 0
(mT <- as(m, "TsparseMatrix"))
str(mT)
mT[1,]
mT[4, drop = FALSE]
stopifnot(identical(mT[lower.tri(mT)],
                    m [lower.tri(m) ]))
mT[lower.tri(mT,diag=TRUE)] <- 0
mT

## Triplet representation with repeated (i,j) entries
## *adds* the corresponding x's:
T2 <- new("dgTMatrix",
          i = as.integer(c(1,1,0,3,3)),
          j = as.integer(c(2,2,4,0,0)), x=10*1:5, Dim=4:5)
str(T2) # contains (i,j,x) slots exactly as above, but
T2 ## has only three non-zero entries, as for repeated (i,j)'s,
## the corresponding x's are "implicitly" added
stopifnot(nnzero(T2) == 3)

```

Diagonal

Construct a Diagonal Matrix

Description

Construct a formally diagonal [Matrix](#), i.e., an object inheriting from virtual class [diagonalMatrix](#) (or, if desired, a *mathematically* diagonal [CsparseMatrix](#)).

Usage

```
Diagonal(n, x = NULL, names = FALSE)
```

```

.sparseDiagonal(n, x = NULL, uplo = "U", shape = "t", unitri = TRUE, kind, cols)
.trDiagonal(n, x = NULL, uplo = "U", unitri = TRUE, kind)
.symDiagonal(n, x = NULL, uplo = "U", kind)

```

Arguments

n	integer indicating the dimension of the (square) matrix. If missing, then <code>length(x)</code> is used.
x	numeric or logical vector listing values for the diagonal entries, to be recycled as necessary. If <code>NULL</code> (the default), then the result is a unit diagonal matrix. <code>.sparseDiagonal()</code> and friends ignore non- <code>NULL</code> x when <code>kind = "n"</code> .
names	either logical <code>TRUE</code> or <code>FALSE</code> or then a character vector of <code>length</code> n. If true <i>and</i> <code>names(x)</code> is not <code>NULL</code> , use that as both row and column names for the resulting matrix. When a character vector, use it for both dimnames.

uplo	one of c("U", "L"), specifying the uplo slot of the result if the result is formally triangular or symmetric.
shape	one of c("t", "s", "g"), indicating if the result should be formally triangular, symmetric, or "general". The result will inherit from virtual class triangularMatrix , symmetricMatrix , or generalMatrix , respectively.
unitri	logical indicating if a formally triangular result with ones on the diagonal should be formally <i>unit</i> triangular, i.e., with diag slot equal to "U" rather than "N".
kind	one of c("d", "l", "n"), indicating the "mode" of the result: numeric, logical, or pattern. The result will inherit from virtual class dsparseMatrix , lsparseMatrix , or nsparseMatrix , respectively. Values other than "n" are ignored when x is non-NULL; in that case the mode is determined by <code>typeof(x)</code> .
cols	optional integer vector with values in 0:(n-1), indexing columns of the specified diagonal matrix. If specified, then the result is (mathematically) $D[, \text{cols}+1]$ rather than D, where $D = \text{Diagonal}(n, x)$, and it is always "general" (i.e., shape is ignored).

Value

`Diagonal()` returns an object inheriting from virtual class [diagonalMatrix](#).

`.sparseDiagonal()` returns a [CsparseMatrix](#) representation of `Diagonal(n, x)` or, if `cols` is given, of `Diagonal(n, x)[, cols+1]`. The precise class of the result depends on `shape` and `kind`.

`.trDiagonal()` and `.symDiagonal()` are simple wrappers, for `.sparseDiagonal(shape = "t")` and `.sparseDiagonal(shape = "s")`, respectively.

`.sparseDiagonal()` exists primarily to leverage efficient C-level methods available for [CsparseMatrix](#).

Author(s)

Martin Maechler

See Also

the generic function [diag](#) for *extraction* of the diagonal from a matrix works for all "Matrices".

[bandSparse](#) constructs a *banded* sparse matrix from its non-zero sub-/super - diagonals. [band\(A\)](#) returns a band matrix containing some sub-/super - diagonals of A.

[Matrix](#) for general matrix construction; further, class [diagonalMatrix](#).

Examples

```
Diagonal(3)
Diagonal(x = 10^(3:1))
Diagonal(x = (1:4) >= 2)#-> "ldiMatrix"

## Use Diagonal() + kronecker() for "repeated-block" matrices:
M1 <- Matrix(0+0:5, 2,3)
(M <- kronecker(Diagonal(3), M1))

(S <- crossprod(Matrix(rbinom(60, size=1, prob=0.1), 10,6)))
```

```
(SI <- S + 10*.symDiagonal(6)) # sparse symmetric still
stopifnot(is(SI, "dsCMatrix"))
(I4 <- .sparseDiagonal(4, shape="t"))# now (2012-10) unitriangular
stopifnot(I4@diag == "U", all(I4 == diag(4)))
```

diagonalMatrix-class *Class "diagonalMatrix" of Diagonal Matrices*

Description

Class "diagonalMatrix" is the virtual class of all diagonal matrices.

Objects from the Class

A virtual Class: No objects may be created from it.

Slots

diag: [character](#) string, either "U" or "N", where "U" means 'unit-diagonal'.

Dim: matrix dimension, and

Dimnames: the [dimnames](#), a [list](#), see the [Matrix](#) class description. Typically `list(NULL, NULL)` for diagonal matrices.

Extends

Class "[sparseMatrix](#)", directly.

Methods

These are just a subset of the signature for which defined methods. Currently, there are (too) many explicit methods defined in order to ensure efficient methods for diagonal matrices.

coerce signature(from = "matrix", to = "diagonalMatrix"): ...

coerce signature(from = "Matrix", to = "diagonalMatrix"): ...

coerce signature(from = "diagonalMatrix", to = "generalMatrix"): ...

coerce signature(from = "diagonalMatrix", to = "triangularMatrix"): ...

coerce signature(from = "diagonalMatrix", to = "nMatrix"): ...

coerce signature(from = "diagonalMatrix", to = "matrix"): ...

coerce signature(from = "diagonalMatrix", to = "sparseVector"): ...

t signature(x = "diagonalMatrix"): ...

and many more methods

solve signature(a = "diagonalMatrix", b, ...): is trivially implemented, of course; see also [solve-methods](#).

which signature(x = "nMatrix"), semantically equivalent to **base** function [which](#)(x, arr.ind).

"Math" signature(x = "diagonalMatrix"): all these group methods return a "diagonalMatrix", apart from `cumsum()` etc which return a *vector* also for **base matrix**.

* signature(e1 = "ddiMatrix", e2="denseMatrix"): arithmetic and other operators from the **Ops** group have a few dozen explicit method definitions, in order to keep the results *diagonal* in many cases, including the following:

/ signature(e1 = "ddiMatrix", e2="denseMatrix"): the result is from class `ddiMatrix` which is typically very desirable. Note that when e2 contains off-diagonal zeros or **NA**s, we implicitly use $0/x = 0$, hence differing from traditional R arithmetic (where $0/0 \mapsto \text{NaN}$), in order to preserve sparsity.

summary (object = "diagonalMatrix"): Returns an object of S3 class "diagSummary" which is the summary of the vector object@x plus a simple heading, and an appropriate **print** method.

See Also

`Diagonal()` as constructor of these matrices, and `isDiagonal`. `ddiMatrix` and `ldiMatrix` are "actual" classes extending "diagonalMatrix".

Examples

```
I5 <- Diagonal(5)
D5 <- Diagonal(x = 10*(1:5))
## trivial (but explicitly defined) methods:
stopifnot(identical(crossprod(I5), I5),
           identical(tcrossprod(I5), I5),
           identical(crossprod(I5, D5), D5),
           identical(tcrossprod(D5, I5), D5),
           identical(solve(D5), solve(D5, I5)),
           all.equal(D5, solve(solve(D5)), tolerance = 1e-12)
           )
solve(D5)# efficient as is diagonal

# an unusual way to construct a band matrix:
rbind2(cbind2(I5, D5),
       cbind2(D5, I5))
```

diagU2N

Transform Triangular Matrices from Unit Triangular to General Triangular and Back

Description

Transform a triangular matrix x, i.e., of class `triangularMatrix`, from (internally!) unit triangular ("unitriangular") to "general" triangular (`diagU2N(x)`) or back (`diagN2U(x)`). Note that the latter, `diagN2U(x)`, also sets the diagonal to one in cases where `diag(x)` was not all one.

`.diagU2N(x)` and `.diagN2U(x)` assume *without* checking that x is a `triangularMatrix` with suitable `diag` slot ("U" and "N", respectively), hence they should be used with care.

Usage

```
diagU2N(x, cl = getClassDef(class(x)), checkDense = FALSE)
diagN2U(x, cl = getClassDef(class(x)), checkDense = FALSE)

.diagU2N(x, cl = getClassDef(class(x)), checkDense = FALSE)
.diagN2U(x, cl = getClassDef(class(x)), checkDense = FALSE)
```

Arguments

`x` a [triangularMatrix](#), often sparse.

`cl` (optional, for speedup only:) class (definition) of `x`.

`checkDense` logical indicating if dense (see [denseMatrix](#)) matrices should be considered at all; i.e., when false, as per default, the result will be sparse even when `x` is dense.

Details

The concept of unit triangular matrices with a diag slot of "U" stems from LAPACK.

Value

a triangular matrix of the same [class](#) but with a different diag slot. For `diagU2N` (semantically) with identical entries as `x`, whereas in `diagN2U(x)`, the off-diagonal entries are unchanged and the diagonal is set to all 1 even if it was not previously.

Note

Such internal storage details should rarely be of relevance to the user. Hence, these functions really are rather *internal* utilities.

See Also

["triangularMatrix"](#), ["dtCMatrix"](#).

Examples

```
(T <- Diagonal(7) + triu(Matrix(rpois(49, 1/4), 7, 7), k = 1))
(uT <- diagN2U(T)) # "unitriangular"
(t.u <- diagN2U(10*T)) # changes the diagonal!
stopifnot(all(T == uT), diag(t.u) == 1,
          identical(T, diagU2N(uT)))
T[upper.tri(T)] <- 5 # still "dtC"
T <- diagN2U(as(T,"triangularMatrix"))
dT <- as(T, "denseMatrix") # (unitriangular)
dT.n <- diagU2N(dT, checkDense = TRUE)
sT.n <- diagU2N(dT)
stopifnot(is(dT.n, "denseMatrix"), is(sT.n, "sparseMatrix"),
          dT@diag == "U", dT.n@diag == "N", sT.n@diag == "N",
          all(dT == dT.n), all(dT == sT.n))
```

dimScale

Scale the Rows and Columns of a Matrix

Description

`dimScale`, `rowScale`, and `colScale` implement $D1 \%*\% x \%*\% D2$, $D \%*\% x$, and $x \%*\% D$ for diagonal matrices $D1$, $D2$, and D with diagonal entries $d1$, $d2$, and d , respectively. Unlike the explicit products, these functions preserve `dimnames(x)` and symmetry where appropriate.

Usage

```
dimScale(x, d1 = sqrt(1/diag(x, names = FALSE)), d2 = d1)
rowScale(x, d)
colScale(x, d)
```

Arguments

`x` a matrix, possibly inheriting from virtual class `Matrix`.
`d1, d2, d` numeric vectors giving factors by which to scale the rows or columns of `x`; they are recycled as necessary.

Details

`dimScale(x)` (with `d1` and `d2` unset) is only roughly equivalent to `cov2cor(x)`. `cov2cor` sets the diagonal entries of the result to 1 (exactly); `dimScale` does not.

Value

The result of scaling `x`, currently always inheriting from virtual class `dMatrix`.

It inherits from `triangularMatrix` if and only if `x` does. In the special case of `dimScale(x, d1, d2)` with identical `d1` and `d2`, it inherits from `symmetricMatrix` if and only if `x` does.

Author(s)

Mikael Jagan

See Also

[cov2cor](#)

Examples

```
n <- 6L
(x <- forceSymmetric(matrix(1, n, n)))
dimnames(x) <- rep.int(list(letters[seq_len(n)]), 2L)

d <- seq_len(n)
(D <- Diagonal(x = d))
```

```
(scx <- dimScale(x, d)) # symmetry and 'dimnames' kept
(mmx <- D %*% x %*% D) # symmetry and 'dimnames' lost
stopifnot(identical(unname(as(scx, "generalMatrix")), mmx))

rowScale(x, d)
colScale(x, d)
```

dMatrix-class

(Virtual) Class "dMatrix" of "double" Matrices

Description

The `dMatrix` class is a virtual class contained by all actual classes of numeric matrices in the **Matrix** package. Similarly, all the actual classes of logical matrices inherit from the `lMatrix` class.

Slots

Common to *all* matrix object in the package:

Dim: Object of class "integer" - the dimensions of the matrix - must be an integer vector with exactly two non-negative values.

Dimnames: list of length two; each component containing NULL or a [character](#) vector length equal the corresponding Dim element.

Methods

There are (relatively simple) group methods (see, e.g., [Arith](#))

Arith signature(e1 = "dMatrix", e2 = "dMatrix"): ...

Arith signature(e1 = "dMatrix", e2 = "numeric"): ...

Arith signature(e1 = "numeric", e2 = "dMatrix"): ...

Math signature(x = "dMatrix"): ...

Math2 signature(x = "dMatrix", digits = "numeric"): this group contains [round\(\)](#) and [signif\(\)](#).

Compare signature(e1 = "numeric", e2 = "dMatrix"): ...

Compare signature(e1 = "dMatrix", e2 = "numeric"): ...

Compare signature(e1 = "dMatrix", e2 = "dMatrix"): ...

Summary signature(x = "dMatrix"): The "Summary" group contains the seven functions [max\(\)](#), [min\(\)](#), [range\(\)](#), [prod\(\)](#), [sum\(\)](#), [any\(\)](#), and [all\(\)](#).

The following methods are also defined for all double matrices:

expm signature(x = "dMatrix"): computes the "*Matrix Exponential*", see [expm](#).

The following methods are defined for all logical matrices:

which signature(x = "lsparseMatrix") and many other subclasses of "lMatrix": as the **base** function [which](#)(x, arr.ind) returns the indices of the **TRUE** entries in x; if `arr.ind` is true, as a 2-column matrix of row and column indices. Since **Matrix** version 1.2-9, if `useNames` is true, as by default, with [dimnames](#), the same as `base::which`.

See Also

The nonzero-pattern matrix class `nMatrix`, which can be used to store non-NA logical matrices even more compactly.

The numeric matrix classes `dgeMatrix`, `dgCMatrix`, and `Matrix`.

`drop0(x, tol=1e-10)` is sometimes preferable to (and more efficient than) `zapsmall(x, digits=10)`.

Examples

```
showClass("dMatrix")

set.seed(101)
round(Matrix(rnorm(28), 4,7), 2)
M <- Matrix(rlnorm(56, sd=10), 4,14)
(M. <- zapsmall(M))
table(as.logical(M. == 0))
```

dmperm

Dulmage-Mendelsohn Permutation / Decomposition

Description

For any $n \times m$ (typically) sparse matrix `x` compute the Dulmage-Mendelsohn row and columns permutations which at first splits the n rows and m columns into coarse partitions each; and then a finer one, reordering rows and columns such that the permuted matrix is “as upper triangular” as possible.

Usage

```
dmperm(x, nAns = 6L, seed = 0L)
```

Arguments

<code>x</code>	a typically sparse matrix; internally coerced to either “ <code>dgCMatrix</code> ” or “ <code>dtCMatrix</code> ”.
<code>nAns</code>	an integer specifying the <code>length</code> of the resulting <code>list</code> . Must be 2, 4, or 6.
<code>seed</code>	an integer code in -1,0,1; determining the (initial) permutation; by default, <code>seed = 0</code> , no (or the identity) permutation; <code>seed = -1</code> uses the “reverse” permutation <code>k:1</code> ; for <code>seed = 1</code> , it is a <i>random</i> permutation (using R’s RNG, <code>seed</code> , etc).

Details

See the book section by Tim Davis; page 122–127, in the References.

Value

a named `list` with (by default) 6 components,

<code>p</code>	integer vector with the permutation <code>p</code> , of length <code>nrow(x)</code> .
<code>q</code>	integer vector with the permutation <code>q</code> , of length <code>ncol(x)</code> .
<code>r</code>	integer vector of length <code>nb+1</code> , where block <code>k</code> is rows <code>r[k]</code> to <code>r[k+1]-1</code> in <code>A[p,q]</code> .
<code>s</code>	integer vector of length <code>nb+1</code> , where block <code>k</code> is cols <code>s[k]</code> to <code>s[k+1]-1</code> in <code>A[p,q]</code> .
<code>rr5</code>	integer vector of length 5, defining the coarse row decomposition.
<code>cc5</code>	integer vector of length 5, defining the coarse column decomposition.

Author(s)

Martin Maechler, with a lot of “encouragement” by Mauricio Vargas.

References

Section 7.4 *Dulmage-Mendelsohn decomposition*, pp. 122 ff of
Timothy A. Davis (2006) *Direct Methods for Sparse Linear Systems*, SIAM Series “Fundamentals of Algorithms”.

See Also

[Schur](#), the class of permutation matrices; “[pMatrix](#)”.

Examples

```
set.seed(17)
(S9 <- rsparsematrix(9, 9, nnz = 10, symmetric=TRUE)) # dsCMatrix
str( dm9 <- dmperm(S9) )
(S9p <- with(dm9, S9[p, q]))
## looks good, but *not* quite upper triangular; these, too:
str( dm9.0 <- dmperm(S9, seed=-1)) # non-random too.
str( dm9_1 <- dmperm(S9, seed= 1)) # a random one
## The last two permutations differ, but have the same effect!
(S9p0 <- with(dm9.0, S9[p, q])) # .. hmm ..
stopifnot(all.equal(S9p0, S9p))# same as as default, but different from the random one
```

```
set.seed(11)
(M <- triu(rsparsematrix(9,11, 1/4)))
dM <- dmperm(M); with(dM, M[p, q])
(Mp <- M[sample.int(nrow(M)), sample.int(ncol(M))])
dMp <- dmperm(Mp); with(dMp, Mp[p, q])
```

```
set.seed(7)
(n7 <- rsparsematrix(5, 12, nnz = 10, rand.x = NULL))
str( dm.7 <- dmperm(n7) )
stopifnot(exprs = {
  lengths(dm.7[1:2]) == dim(n7)
```



```

    identical(dm.7,      dmperm(as(n7, "dMatrix")))
    identical(dm.7[1:4], dmperm(n7, nAns=4))
    identical(dm.7[1:2], dmperm(n7, nAns=2))
  })

```

dpoMatrix-class	<i>Positive Semi-definite Dense (Packed Non-packed) Numeric Matrices</i>
-----------------	--

Description

- The "dpoMatrix" class is the class of positive-semidefinite symmetric matrices in nonpacked storage.
- The "dppMatrix" class is the same except in packed storage. Only the upper triangle or the lower triangle is required to be available.
- The "corMatrix" and "copMatrix" classes represent correlation matrices. They extend "dpoMatrix" and "dppMatrix", respectively, with an additional slot `sd` allowing restoration of the original covariance matrix.

Objects from the Class

Objects can be created by calls of the form `new("dpoMatrix", ...)` or from `crossprod` applied to an "dgeMatrix" object.

Slots

- uplo:** Object of class "character". Must be either "U", for upper triangular, and "L", for lower triangular.
- x:** Object of class "numeric". The numeric values that constitute the matrix, stored in column-major order.
- Dim:** Object of class "integer". The dimensions of the matrix which must be a two-element vector of non-negative integers.
- Dimnames:** inherited from class "Matrix"
- factors:** Object of class "list". A named list of factorizations that have been computed for the matrix.
- sd:** (for "corMatrix" and "copMatrix") a **numeric** vector of length `n` containing the (original) $\sqrt{\text{var}(\cdot)}$ entries which allow reconstruction of a covariance matrix from the correlation matrix.

Extends

- Class "dsyMatrix", directly.
- Classes "dgeMatrix", "symmetricMatrix", and many more by class "dsyMatrix".

Methods

- chol** signature($x = \text{"dpoMatrix"}$): Returns (and stores) the Cholesky decomposition of x , see [chol](#).
- determinant** signature($x = \text{"dpoMatrix"}$): Returns the [determinant](#) of x , via `chol(x)`, see above.
- rcond** signature($x = \text{"dpoMatrix"}$, $\text{norm} = \text{"character"}$): Returns (and stores) the reciprocal of the condition number of x . The norm can be "0" for the one-norm (the default) or "I" for the infinity-norm. For symmetric matrices the result does not depend on the norm.
- solve** signature($a = \text{"dpoMatrix"}$, $b = \text{"..."}$), and
- solve** signature($a = \text{"dppMatrix"}$, $b = \text{"..."}$) work via the Cholesky composition, see also the Matrix [solve-methods](#).
- Arith** signature($e1 = \text{"dpoMatrix"}$, $e2 = \text{"numeric"}$) (and quite a few other signatures): The result of ("elementwise" defined) arithmetic operations is typically *not* positive-definite anymore. The only exceptions, currently, are multiplications, divisions or additions with *positive* `length(.) == 1` numbers (or [logicals](#)).

Note

Currently the validity methods for these classes such as `getValidity(getClass("dpoMatrix"))` for efficiency reasons only check the diagonal entries of the matrix – they may not be negative. This is only necessary but not sufficient for a symmetric matrix to be positive semi-definite.

A more reliable (but often more expensive) check for positive semi-definiteness would look at the signs of `diag(BunchKaufman(.))` (with some tolerance for very small negative values), and for (strict) positive definiteness at something like `!inherits(tryCatch(chol(.), error=identity), "error")`. Indeed, when *coercing* to these classes, a version of [Cholesky\(\)](#) or `chol()` is typically used, e.g., see `selectMethod("coerce", c(from="dsyMatrix", to="dpoMatrix"))`.

See Also

Classes [dsyMatrix](#) and [dgeMatrix](#); further, [Matrix](#), [rcond](#), [chol](#), [solve](#), [crossprod](#).

Examples

```
h6 <- Hilbert(6)
rcond(h6)
str(h6)
h6 * 27720 # is ``integer``
solve(h6)
str(hp6 <- pack(h6))

### Note that as(*, "corMatrix") *scales* the matrix
(ch6 <- as(h6, "corMatrix"))
stopifnot(all.equal(as(h6 * 27720, "dsyMatrix"), round(27720 * h6),
                    tolerance = 1e-14),
          all.equal(ch6@sd^(-2), 2*(1:6)-1,
                    tolerance = 1e-12))
chch <- Cholesky(ch6, perm = FALSE)
stopifnot(identical(chch, ch6@factors$Cholesky),
          all(abs(crossprod(as(chch, "dtrMatrix")) - ch6) < 1e-10))
```

`drop0`*Drop Non-Structural Zeros from a Sparse Matrix*

Description

Deletes “non-structural” zeros (i.e., zeros stored explicitly, in memory) from a sparse matrix and returns the result.

Usage

```
drop0(x, tol = 0, is.Csparse = NA, give.Csparse = TRUE)
```

Arguments

<code>x</code>	a Matrix , typically inheriting from virtual class sparseMatrix . denseMatrix and traditional vectors and matrices are coerced to CsparseMatrix , with zeros dropped automatically, hence users passing such <code>x</code> should consider <code>as(x, "CsparseMatrix")</code> instead, notably in the <code>tol = 0</code> case.
<code>tol</code>	a non-negative number. If <code>x</code> is numeric, then entries less than or equal to <code>tol</code> in absolute value are deleted.
<code>is.Csparse</code>	a logical used only if <code>give.Csparse</code> is <code>TRUE</code> , indicating if <code>x</code> already inherits from virtual class CsparseMatrix , in which case coercion is not attempted, permitting some (typically small) speed-up.
<code>give.Csparse</code>	a logical indicating if the result must inherit from virtual class CsparseMatrix . If <code>FALSE</code> and <code>x</code> inherits from RsparseMatrix , TsparseMatrix , or indMatrix , then the result preserves the class of <code>x</code> . The default value is <code>TRUE</code> only for backwards compatibility.

Value

A [sparseMatrix](#), the result of deleting non-structural zeros from `x`, possibly after coercion.

Note

`drop0` is sometimes called in conjunction with [zapsmall](#), e.g., when dealing with sparse matrix products; see the example.

See Also

Function [sparseMatrix](#), for constructing objects inheriting from virtual class [sparseMatrix](#); [nnzero](#).

Examples

```
(m <- sparseMatrix(i = 1:8, j = 2:9, x = c(0:2, 3:-1),
                  dims = c(10L, 20L)))
drop0(m)

## A larger example:
t5 <- new("dtCMatrix", Dim = c(5L, 5L), uplo = "L",
         x = c(10, 1, 3, 10, 1, 10, 1, 10, 10),
         i = c(0L,2L,4L, 1L, 3L,2L,4L, 3L, 4L),
         p = c(0L, 3L, 5L, 7:9))
TT <- kronecker(t5, kronecker(kronecker(t5, t5), t5))
IT <- solve(TT)
I. <- TT %*% IT ; nnzero(I.) # 697 ( == 625 + 72 )
I.0 <- drop0(zapsmall(I.))
## which actually can be more efficiently achieved by
I.. <- drop0(I., tol = 1e-15)
stopifnot(all(I.0 == Diagonal(625)), nnzero(I..) == 625)
```

dsCMatrix-class

*Numeric Symmetric Sparse (column compressed) Matrices***Description**

The dsCMatrix class is a class of symmetric, sparse numeric matrices in the compressed, column-oriented format. In this implementation the non-zero elements in the columns are sorted into increasing row order.

The dsTMatrix class is the class of symmetric, sparse numeric matrices in triplet format.

Objects from the Class

Objects can be created by calls of the form `new("dsCMatrix", ...)` or `new("dsTMatrix", ...)`, or automatically via e.g., `as(*, "symmetricMatrix")`, or (for dsCMatrix) also from `Matrix(.)`.

Creation "from scratch" most efficiently happens via `sparseMatrix(*, symmetric=TRUE)`.

Slots

- uplo:** A character object indicating if the upper triangle ("U") or the lower triangle ("L") is stored.
- i:** Object of class "integer" of length nnZ (*half* number of non-zero elements). These are the row numbers for each non-zero element in the lower triangle of the matrix.
- p:** (only in class "dsCMatrix":) an [integer](#) vector for providing pointers, one for each column, see the detailed description in [CsparseMatrix](#).
- j:** (only in class "dsTMatrix":) Object of class "integer" of length nnZ (as i). These are the column numbers for each non-zero element in the lower triangle of the matrix.
- x:** Object of class "numeric" of length nnZ – the non-zero elements of the matrix (to be duplicated for full matrix).
- factors:** Object of class "list" - a list of factorizations of the matrix.
- Dim:** Object of class "integer" - the dimensions of the matrix - must be an integer vector with exactly two non-negative values.

Extends

Both classes extend classes and [symmetricMatrix](#) [dsparseMatrix](#) directly; dsCMatrix further directly extends [CsparseMatrix](#), where dsTMatrix does [TsparseMatrix](#).

Methods

solve signature(`a = "dsCMatrix"`, `b = "..."`): `x <- solve(a,b)` solves $Ax = b$ for x ; see [solve-methods](#).

chol signature(`x = "dsCMatrix"`, `pivot = "logical"`): Returns (and stores) the Cholesky decomposition of x , see [chol](#).

Cholesky signature(`A = "dsCMatrix"`, ...): Computes more flexibly Cholesky decompositions, see [Cholesky](#).

determinant signature(`x = "dsCMatrix"`, `logarithm = "missing"`): Evaluate the determinant of x on the logarithm scale. This creates and stores the Cholesky factorization.

determinant signature(`x = "dsCMatrix"`, `logarithm = "logical"`): Evaluate the determinant of x on the logarithm scale or not, according to the `logarithm` argument. This creates and stores the Cholesky factorization.

t signature(`x = "dsCMatrix"`): Transpose. As for all symmetric matrices, a matrix for which the upper triangle is stored produces a matrix for which the lower triangle is stored and vice versa, i.e., the `uplo` slot is swapped, and the row and column indices are interchanged.

t signature(`x = "dsTMatrix"`): Transpose. The `uplo` slot is swapped from "U" to "L" or vice versa, as for a "dsCMatrix", see above.

See Also

Classes [dgCMatrix](#), [dgTMatrix](#), [dgeMatrix](#) and those mentioned above.

Examples

```
mm <- Matrix(toeplitz(c(10, 0, 1, 0, 3)), sparse = TRUE)
mm # automatically dsCMatrix
str(mm)
mT <- as(as(mm, "generalMatrix"), "TsparseMatrix")

## Either
(symM <- as(mT, "symmetricMatrix")) # dsT
(symC <- as(symM, "CsparseMatrix")) # dsC
## or
sT <- Matrix(mT, sparse=TRUE, forceCheck=TRUE) # dsT

sym2 <- as(symC, "TsparseMatrix")
## --> the same as 'symM', a "dsTMatrix"
```

dsparseMatrix-class *Virtual Class "dsparseMatrix" of Numeric Sparse Matrices*

Description

The Class "dsparseMatrix" is the virtual (super) class of all numeric sparse matrices.

Slots

Dim: the matrix dimension, see class "[Matrix](#)".

Dimnames: see the "[Matrix](#)" class.

x: a [numeric](#) vector containing the (non-zero) matrix entries.

Extends

Class "dMatrix" and "sparseMatrix", directly.

Class "Matrix", by the above classes.

See Also

the documentation of the (non virtual) sub classes, see `showClass("dsparseMatrix")`; in particular, [dgTMatrix](#), [dgCMatrix](#), and [dgRMatrix](#).

Examples

```
showClass("dsparseMatrix")
```

dsRMatrix-class *Symmetric Sparse Compressed Row Matrices*

Description

The dsRMatrix class is a class of symmetric, sparse matrices in the compressed, row-oriented format. In this implementation the non-zero elements in the rows are sorted into increasing column order.

Objects from the Class

These ".RMatrix" classes are currently still mostly unimplemented!

Objects can be created by calls of the form `new("dsRMatrix", ...)`.

Slots

- uplo:** A character object indicating if the upper triangle ("U") or the lower triangle ("L") is stored. At present only the lower triangle form is allowed.
- j:** Object of class "integer" of length nnzero (number of non-zero elements). These are the row numbers for each non-zero element in the matrix.
- p:** Object of class "integer" of pointers, one for each row, to the initial (zero-based) index of elements in the row.
- factors:** Object of class "list" - a list of factorizations of the matrix.
- x:** Object of class "numeric" - the non-zero elements of the matrix.
- Dim:** Object of class "integer" - the dimensions of the matrix - must be an integer vector with exactly two non-negative values.
- Dimnames:** List of length two, see [Matrix](#).

Extends

Classes [dsparseMatrix](#), [symmetricMatrix](#), and [RsparseMatrix](#), directly.

Class "dMatrix", by class "dsparseMatrix"; class "sparseMatrix", by classes "dsparseMatrix" and "RsparseMatrix".

Methods

forceSymmetric signature(x = "dsRMatrix", uplo = "missing"): a trivial method just returning x

forceSymmetric signature(x = "dsRMatrix", uplo = "character"): if uplo == x@uplo, this trivially returns x; otherwise t(x).

See Also

the classes [dgCMatrix](#), [dgTMatrix](#), and [dgeMatrix](#).

Examples

```
(m0 <- new("dsRMatrix"))
m2 <- new("dsRMatrix", Dim = c(2L,2L),
         x = c(3,1), j = c(1L,1L), p = 0:2)
m2
stopifnot(colSums(as(m2, "TsparseMatrix")) == 3:4)
str(m2)
(ds2 <- forceSymmetric(diag(2))) # dsy*
dR <- as(ds2, "RsparseMatrix")
dR # dsRMatrix
```

dsyMatrix-class

*Symmetric Dense (Packed or Unpacked) Numeric Matrices***Description**

- The "dsyMatrix" class is the class of symmetric, dense matrices in *non-packed* storage and
- "dspMatrix" is the class of symmetric dense matrices in *packed* storage, see [pack\(\)](#). Only the upper triangle or the lower triangle is stored.

Objects from the Class

Objects can be created by calls of the form `new("dsyMatrix", ...)` or `new("dspMatrix", ...)`, respectively.

Slots

uplo: Object of class "character". Must be either "U", for upper triangular, and "L", for lower triangular.

x: Object of class "numeric". The numeric values that constitute the matrix, stored in column-major order.

Dim,Dimnames: The dimension (a length-2 "integer") and corresponding names (or NULL), see the [Matrix](#).

factors: Object of class "list". A named list of factorizations that have been computed for the matrix.

Extends

"dsyMatrix" extends class "dgeMatrix", directly, whereas

"dspMatrix" extends class "ddenseMatrix", directly.

Both extend class "symmetricMatrix", directly, and class "Matrix" and others, *indirectly*, use [showClass\("dsyMatrix"\)](#), e.g., for details.

Methods

norm signature(`x = "dspMatrix"`, `type = "character"`), or `x = "dsyMatrix"` or `type = "missing"`: Computes the matrix norm of the desired type, see, [norm](#).

rcond signature(`x = "dspMatrix"`, `type = "character"`), or `x = "dsyMatrix"` or `type = "missing"`: Computes the reciprocal condition number, [rcond\(\)](#).

solve signature(`a = "dspMatrix"`, `b = "..."`), and

solve signature(`a = "dsyMatrix"`, `b = "..."`): `x <- solve(a,b)` solves $Ax = b$ for x ; see [solve-methods](#).

t signature(`x = "dsyMatrix"`): Transpose; swaps from upper triangular to lower triangular storage, i.e., the uplo slot from "U" to "L" or vice versa, the same as for all symmetric matrices.

See Also

The *positive (Semi-)definite* dense (packed or non-packed numeric matrix classes [dpoMatrix](#), [dppMatrix](#) and [corMatrix](#),

Classes [dgeMatrix](#) and [Matrix](#); [solve](#), [norm](#), [rcond](#), [t](#)

Examples

```
## Only upper triangular part matters (when uplo == "U" as per default)
(sy2 <- new("dsyMatrix", Dim = as.integer(c(2,2)), x = c(14, NA, 32, 77)))
str(t(sy2)) # uplo = "L", and the lower tri. (i.e. NA is replaced).
```

```
chol(sy2) #-> "Cholesky" matrix
(sp2 <- pack(sy2)) # a "dspMatrix"
```

```
## Coercing to dpoMatrix gives invalid object:
sy3 <- new("dsyMatrix", Dim = as.integer(c(2,2)), x = c(14, -1, 2, -7))
try(as(sy3, "dpoMatrix")) # -> error: not positive definite
```

```
## 4x4 example
m <- matrix(0,4,4); m[upper.tri(m)] <- 1:6
(sym <- m+t(m)+diag(11:14, 4))
(S1 <- pack(sym))
(S2 <- t(S1))
stopifnot(all(S1 == S2)) # equal "seen as matrix", but differ internally :
str(S1)
S2@x
```

dtMatrix-class

Triangular, (compressed) sparse column matrices

Description

The "dtMatrix" class is a class of triangular, sparse matrices in the compressed, column-oriented format. In this implementation the non-zero elements in the columns are sorted into increasing row order.

The "dtTMatrix" class is a class of triangular, sparse matrices in triplet format.

Objects from the Class

Objects can be created by calls of the form `new("dtMatrix", ...)` or calls of the form `new("dtTMatrix", ...)`, but more typically automatically via `Matrix()` or coercions such as `as(x, "triangularMatrix")`.

Slots

`uplo`: Object of class "character". Must be either "U", for upper triangular, and "L", for lower triangular.

- diag:** Object of class "character". Must be either "U", for unit triangular (diagonal is all ones), or "N"; see [triangularMatrix](#).
- p:** (only present in "dtCMatrix":) an [integer](#) vector for providing pointers, one for each column, see the detailed description in [CsparseMatrix](#).
- i:** Object of class "integer" of length nnzero (number of non-zero elements). These are the row numbers for each non-zero element in the matrix.
- j:** Object of class "integer" of length nnzero (number of non-zero elements). These are the column numbers for each non-zero element in the matrix. (Only present in the dtTMatrix class.)
- x:** Object of class "numeric" - the non-zero elements of the matrix.
- Dim,Dimnames:** The dimension (a length-2 "integer") and corresponding names (or NULL), inherited from the [Matrix](#), see there.

Extends

Class "dgCMatrix", directly. Class "triangularMatrix", directly. Class "dMatrix", "sparseMatrix", and more by class "dgCMatrix" etc, see the examples.

Methods

- solve** signature(a = "dtCMatrix", b = "..."): sparse triangular solve (aka "backsolve" or "forwardsolve"), see [solve-methods](#).
- t** signature(x = "dtCMatrix"): returns the transpose of x
- t** signature(x = "dtTMatrix"): returns the transpose of x

See Also

Classes [dgCMatrix](#), [dgTMatrix](#), [dgeMatrix](#), and [dtrMatrix](#).

Examples

```
showClass("dtCMatrix")
showClass("dtTMatrix")
t1 <- new("dtTMatrix", x= c(3,7), i= 0:1, j=3:2, Dim= as.integer(c(4,4)))
t1
## from 0-diagonal to unit-diagonal {low-level step}:
tu <- t1 ; tu@diag <- "U"
tu
(cu <- as(tu, "CsparseMatrix"))
str(cu)# only two entries in @i and @x
stopifnot(cu@i == 1:0,
           all(2 * symmpart(cu) == Diagonal(4) + forceSymmetric(cu)))

t1[1,2:3] <- -1:-2
diag(t1) <- 10*c(1:2,3:2)
t1 # still triangular
(it1 <- solve(t1))
t1. <- solve(it1)
all(abs(t1 - t1.) < 10 * .Machine$double.eps)
```

```
## 2nd example
U5 <- new("dtCMatrix", i= c(1L, 0:3), p=c(0L,0L,0:2, 5L), Dim = c(5L, 5L),
         x = rep(1, 5), diag = "U")
U5
(iu <- solve(U5)) # contains one '0'
validObject(iu2 <- solve(U5, Diagonal(5)))# failed in earlier versions

I5 <- iu **% U5 # should equal the identity matrix
i5 <- iu2 **% U5
m53 <- matrix(1:15, 5,3, dimnames=list(NULL,letters[1:3]))
asDiag <- function(M) as(drop0(M), "diagonalMatrix")
stopifnot(
  all.equal(Diagonal(5), asDiag(I5), tolerance=1e-14) ,
  all.equal(Diagonal(5), asDiag(i5), tolerance=1e-14) ,
  identical(list(NULL, dimnames(m53)[[2]]), dimnames(solve(U5, m53)))
)
```

dtpMatrix-class

Packed Triangular Dense Matrices - "dtpMatrix"

Description

The "dtpMatrix" class is the class of triangular, dense, numeric matrices in packed storage. The "dtrMatrix" class is the same except in nonpacked storage.

Objects from the Class

Objects can be created by calls of the form `new("dtpMatrix", ...)` or by coercion from other classes of matrices.

Slots

uplo: Object of class "character". Must be either "U", for upper triangular, and "L", for lower triangular.

diag: Object of class "character". Must be either "U", for unit triangular (diagonal is all ones), or "N"; see [triangularMatrix](#).

x: Object of class "numeric". The numeric values that constitute the matrix, stored in column-major order. For a packed square matrix of dimension $d \times d$, `length(x)` is of length $d(d+1)/2$ (also when `diag == "U"`!).

Dim,Dimnames: The dimension (a length-2 "integer") and corresponding names (or NULL), inherited from the [Matrix](#), see there.

Extends

Class "ddenseMatrix", directly. Class "triangularMatrix", directly. Class "dMatrix" and more by class "ddenseMatrix" etc, see the examples.

Methods

- %*%** signature(x = "dtpMatrix", y = "dgeMatrix"): Matrix multiplication; ditto for several other signature combinations, see `showMethods("%*%", class = "dtpMatrix")`.
- determinant** signature(x = "dtpMatrix", logarithm = "logical"): the `determinant(x)` trivially is `prod(diag(x))`, but computed on log scale to prevent over- and underflow.
- diag** signature(x = "dtpMatrix"): ...
- norm** signature(x = "dtpMatrix", type = "character"): ...
- rcond** signature(x = "dtpMatrix", norm = "character"): ...
- solve** signature(a = "dtpMatrix", b = "..."): efficiently using internal backsolve or forward-solve, see [solve-methods](#).
- t** signature(x = "dtpMatrix"): `t(x)` remains a "dtpMatrix", lower triangular if x is upper triangular, and vice versa.

See Also

Class [dtrMatrix](#)

Examples

```
showClass("dtrMatrix")

example("dtrMatrix-class", echo=FALSE)
(p1 <- pack(T2))
str(p1)
(pp <- pack(T))
(ip1 <- solve(p1))
stopifnot(length(p1@x) == 3, length(pp@x) == 3,
           p1 @ uplo == T2 @ uplo, pp @ uplo == T @ uplo,
           identical(t(pp), p1), identical(t(p1), pp),
           all((l.d <- p1 - T2) == 0), is(l.d, "dtpMatrix"),
           all((u.d <- pp - T) == 0), is(u.d, "dtpMatrix"),
           l.d@uplo == T2@uplo, u.d@uplo == T@uplo,
           identical(t(ip1), solve(pp)), is(ip1, "dtpMatrix"),
           all.equal(as(solve(p1,p1), "diagonalMatrix"), Diagonal(2)))
```

dtRMatrix-class

Triangular Sparse Compressed Row Matrices

Description

The `dtRMatrix` class is a class of triangular, sparse matrices in the compressed, row-oriented format. In this implementation the non-zero elements in the rows are sorted into increasing column order.

Objects from the Class

This class is currently still mostly unimplemented!

Objects can be created by calls of the form `new("dtRMatrix", ...)`.

Slots

uplo: Object of class "character". Must be either "U", for upper triangular, and "L", for lower triangular. At present only the lower triangle form is allowed.

diag: Object of class "character". Must be either "U", for unit triangular (diagonal is all ones), or "N"; see [triangularMatrix](#).

j: Object of class "integer" of length `nzero(.)` (number of non-zero elements). These are the row numbers for each non-zero element in the matrix.

p: Object of class "integer" of pointers, one for each row, to the initial (zero-based) index of elements in the row. (Only present in the `dsRMatrix` class.)

x: Object of class "numeric" - the non-zero elements of the matrix.

Dim: The dimension (a length-2 "integer")

Dimnames: corresponding names (or NULL), inherited from the [Matrix](#), see there.

Extends

Class "dgRMatrix", directly. Class "dsparseMatrix", by class "dgRMatrix". Class "dMatrix", by class "dgRMatrix". Class "sparseMatrix", by class "dgRMatrix". Class "Matrix", by class "dgRMatrix".

Methods

No methods currently with class "dsRMatrix" in the signature.

See Also

Classes [dgCMatrix](#), [dgTMatrix](#), [dgeMatrix](#)

Examples

```
(m0 <- new("dtRMatrix"))
(m2 <- new("dtRMatrix", Dim = c(2L,2L),
          x = c(5, 1:2), p = c(0L,2:3), j= c(0:1,1L)))
str(m2)
(m3 <- as(Diagonal(2), "RsparseMatrix"))# --> dtRMatrix
```

dtrMatrix-class *Triangular, dense, numeric matrices*

Description

The "dtrMatrix" class is the class of triangular, dense, numeric matrices in nonpacked storage. The "dtpMatrix" class is the same except in packed storage, see [pack\(\)](#).

Objects from the Class

Objects can be created by calls of the form `new("dtrMatrix", ...)`.

Slots

- uplo:** Object of class "character". Must be either "U", for upper triangular, and "L", for lower triangular.
- diag:** Object of class "character". Must be either "U", for unit triangular (diagonal is all ones), or "N"; see [triangularMatrix](#).
- x:** Object of class "numeric". The numeric values that constitute the matrix, stored in column-major order.
- Dim:** Object of class "integer". The dimensions of the matrix which must be a two-element vector of non-negative integers.

Extends

Class "ddenseMatrix", directly. Class "triangularMatrix", directly. Class "Matrix" and others, by class "ddenseMatrix".

Methods

Among others (such as matrix products, e.g. [?crossprod-methods](#)),

norm signature(x = "dtrMatrix", type = "character"): ..

rcond signature(x = "dtrMatrix", norm = "character"): ..

solve signature(a = "dtrMatrix", b = "..."): efficiently use a "forwardsolve" or backsolve for a lower or upper triangular matrix, respectively, see also [solve-methods](#).

+, -, *, ..., ==, >=, ... all the [Ops](#) group methods are available. When applied to two triangular matrices, these return a triangular matrix when easily possible.

See Also

Classes [ddenseMatrix](#), [dtpMatrix](#), [triangularMatrix](#)

Examples

```

(m <- rbind(2:3, 0:-1))
(M <- as(m, "generalMatrix"))

(T <- as(M, "triangularMatrix")) # formally upper triangular
(T2 <- as(t(M), "triangularMatrix"))
stopifnot(T@uplo == "U", T2@uplo == "L", identical(T2, t(T)))

m <- matrix(0,4,4); m[upper.tri(m)] <- 1:6
(t1 <- Matrix(m+diag(,4)))
str(t1p <- pack(t1))
(t1pu <- diagN2U(t1p))
stopifnot(exprs = {
  inherits(t1, "dtrMatrix"); validObject(t1)
  inherits(t1p, "dtpMatrix"); validObject(t1p)
  inherits(t1pu, "dtCMatrix"); validObject(t1pu)
  t1pu@x == 1:6
  all(t1pu == t1p)
  identical((t1pu - t1)@x, numeric())# sparse all-0
})

```

 expand-methods

Expand Matrix Factorizations

Description

expand1 and expand2 construct matrix factors from objects specifying matrix factorizations. Such objects typically do not store the factors explicitly, employing instead a compact representation to save memory.

Usage

```

expand1(x, which, ...)
expand2(x, ...)

expand(x, ...)

```

Arguments

x	a matrix factorization, typically inheriting from virtual class MatrixFactorization .
which	a character string indicating a matrix factor.
...	further arguments passed to or from methods.

Details

Methods for `expand` are retained only for backwards compatibility with **Matrix** < 1.6-0. New code should use `expand1` and `expand2`, whose methods provide more control and behave more consistently. Notably, `expand2` obeys the rule that the product of the matrix factors in the returned list should reproduce (within some tolerance) the factorized matrix, *including* its dimnames.

Hence if `x` is a matrix and `y` is its factorization, then

```
all.equal(as(x, "matrix"), as(Reduce(`%*%`, expand2(y)), "matrix"))
```

should in most cases return TRUE.

Value

`expand1` returns an object inheriting from virtual class **Matrix**, representing the factor indicated by which, always without row and column names.

`expand2` returns a list of factors, typically with names using conventional notation, as in `list(L=, U=)`. The first and last factors get the row and column names of the factorized matrix, which are preserved in the `Dimnames` slot of `x`.

Methods

The following table lists methods for `expand1` together with allowed values of argument `which`.

class(x)	which
Schur	c("Q", "T", "Q.")
denseLU	c("P1", "P1.", "L", "U")
sparseLU	c("P1", "P1.", "P2", "P2.", "L", "U")
sparseQR	c("P1", "P1.", "P2", "P2.", "Q", "Q1", "R", "R1")
BunchKaufman, pBunchKaufman	c("U", "DU", "U.", "L", "DL", "L.")
Cholesky, pCholesky	c("P1", "P1.", "L1", "D", "L1.", "L", "L.")
CHMsimpl, CHMsimpl	c("P1", "P1.", "L1", "D", "L1.", "L", "L.")

Methods for `expand2` and `expand` are described below. Factor names and classes apply also to `expand1`.

`expand2` signature(`x = "CHMsimpl"`): expands the factorization $A = P_1' L_1 D L_1' P_1 = P_1' L L' P_1$ as `list(P1., L1, D, L1., P1)` (the default) or as `list(P1., L, L., P1)`, depending on optional logical argument `LDL`. `P1` and `P1.` are **pMatrix**, `L1`, `L1.`, `L`, and `L.` are **dtMatrix**, and `D` is a **ddiMatrix**.

`expand2` signature(`x = "CHMsuper"`): as `CHMsimpl`, but the triangular factors are stored as **dgMatrix**.

`expand2` signature(`x = "p?Cholesky"`): expands the factorization $A = L_1 D L_1' = L L'$ as `list(L1, D, L1.)` (the default) or as `list(L, L.)`, depending on optional logical argument `LDL`. `L1`, `L1.`, `L`, and `L.` are **dtrMatrix** or **dtpMatrix**, and `D` is a **ddiMatrix**.

`expand2` signature(`x = "p?BunchKaufman"`): expands the factorization $A = U D_U U' = L D_L L'$ where $U = \prod_{k=1}^{b_U} P_k U_k$ and $L = \prod_{k=1}^{b_L} P_k L_k$ as `list(U, DU, U.)` or `list(L, DL, L.)`, depending on `x@uplo`. If optional argument `complete` is TRUE, then an unnamed list giving the full expansion with $2b_U + 1$ or $2b_L + 1$ matrix factors is returned instead. P_k are represented

as `pMatrix`, U_k and L_k are represented as `dtMatrix`, and D_U and D_L are represented as `dsMatrix`.

`expand2 signature(x = "Schur")`: expands the factorization $A = QTQ'$ as `list(Q, T, Q.)`. Q and $Q.$ are `x@Q` and `t(x@Q)` modulo `Dimnames`, and T is `x@T`.

`expand2 signature(x = "sparseLU")`: expands the factorization $A = P'_1 L U P'_2$ as `list(P1., L, U, P2.)`. $P1.$ and $P2.$ are `pMatrix`, and L and U are `dtMatrix`.

`expand2 signature(x = "denseLU")`: expands the factorization $A = P'_1 L U$ as `list(P1., L, U)`. $P1.$ is a `pMatrix`, and L and U are `dtrMatrix` if square and `dgeMatrix` otherwise.

`expand2 signature(x = "sparseQR")`: expands the factorization $A = P'_1 Q R P'_2 = P'_1 Q_1 R_1 P'_2$ as `list(P1., Q, R, P2.)` or `list(P1., Q1, R1, P2.)`, depending on optional logical argument `complete`. $P1.$ and $P2.$ are `pMatrix`, Q and $Q1$ are `dgeMatrix`, R is a `dgMatrix`, and $R1$ is a `dtMatrix`.

`expand signature(x = "CHMfactor")`: as `expand2`, but returning `list(P, L)`. `expand(x)[["P"]]` and `expand2(x)[["P1"]]` represent the same permutation matrix P_1 but have opposite margin slots and inverted perm slots. The components of `expand(x)` do not preserve `x@Dimnames`.

`expand signature(x = "sparseLU")`: as `expand2`, but returning `list(P, L, U, Q)`. `expand(x)[["Q"]]` and `expand2(x)[["P2. "]]` represent the same permutation matrix P'_2 but have opposite margin slots and inverted perm slots. `expand(x)[["P"]]` represents the permutation matrix P_1 rather than its transpose P'_1 ; it is `expand2(x)[["P1. "]]` with an inverted perm slot. `expand(x)[["L"]]` and `expand2(x)[["L "]]` represent the same unit lower triangular matrix L , but with diag slot equal to "N" and "U", respectively. `expand(x)[["L "]]` and `expand(x)[["U "]]` store the *permuted* first and second components of `x@Dimnames` in their `Dimnames` slots.

`expand signature(x = "denseLU")`: as `expand2`, but returning `list(L, U, P)`. `expand(x)[["P"]]` and `expand2(x)[["P1. "]]` are identical modulo `Dimnames`. The components of `expand(x)` do not preserve `x@Dimnames`.

See Also

The virtual class `MatrixFactorization` of matrix factorizations.

Generic functions `Cholesky`, `BunchKaufman`, `Schur`, `lu`, and `qr` for *computing* factorizations.

Examples

```
showMethods("expand1", inherited = FALSE)
showMethods("expand2", inherited = FALSE)
set.seed(0)

(A <- Matrix(rnorm(9L, 0, 10), 3L, 3L))
(lu.A <- lu(A))
(e.lu.A <- expand2(lu.A))
stopifnot(exprs = {
  is.list(e.lu.A)
  identical(names(e.lu.A), c("P1.", "L", "U"))
  all(sapply(e.lu.A, is, "Matrix"))
  all.equal(as(A, "matrix"), as(Reduce("%*%", e.lu.A), "matrix"))
})

## 'expand1' and 'expand2' give equivalent results modulo
```

```
## dimnames and representation of permutation matrices;
## see also function 'alt' in example("Cholesky-methods")
(a1 <- sapply(names(e.lu.A), expand1, x = lu.A, simplify = FALSE))
all.equal(a1, e.lu.A)

## see help("denseLU-class") and others for more examples
```

expm-methods

*Matrix Exponential***Description**

Compute the exponential of a matrix.

Usage

```
expm(x)
```

Arguments

`x` a matrix, typically inheriting from the `dMatrix` class.

Details

The exponential of a matrix is defined as the infinite Taylor series $\text{expm}(A) = I + A + A^2/2! + A^3/3! + \dots$ (although this is definitely not the way to compute it). The method for the `dgeMatrix` class uses Ward's diagonal Pade' approximation with three step preconditioning, a recommendation from Moler & Van Loan (1978) "Nineteen dubious ways...".

Value

The matrix exponential of `x`.

Author(s)

This is a translation of the implementation of the corresponding Octave function contributed to the Octave project by A. Scottedward Hodel <A.S.Hodel@Eng.Auburn.EDU>. A bug in there has been fixed by Martin Maechler.

References

https://en.wikipedia.org/wiki/Matrix_exponential

Cleve Moler and Charles Van Loan (2003) Nineteen dubious ways to compute the exponential of a matrix, twenty-five years later. *SIAM Review* **45**, 1, 3–49. doi:10.1137/S00361445024180

for historical reference mostly:

Moler, C. and Van Loan, C. (1978) Nineteen dubious ways to compute the exponential of a matrix. *SIAM Review* **20**, 4, 801–836. doi:10.1137/1020098

Eric W. Weisstein et al. (1999) *Matrix Exponential*. From MathWorld, <https://mathworld.wolfram.com/MatrixExponential.html>

See Also

Package **expm**, which provides newer (in some cases faster, more accurate) algorithms for computing the matrix exponential via its own (non-generic) function `expm()`. **expm** also implements `logm()`, `sqrtm()`, etc.

Generic function [Schur](#).

Examples

```
(m1 <- Matrix(c(1,0,1,1), ncol = 2))
(e1 <- expm(m1)) ; e <- exp(1)
stopifnot(all.equal(e1@x, c(e,0,e,e), tolerance = 1e-15))
(m2 <- Matrix(c(-49, -64, 24, 31), ncol = 2))
(e2 <- expm(m2))
(m3 <- Matrix(cbind(0, rbind(6*diag(3), 0)))) # sparse!
(e3 <- expm(m3)) # upper triangular
```

externalFormats

Read and write external matrix formats

Description

Read matrices stored in the Harwell-Boeing or MatrixMarket formats or write `sparseMatrix` objects to one of these formats.

Usage

```
readHB(file)
readMM(file)
writeMM(obj, file, ...)
```

Arguments

<code>obj</code>	a real sparse matrix
<code>file</code>	for <code>writeMM</code> - the name of the file to be written. For <code>readHB</code> and <code>readMM</code> the name of the file to read, as a character scalar. The names of files storing matrices in the Harwell-Boeing format usually end in <code>".rua"</code> or <code>".rsa"</code> . Those storing matrices in the MatrixMarket format usually end in <code>".mtx"</code> . Alternatively, <code>readHB</code> and <code>readMM</code> accept connection objects.
<code>...</code>	optional additional arguments. Currently none are used in any methods.

Value

The `readHB` and `readMM` functions return an object that inherits from the `"Matrix"` class. Methods for the `writeMM` generic functions usually return `NULL` and, as a side effect, the matrix `obj` is written to file in the MatrixMarket format (`writeMM`).

Note

The Harwell-Boeing format is older and less flexible than the MatrixMarket format. The function `writeHB` was deprecated and has now been removed. Please use `writeMM` instead.

Note that these formats do *not* know anything about `dimnames`, hence these are dropped by `writeMM()`.

A very simple way to export small sparse matrices `S`, is to use `summary(S)` which returns a `data.frame` with columns `i`, `j`, and possibly `x`, see `summary` in `sparseMatrix-class`, and an example below.

References

<https://math.nist.gov/MatrixMarket/>

<https://sparse.tamu.edu/>

Examples

```
str(pores <- readMM(system.file("external/pores_1.mtx", package = "Matrix")))
str(utm <- readHB(system.file("external/utm300.rua" , package = "Matrix")))
str(lundA <- readMM(system.file("external/lund_a.mtx" , package = "Matrix")))
str(lundA <- readHB(system.file("external/lund_a.rsa" , package = "Matrix")))
## https://math.nist.gov/MatrixMarket/data/Harwell-Boeing/counterx/counterx.htm
str(jgl <- readMM(system.file("external/jgl009.mtx" , package = "Matrix")))

## NOTE: The following examples take quite some time
## ---- even on a fast internet connection:
if(FALSE) {
## The URL has been corrected, but we need an untar step:
u. <- url("https://www.cise.ufl.edu/research/sparse/RB/Boeing/msc00726.tar.gz")
str(sm <- readHB(gzcon(u.)))
}

data(KNex, package = "Matrix")
## Store as MatrixMarket (".mtx") file, here inside temporary dir./folder:
(MMfile <- file.path(tempdir(), "mmMM.mtx"))
writeMM(KNex$mm, file=MMfile)
file.info(MMfile)[,c("size", "ctime")] # (some confirmation of the file's)

## very simple export - in triplet format - to text file:
data(CAex, package = "Matrix")
s.CA <- summary(CAex)
s.CA # shows (i, j, x) [columns of a data frame]
message("writing to ", outf <- tempfile())
write.table(s.CA, file = outf, row.names=FALSE)
## and read it back -- showing off sparseMatrix():
str(dd <- read.table(outf, header=TRUE))
## has columns (i, j, x) -> we can use via do.call() as arguments to sparseMatrix():
mm <- do.call(sparseMatrix, dd)
stopifnot(all.equal(mm, CAex, tolerance=1e-15))
```

Description

Multiplies a matrix or vector on the left or right by a factor from a matrix factorization or its transpose.

Usage

```
facmul(x, factor, y, trans = FALSE, left = TRUE, ...)
```

Arguments

<code>x</code>	a MatrixFactorization object.
<code>factor</code>	a character string indicating a factor in the factorization represented by <code>x</code> , typically an element of <code>names(expand2(x, ...))</code> .
<code>y</code>	a matrix or vector to be multiplied on the left or right by the factor or its transpose.
<code>trans</code>	a logical indicating if the transpose of the factor should be used, rather than the factor itself.
<code>left</code>	a logical indicating if the <code>y</code> should be multiplied on the left by the factor, rather than on the right.
<code>...</code>	further arguments passed to or from methods.

Details

`facmul` is experimental and currently no methods are exported from **Matrix**.

Value

The value of `op(M) %*% y` or `y %*% op(M)`, depending on `left`, where `M` is the factor (always *without* `dimnames`) and `op(M)` is `M` or `t(M)`, depending on `trans`.

Examples

```
## Conceptually, methods for 'facmul' _would_ behave as follows ...
## Not run:
n <- 3L
x <- lu(Matrix(rnorm(n * n), n, n))
y <- rnorm(n)
L <- unname(expand2(x)[[nm <- "L"]])
stopifnot(exprs = {
  all.equal(facmul(x, nm, y, trans = FALSE, left = TRUE), L %*% y)
  all.equal(facmul(x, nm, y, trans = FALSE, left = FALSE), y %*% L)
  all.equal(facmul(x, nm, y, trans = TRUE, left = TRUE), crossprod(L, y))
  all.equal(facmul(x, nm, y, trans = TRUE, left = FALSE), tcrossprod(y, L))
})
```

```

})

## End(Not run)

```

fastMisc

“Low Level” Coercions and Methods

Description

“Semi-API” functions used internally by **Matrix**, often to bypass S4 dispatch and avoid the associated overhead. These are exported to provide this capability to expert users. Typical users should continue to rely on S4 generic functions to dispatch suitable methods, by calling, e.g., `as(. , <class>)` for coercions.

Usage

```

.M2kind(from, kind = ".", sparse = NA)

.M2gen(from, kind = ".")
.M2sym(from, ...)
.M2tri(from, ...)
.M2diag(from)

.M2v(from)
.M2m(from)
.M2unpacked(from)
.M2packed(from)
.M2C(from)
.M2R(from)
.M2T(from)

.M2V(from)
.m2V(from, kind = ".")

.sparse2dense(from, packed = FALSE)
.diag2dense(from, kind = ".", shape = "t", packed = FALSE, uplo = "U")
.ind2dense(from, kind = "n")
.m2dense(from, class = ".ge", uplo = "U", diag = "N", trans = FALSE)

.dense2sparse(from, repr = "C")
.diag2sparse(from, kind = ".", shape = "t", repr = "C", uplo = "U")
.ind2sparse(from, kind = "n", repr = ".")
.m2sparse(from, class = ".gC", uplo = "U", diag = "N", trans = FALSE)

.tCRT(x, lazy = TRUE)

.diag.dsC(x, Chx = Cholesky(x, LDL = TRUE), res.kind = "diag")

```

```
.solve.dgC.lu (a, b, tol = .Machine$double.eps, check = TRUE)
.solve.dgC.qr (a, b, order = 3L, check = TRUE)
.solve.dgC.chol(a, b, check = TRUE)

.updateCHMfactor(object, parent, mult = 0)
```

Arguments

from, x, a, b	a Matrix , matrix, or vector.
kind	a string (".", "z", "n", "l", or "d") specifying the “kind” of the result. "." indicates that the kind of from should be preserved. "z" is equivalent to "n" if from is complex and to "d" otherwise. "n" indicates that the result should inherit from nMatrix or nsparseVector (and so on).
shape	a string (".", "g", "s", or "t") specifying the “shape” of the result. "." indicates that the shape of from should be preserved. "g" indicates that the result should inherit from generalMatrix (and so on).
repr	a string (".", "C", "R", or "T") specifying the sparse representation of the result. "." is accepted only by .ind2sparse and indicates the most efficient representation, which is "C" ("R") for <code>margin = 2 (1)</code> . "C" indicates that the result should inherit from CsparseMatrix (and so on).
packed	a logical indicating if the result should inherit from packedMatrix rather than from unpackedMatrix . It is ignored for from inheriting from generalMatrix .
sparse	a logical indicating if the result should inherit from sparseMatrix rather than from denseMatrix . If NA, then the result will be formally sparse if and only if from is.
uplo	a string ("U" or "L") indicating whether the result (if symmetric or triangular) should store the upper or lower triangle of from. The elements of from in the opposite triangle are ignored.
diag	a string ("N" or "U") indicating whether the result (if triangular) should be formally nonunit or unit triangular. In the unit triangular case, the diagonal elements of from are ignored.
trans	a logical indicating if the result should be a 1-row matrix rather than a 1-column matrix where from is a vector but not a matrix.
class	a string whose first three characters specify the class of the result. It should match the pattern <code>^[.nld](ge sy tr sp tp)"</code> for .m2dense and <code>^[.nld][gst][CRT]"</code> for .m2sparse , where "." in the first position is equivalent to "l" for logical arguments and "d" for numeric arguments.
...	optional arguments passed to isSymmetric or isTriangular .
lazy	a logical indicating if the transpose should be constructed with minimal allocation, but possibly <i>without</i> preserving representation.
Chx	optionally, the Cholesky (x, ...) factorization of x. If supplied, then x is unused.
res.kind	a string in <code>c("trace", "sumLog", "prod", "min", "max", "range", "diag", "diagBack")</code> .

tol	see lu-methods .
order	see qr-methods .
check	a logical indicating if the first argument should be tested for inheritance from dgCMatrix and coerced if necessary. Set to FALSE for speed only if it is known to already inherit from dgCMatrix .
object	a Cholesky factorization inheriting from virtual class CHMfactor, almost always the result of a call to generic function Cholesky .
parent	an object of class dsCMatrix or class dgCMatrix .
mult	a numeric vector of positive length. Only the first element is used, and that must be finite.

Details

Functions with names of the form `.<A>2` implement coercions from virtual class A to the “nearest” non-virtual subclass of virtual class B, where the virtual classes are abbreviated as follows:

M [Matrix](#)
V [sparseVector](#)
m [matrix](#)
v [vector](#)
dense [denseMatrix](#)
unpacked [unpackedMatrix](#)
packed [packedMatrix](#)
sparse [CsparseMatrix](#), [RsparseMatrix](#), or [TsparseMatrix](#)
C [CsparseMatrix](#)
R [RsparseMatrix](#)
T [TsparseMatrix](#)
gen [generalMatrix](#)
sym [symmetricMatrix](#)
tri [triangularMatrix](#)
diag [diagonalMatrix](#)
ind [indMatrix](#)

Abbreviations should be seen as a guide, rather than as an exact description of behaviour. Notably, `.m2dense`, `.m2sparse`, and `.m2V` accept vectors that are not matrices.

`.tCRT(x)`: If `lazy = TRUE`, then `.tCRT` constructs the transpose of `x` using the most efficient representation, which for ‘CRT’ is ‘RCT’. If `lazy = FALSE`, then `.tCRT` preserves the representation of `x`, behaving as the corresponding methods for generic function `t`.

`.diag.dsC(x)`: `.diag.dsC` computes (or uses if `Chx` is supplied) the Cholesky factorization of `x` as LDL' in order to calculate one of several possible statistics from the diagonal entries of D . See `res.kind` under ‘Arguments’.

`.solve.dgC.*(a, b)`: `.solve.dgC.lu(a, b)` needs a square matrix `a`. `.solve.dgC.qr(a, b)` needs a “long” matrix `a`, with `nrow(a) >= ncol(a)`. `.solve.dgC.chol(a, b)` needs a “wide” matrix `a`, with `nrow(a) <= ncol(a)`.

All three may be used to solve sparse linear systems directly. Only `.solve.dgC.qr` and `.solve.dgC.chol` be used to solve sparse *least squares* problems.

`.updateCHMfactor(object, parent, mult)`: `.updateCHMfactor` updates `object` with the result of Cholesky factorizing `F(parent) + mult[1] * diag(nrow(parent))`, i.e., `F(parent)` plus `mult[1]` times the identity matrix, where `F = identity` if `parent` is a `dsCMatrix` and `F = tcrossprod` if `parent` is a `dgCMatrix`. The nonzero pattern of `F(parent)` must match that of `S` if `object = Cholesky(S, ...)`.

Examples

```
D. <- diag(x = c(1, 1, 2, 3, 5, 8))
D.0 <- Diagonal(x = c(0, 0, 0, 3, 5, 8))
S. <- toeplitz(as.double(1:6))
C. <- new("dgCMatrix", Dim = c(3L, 4L),
          p = c(0L, 1L, 1L, 1L, 3L), i = c(1L, 0L, 2L), x = c(-8, 2, 3))

stopifnot(exprs = {
  identical(.M2tri(D.), as(D., "triangularMatrix"))
  identical(.M2sym(D.), as(D., "symmetricMatrix"))
  identical(.M2diag(D.), as(D., "diagonalMatrix"))
  identical(.M2kind(C., "l"),
            as(C., "lMatrix"))
  identical(.M2kind(.sparse2dense(C.), "l"),
            as(as(C., "denseMatrix"), "lMatrix"))
  identical(.diag2sparse(D.0, ".", "t", "C"),
            .dense2sparse(.diag2dense(D.0, ".", "t", TRUE), "C"))
  identical(.M2gen(.diag2dense(D.0, ".", "s", FALSE)),
            .sparse2dense(.M2gen(.diag2sparse(D.0, ".", "s", "T"))))
  identical(S.,
            .M2m(.m2sparse(S., ".sR")))
  identical(S. * lower.tri(S.) + diag(1, 6L),
            .M2m(.m2dense(S., ".tr", "L", "U")))
  identical(.M2R(C.), .M2R(.M2T(C.)))
  identical(.tCRT(C.), .M2R(t(C.)))
})

A <- tcrossprod(C.)/6 + Diagonal(3, 1/3); A[1,2] <- 3; A
stopifnot(exprs = {
  is.numeric(x. <- c(2.2, 0, -1.2))
  all.equal(x., .solve.dgC.lu(A, c(1,0,0), check=FALSE))
  all.equal(x., .solve.dgC.qr(A, c(1,0,0), check=FALSE))
})

## Solving sparse least squares:

X <- rbind(A, Diagonal(3)) # design matrix X (for L.S.)
Xt <- t(X)                # *transposed* X (for L.S.)
(y <- drop(crossprod(Xt, 1:3)) + c(-1,1)/1000) # small rand.err.
```

```
str(solveCh <- .solve.dgC.chol(Xt, y, check=FALSE)) # Xt *is* dgC..
stopifnot(exprs = {
  all.equal(solveCh$coef, 1:3, tol = 1e-3)# rel.err ~ 1e-4
  all.equal(solveCh$coef, drop(solve(tcrossprod(Xt), Xt %% y)))
  all.equal(solveCh$coef, .solve.dgC.qr(X, y, check=FALSE))
})
```

forceSymmetric-methods

Force a Matrix to 'symmetricMatrix' Without Symmetry Checks

Description

Force a square matrix `x` to a `symmetricMatrix`, **without** a symmetry check as it would be applied for `as(x, "symmetricMatrix")`.

Usage

```
forceSymmetric(x, uplo)
```

Arguments

<code>x</code>	any square matrix (of numbers), either “traditional” (<code>matrix</code>) or inheriting from <code>Matrix</code> .
<code>uplo</code>	optional string, “U” or “L” indicating which “triangle” half of <code>x</code> should determine the result. The default is “U” unless <code>x</code> already has a <code>uplo</code> slot (i.e., when it is <code>symmetricMatrix</code> , or <code>triangularMatrix</code>), where the default will be <code>x@uplo</code> .

Value

a square matrix inheriting from class `symmetricMatrix`.

See Also

`symmpart` for the symmetric part of a matrix, or the coercions `as(x, <symmetricMatrix class>)`.

Examples

```
## Hilbert matrix
i <- 1:6
h6 <- 1/outer(i - 1L, i, "+")
sd <- sqrt(diag(h6))
hh <- t(h6/sd)/sd # theoretically symmetric
isSymmetric(hh, tol=0) # FALSE; hence
try( as(hh, "symmetricMatrix") ) # fails, but this works fine:
H6 <- forceSymmetric(hh)

## result can be pretty surprising:
(M <- Matrix(1:36, 6))
```

```
forceSymmetric(M) # symmetric, hence very different in lower triangle
(tm <- tril(M))
forceSymmetric(tm)
```

formatSparseM

*Formatting Sparse Numeric Matrices Utilities***Description**

Utilities for formatting sparse numeric matrices in a flexible way. These functions are used by the [format](#) and `print` methods for sparse matrices and can be applied as well to standard R matrices. Note that *all* arguments but the first are optional.

`formatSparseM()` is the main “workhorse” of [formatSpMatrix](#), the format method for sparse matrices.

`.formatSparseSimple()` is a simple helper function, also dealing with (short/empty) column names construction.

Usage

```
formatSparseM(x, zero.print = ".", align = c("fancy", "right"),
             m = as(x,"matrix"), asLogical=NULL, uniDiag=NULL,
             digits=NULL, cx, iN0, dn = dimnames(m))
```

```
.formatSparseSimple(m, asLogical=FALSE, digits=NULL,
                   col.names, note.dropping.colnames = TRUE,
                   dn=dimnames(m))
```

Arguments

<code>x</code>	an R object inheriting from class sparseMatrix .
<code>zero.print</code>	character which should be used for <i>structural</i> zeroes. The default "." may occasionally be replaced by " " (blank); using "0" would look almost like <code>print()</code> ing of non-sparse matrices.
<code>align</code>	a string specifying how the <code>zero.print</code> codes should be aligned, see formatSpMatrix .
<code>m</code>	(optional) a (standard R) matrix version of <code>x</code> .
<code>asLogical</code>	should the matrix be formatted as a logical matrix (or rather as a numeric one); mostly for <code>formatSparseM()</code> .
<code>uniDiag</code>	logical indicating if the diagonal entries of a sparse unit triangular or unit-diagonal matrix should be formatted as "I" instead of "1" (to emphasize that the 1's are “structural”).
<code>digits</code>	significant digits to use for printing, see print.default .
<code>cx</code>	(optional) character matrix; a formatted version of <code>x</code> , still with strings such as "0.00" for the zeros.
<code>iN0</code>	(optional) integer vector, specifying the location of the <i>non-zeroes</i> of <code>x</code> .

col.names, note.dropping.colnames
 see [formatSpMatrix](#).

dn [dimnames](#) to be used; a list (of length two) with row and column names (or NULL).

Value

a character matrix like `cx`, where the zeros have been replaced with (padded versions of) `zero.print`. As this is a *dense* matrix, do not use these functions for really large (really) sparse matrices!

Author(s)

Martin Maechler

See Also

[formatSpMatrix](#) which calls `formatSparseM()` and is the `format` method for sparse matrices.
[printSpMatrix](#) which is used by the (typically implicitly called) `show` and `print` methods for sparse matrices.

Examples

```
m <- suppressWarnings(matrix(c(0, 3.2, 0,0, 11,0,0,0,0,-7,0), 4,9))
fm <- formatSparseM(m)
noquote(fm)
## nice, but this is nicer {with "units" vertically aligned}:
print(fm, quote=FALSE, right=TRUE)
## and "the same" as :
Matrix(m)

## align = "right" is cheaper --> the "." are not aligned:
noquote(f2 <- formatSparseM(m,align="r"))
stopifnot(f2 == fm | m == 0, dim(f2) == dim(m),
          (f2 == ".") == (m == 0))
```

generalMatrix-class *Class "generalMatrix" of General Matrices*

Description

Virtual class of “general” matrices; i.e., matrices that do not have a known property such as symmetric, triangular, or diagonal.

Objects from the Class

A virtual Class: No objects may be created from it.

Slots

`Dim`, `Dimnames` inherited from virtual class [Matrix](#).

`factors` a list of [MatrixFactorization](#) objects caching factorizations of the matrix. Typically, it is initialized as an empty list and updated “automagically” whenever a factorization is computed.

Extends

Class “[Matrix](#)”, directly.

See Also

Virtual classes [symmetricMatrix](#), [triangularMatrix](#), and [diagonalMatrix](#).

Hilbert

Generate a Hilbert matrix

Description

Generate the n by n symmetric Hilbert matrix. Because these matrices are ill-conditioned for moderate to large n , they are often used for testing numerical linear algebra code.

Usage

```
Hilbert(n)
```

Arguments

`n` a non-negative integer.

Value

the n by n symmetric Hilbert matrix as a “[dpoMatrix](#)” object.

See Also

the class [dpoMatrix](#)

Examples

```
Hilbert(6)
```

Description

Methods for function `image` in package **Matrix**. An image of a matrix simply color codes all matrix entries and draws the $n \times m$ matrix using an $n \times m$ grid of (colored) rectangles.

The **Matrix** package image methods are based on `levelplot()` from package **lattice**; hence these methods return an “object” of class “trellis”, producing a graphic when (auto-) `print()`ed.

Usage

```
## S4 method for signature 'dgTMatrix'
image(x,
      xlim = c(1, di[2]),
      ylim = c(di[1], 1), aspect = "iso",
      sub = sprintf("Dimensions: %d x %d", di[1], di[2]),
      xlab = "Column", ylab = "Row", cuts = 15,
      useRaster = FALSE,
      useAbs = NULL, colorkey = !useAbs,
      col.regions = NULL,
      lwd = NULL, border.col = NULL, ...)
```

Arguments

<code>x</code>	a Matrix object, i.e., fulfilling <code>is(x, "Matrix")</code> .
<code>xlim, ylim</code>	x- and y-axis limits; may be used to “zoom into” matrix. Note that x, y “feel reversed”: <code>ylim</code> is for the rows (= 1st index) and <code>xlim</code> for the columns (= 2nd index). For convenience, when the limits are integer valued, they are both extended by 0.5; also, <code>ylim</code> is always used decreasingly.
<code>aspect</code>	aspect ratio specified as number (y/x) or string; see <code>levelplot</code> .
<code>sub, xlab, ylab</code>	axis annotation with sensible defaults; see <code>plot.default</code> .
<code>cuts</code>	number of levels the range of matrix values would be divided into.
<code>useRaster</code>	logical indicating if raster graphics should be used (instead of the tradition rectangle vector drawing). If true, <code>panel.levelplot.raster</code> (from lattice package) is used, and the colorkey is also done via rasters, see also <code>levelplot</code> and possibly <code>grid.raster</code> . Note that using raster graphics may often be faster, but can be slower, depending on the matrix dimensions and the graphics device (dimensions).
<code>useAbs</code>	logical indicating if <code>abs(x)</code> should be shown; if TRUE, the former (implicit) default, the default <code>col.regions</code> will be grey colors (and no colorkey drawn). The default is FALSE unless the matrix has no negative entries.
<code>colorkey</code>	logical indicating if a color key aka ‘legend’ should be produced. Default is to draw one, unless <code>useAbs</code> is true. You can also specify a list, see <code>levelplot</code> , such as <code>list(raster=TRUE)</code> in the case of rastering.

<code>col.regions</code>	vector of gradually varying colors; see levelplot .
<code>lwd</code>	(only used when <code>useRaster</code> is <code>false</code> ;) non-negative number or <code>NULL</code> (default), specifying the line-width of the rectangles of each non-zero matrix entry (drawn by grid.rect). The default depends on the matrix dimension and the device size.
<code>border.col</code>	color for the border of each rectangle. <code>NA</code> means no border is drawn. When <code>NULL</code> as by default, <code>border.col <- if(lwd < .01) NA else NULL</code> is used. Consider using an opaque color instead of <code>NULL</code> which corresponds to <code>grid::get.gpar("col")</code> .
<code>...</code>	further arguments passed to methods and levelplot , notably at for specifying (possibly non equidistant) cut values for dividing the matrix values (superseding cuts above).

Value

as all **lattice** graphics functions, `image(<Matrix>)` returns a "trellis" object, effectively the result of [levelplot\(\)](#).

Methods

All methods currently end up calling the method for the [dgTMatrix](#) class. Use `showMethods(image)` to list them all.

See Also

[levelplot](#), and [print.trellis](#) from package **lattice**.

Examples

```
showMethods(image)
## And if you want to see the method definitions:
showMethods(image, includeDefs = TRUE, inherited = FALSE)

data(CAex, package = "Matrix")
image(CAex, main = "image(CAex)") -> imgC; imgC
stopifnot(!is.null(leg <- imgC$legend), is.list(leg$right)) # failed for 2 days ..
image(CAex, useAbs=TRUE, main = "image(CAex, useAbs=TRUE)")

cCA <- Cholesky(crossprod(CAex), Imult = .01)
## See ?print.trellis --- place two image() plots side by side:
print(image(cCA, main="Cholesky(crossprod(CAex), Imult = .01)",
  split=c(x=1,y=1,nx=2, ny=1), more=TRUE)
print(image(cCA, useAbs=TRUE),
  split=c(x=2,y=1,nx=2,ny=1))

data(USCounties, package = "Matrix")
image(USCounties)# huge
image(sign(USCounties))## just the pattern
# how the result looks, may depend heavily on
# the device, screen resolution, antialiasing etc
# e.g. x11(type="Xlib") may show very differently than cairo-based
```

```

## Drawing borders around each rectangle;
  # again, viewing depends very much on the device:
image(USCounties[1:400,1:200], lwd=.1)
## Using (xlim,ylim) has advantage : matrix dimension and (col/row) indices:
image(USCounties, c(1,200), c(1,400), lwd=.1)
image(USCounties, c(1,300), c(1,200), lwd=.5 )
image(USCounties, c(1,300), c(1,200), lwd=.01)
## These 3 are all equivalent :
(I1 <- image(USCounties, c(1,100), c(1,100), useAbs=FALSE))
I2 <- image(USCounties, c(1,100), c(1,100), useAbs=FALSE, border.col=NA)
I3 <- image(USCounties, c(1,100), c(1,100), useAbs=FALSE, lwd=2, border.col=NA)
stopifnot(all.equal(I1, I2, check.environment=FALSE),
          all.equal(I2, I3, check.environment=FALSE))
## using an opaque border color
image(USCounties, c(1,100), c(1,100), useAbs=FALSE, lwd=3, border.col = adjustcolor("skyblue", 1/2))

if(interactive() || nzchar(Sys.getenv("R_MATRIX_CHECK_EXTRA"))) {
## Using raster graphics: For PDF this would give a 77 MB file,
## however, for such a large matrix, this is typically considerably
## *slower* (than vector graphics rectangles) in most cases :
if(doPNG <- !dev.interactive())
  png("image-USCounties-raster.png", width=3200, height=3200)
image(USCounties, useRaster = TRUE) # should not suffer from anti-aliasing
if(doPNG)
  dev.off()
  ## and now look at the *.png image in a viewer you can easily zoom in and out
}#only if(doExtras)

```

index-class

Virtual Class "index" of Index Vectors

Description

Class `index` is a virtual class designating index vectors, or “subscripts”, for (possibly named) vectors and arrays. It is typically used in signatures of methods for the subscript and subassignment operators, namely `[` and `[<-`. It is implemented as a *union* of the atomic vector classes `numeric`, `logical`, and `character`.

See Also

`[`, `[-methods`, and `[<--methods`.

Examples

```
showClass("index")
```


Description

The `indMatrix` class is the class of row and column *index* matrices, stored as 1-based integer index vectors. A row (column) index matrix is a matrix whose rows (columns) are standard unit vectors. Such matrices are useful when mapping observations to discrete sets of covariate values.

Multiplying a matrix on the left by a row index matrix is equivalent to indexing its rows, i.e., sampling the rows “with replacement”. Analogously, multiplying a matrix on the right by a column index matrix is equivalent to indexing its columns. Indeed, such products are implemented in **Matrix** as indexing operations; see ‘Details’ below.

A matrix whose rows *and* columns are standard unit vectors is called a *permutation* matrix. This special case is designated by the `pMatrix` class, a direct subclass of `indMatrix`.

Details

The transpose of an index matrix is an index matrix with identical `perm` but opposite `margin`. Hence the transpose of a row index matrix is a column index matrix, and vice versa.

The cross product of a row index matrix `R` and itself is a diagonal matrix whose diagonal entries are the the number of entries in each column of `R`.

Given a row index matrix `R` with `perm` slot `p`, a column index matrix `C` with `perm` slot `q`, and a matrix `M` with conformable dimensions, we have

$$\begin{array}{llll}
 RM & = & R \%*\% M & = & M[p,] \\
 MC & = & M \%*\% C & = & M[, q] \\
 C'M & = & \text{crossprod}(C, M) & = & M[q,] \\
 MR' & = & \text{tcrossprod}(M, R) & = & M[, p] \\
 R'R & = & \text{crossprod}(R) & = & \text{Diagonal}(x=\text{tabulate}(p, \text{ncol}(R))) \\
 CC' & = & \text{tcrossprod}(C) & = & \text{Diagonal}(x=\text{tabulate}(q, \text{nrow}(C)))
 \end{array}$$

Operations on index matrices that result in index matrices will accordingly return an `indMatrix`. These include products of two column index matrices and (equivalently) column-indexing of a column index matrix (when dimensions are not dropped). Most other operations on `indMatrix` treat them as sparse nonzero pattern matrices (i.e., inheriting from virtual class `nsparseMatrix`). Hence vector-valued subsets of `indMatrix`, such as those given by `diag`, are always of type “logical”.

Objects from the Class

Objects can be created explicitly with calls of the form `new("indMatrix", ...)`, but they are more commonly created by coercing 1-based integer index vectors, with calls of the form `as(., "indMatrix")`; see ‘Methods’ below.

Slots

`margin` an integer, either 1 or 2, specifying whether the matrix is a row (1) or column (2) index.

`perm` a 1-based integer index vector, i.e., a vector of length `Dim[margin]` with elements taken from `1:Dim[1+margin%%2]`.

`Dim,Dimnames` inherited from virtual superclass `Matrix`.

Extends

Classes "`sparseMatrix`" and "`generalMatrix`", directly.

Methods

`%%` signature(`x = "indMatrix"`, `y = "Matrix"`) and others listed by `showMethods("%*%", classes = "indMatrix")`: matrix products implemented where appropriate as indexing operations.

`coerce` signature(`from = "numeric"`, `to = "indMatrix"`): supporting typical `indMatrix` construction from a vector of positive integers. Row indexing is assumed.

`coerce` signature(`from = "list"`, `to = "indMatrix"`): supporting `indMatrix` construction for row *and* column indexing, including index vectors of length 0 and index vectors whose maximum is less than the number of rows or columns being indexed.

`coerce` signature(`from = "indMatrix"`, `to = "matrix"`): coercion to a traditional `matrix` of `logical` type, with `FALSE` and `TRUE` in place of 0 and 1.

`t` signature(`x = "indMatrix"`): the transpose, which is an `indMatrix` with identical `perm` but opposite `margin`.

`rowSums, rowMeans, colSums, colMeans` signature(`x = "indMatrix"`): row and column sums and means.

`rbind2, cbind2` signature(`x = "indMatrix"`, `y = "indMatrix"`): row-wise catenation of two row index matrices with equal numbers of columns and column-wise catenation of two column index matrices with equal numbers of rows.

kronecker signature(`X = "indMatrix"`, `Y = "indMatrix"`): Kronecker product of two row index matrices or two column index matrices, giving the row or column index matrix corresponding to their "interaction".

Author(s)

Fabian Scheipl at 'uni-muenchen.de', building on the existing class `pMatrix` after a nice hike's conversation with Martin Maechler. Methods for `crossprod(x, y)` and `kronecker(x, y)` with both arguments inheriting from `indMatrix` were made considerably faster thanks to a suggestion by Boris Vaillant. Diverse tweaks by Martin Maechler and Mikael Jagan, notably the latter's implementation of `margin`, prior to which the `indMatrix` class was designated only for row index matrices.

See Also

Subclass `pMatrix` of permutation matrices, a special case of index matrices; virtual class `nMatrix` of nonzero pattern matrices, and its subclasses.

Examples

```

p1 <- as(c(2,3,1), "pMatrix")
(sm1 <- as(rep(c(2,3,1), e=3), "indMatrix"))
stopifnot(all(sm1 == p1[rep(1:3, each=3),]))

## row-indexing of a <pMatrix> turns it into an <indMatrix>:
class(p1[rep(1:3, each=3),])

set.seed(12) # so we know '10' is in sample
## random index matrix for 30 observations and 10 unique values:
(s10 <- as(sample(10, 30, replace=TRUE), "indMatrix"))

## Sample rows of a numeric matrix :
(mm <- matrix(1:10, nrow=10, ncol=3))
s10 %*% mm

set.seed(27)
IM1 <- as(sample(1:20, 100, replace=TRUE), "indMatrix")
IM2 <- as(sample(1:18, 100, replace=TRUE), "indMatrix")
(c12 <- crossprod(IM1, IM2))
## same as cross-tabulation of the two index vectors:
stopifnot(all(c12 - unclass(table(IM1@perm, IM2@perm)) == 0))

# 3 observations, 4 implied values, first does not occur in sample:
as(2:4, "indMatrix")
# 3 observations, 5 values, first and last do not occur in sample:
as(list(2:4, 5), "indMatrix")

as(sm1, "nMatrix")
s10[1:7, 1:4] # gives an "ngTMatrix" (most economic!)
s10[1:4, ] # preserves "indMatrix"-class

I1 <- as(c(5:1,6:4,7:3), "indMatrix")
I2 <- as(7:1, "pMatrix")
(I12 <- rbind(I1, I2))
stopifnot(is(I12, "indMatrix"),
          identical(I12, rbind(I1, I2)),
          colSums(I12) == c(2L,2:4,4:2))

```

Description

invertPerm and signPerm compute the inverse and sign of a length-n permutation vector. isPerm tests if a length-n integer vector is a valid permutation vector. asPerm coerces a length-m transposition vector to a length-n permutation vector, where $m \leq n$.

Usage

```
invertPerm(p, off = 1L, ioff = 1L)
signPerm(p, off = 1L)
isPerm(p, off = 1L)
asPerm(pivot, off = 1L, ioff = 1L, n = length(pivot))

invPerm(p, zero.p = FALSE, zero.res = FALSE)
```

Arguments

<code>p</code>	an integer vector of length <code>n</code> .
<code>pivot</code>	an integer vector of length <code>m</code> .
<code>off</code>	an integer offset, indicating that <code>p</code> is a permutation of <code>off+0:(n-1)</code> or that <code>pivot</code> contains <code>m</code> values sampled with replacement from <code>off+0:(n-1)</code> .
<code>ioff</code>	an integer offset, indicating that the result should be a permutation of <code>ioff+0:(n-1)</code> .
<code>n</code>	a integer greater than or equal to <code>m</code> , indicating the length of the result. Transpositions are applied to a permutation vector initialized as <code>seq_len(n)</code> .
<code>zero.p</code>	a logical. Equivalent to <code>off=0</code> if TRUE and <code>off=1</code> if FALSE.
<code>zero.res</code>	a logical. Equivalent to <code>ioff=0</code> if TRUE and <code>ioff=1</code> if FALSE.

Details

`invertPerm(p, off, ioff=1)` is equivalent to `order(p)` or `sort.list(p)` for all values of `off`. For the default value `off=1`, it returns the value of `p` after `p[p] <- seq_along(p)`.

`invPerm` is a simple wrapper around `invertPerm`, retained for backwards compatibility.

Value

By default, i.e., with `off=1` and `ioff=1`:

`invertPerm(p)` returns an integer vector of length `length(p)` such that `p[invertPerm(p)]` and `invertPerm(p)[p]` are both `seq_along(p)`, i.e., the identity permutation.

`signPerm(p)` returns 1 if `p` is an even permutation and -1 otherwise (i.e., if `p` is odd).

`isPerm(p)` returns TRUE if `p` is a permutation of `seq_along(p)` and FALSE otherwise.

`asPerm(pivot)` returns the result of transposing elements `i` and `pivot[i]` of a permutation vector initialized as `seq_len(n)`, for `i` in `seq_along(pivot)`.

See Also

Class [pMatrix](#) of permutation matrices.

Examples

```
p <- sample(10L) # a random permutation vector
ip <- invertPerm(p)
s <- signPerm(p)
```

```

## 'p' and 'ip' are indeed inverses:
stopifnot(exprs = {
  isPerm(p)
  isPerm(ip)
  identical(s, 1L) || identical(s, -1L)
  identical(s, signPerm(ip))
  identical(p[ip], 1:10)
  identical(ip[p], 1:10)
  identical(invertPerm(ip), p)
})

## Product of transpositions (1 2)(2 1)(4 3)(6 8)(10 1) = (3 4)(6 8)(1 10)
pivot <- c(2L, 1L, 3L, 3L, 5L, 8L, 7L, 8L, 9L, 1L)
q <- asPerm(pivot)
stopifnot(exprs = {
  identical(q, c(10L, 2L, 4L, 3L, 5L, 8L, 7L, 6L, 9L, 1L))
  identical(q[q], seq_len(10L)) # because the permutation is odd:
  signPerm(q) == -1L
})

invPerm # a less general version of 'invertPerm'

```

is.na-methods

is.na(), is.finite() Methods for 'Matrix' Objects

Description

Methods for generic functions [anyNA\(\)](#), [is.na\(\)](#), [is.nan\(\)](#), [is.infinite\(\)](#), and [is.finite\(\)](#), for objects inheriting from virtual class [Matrix](#) or [sparseVector](#).

Usage

```

## S4 method for signature 'denseMatrix'
is.na(x)
## S4 method for signature 'sparseMatrix'
is.na(x)
## S4 method for signature 'diagonalMatrix'
is.na(x)
## S4 method for signature 'indMatrix'
is.na(x)
## S4 method for signature 'sparseVector'
is.na(x)
## ...
## and likewise for anyNA, is.nan, is.infinite, is.finite

```

Arguments

`x` an R object, here a sparse or dense matrix or vector.

Value

For `is.*()`, an `nMatrix` or `nsparseVector` matching the dimensions of `x` and specifying the positions in `x` of (some subset of) `NA`, `NaN`, `Inf`, and `-Inf`. For `anyNA()`, `TRUE` if `x` contains `NA` or `NaN` and `FALSE` otherwise.

See Also

[NA](#), [NaN](#), [Inf](#)

Examples

```
(M <- Matrix(1:6, nrow = 4, ncol = 3,
            dimnames = list(letters[1:4], LETTERS[1:3])))
stopifnot(!anyNA(M), !any(is.na(M)))

M[2:3, 2] <- NA
(inM <- is.na(M))
stopifnot(anyNA(M), sum(inM) == 2)

(A <- spMatrix(nrow = 10, ncol = 20,
              i = c(1, 3:8), j = c(2, 9, 6:10), x = 7 * (1:7)))
stopifnot(!anyNA(A), !any(is.na(A)))

A[2, 3] <- A[1, 2] <- A[5, 5:9] <- NA
(inA <- is.na(A))
stopifnot(anyNA(A), sum(inA) == 1 + 1 + 5)
```

is.null.DN

Are the Dimnames dn NULL-like ?

Description

Are the `dimnames` dn `NULL`-like?

`is.null.DN(dn)` is less strict than `is.null(dn)`, because it is also true (`TRUE`) when the `dimnames` `dn` are “like” `NULL`, or `list(NULL, NULL)`, as they can easily be for the traditional R matrices (`matrix`) which have no formal `class` definition, and hence much freedom in how their `dimnames` look like.

Usage

```
is.null.DN(dn)
```

Arguments

`dn` `dimnames()` of a `matrix`-like R object.

Value

logical `TRUE` or `FALSE`.

Note

This function is really to be used on “traditional” matrices rather than those inheriting from `Matrix`, as the latter will always have `dimnames` `list(NULL, NULL)` exactly, in such a case.

Author(s)

Martin Maechler

See Also

`is.null`, `dimnames`, `matrix`.

Examples

```
m1 <- m2 <- m3 <- m4 <- m <-
  matrix(round(100 * rnorm(6)), 2, 3)
dimnames(m1) <- list(NULL, NULL)
dimnames(m2) <- list(NULL, character())
dimnames(m3) <- rev(dimnames(m2))
dimnames(m4) <- rep(list(character()),2)

m4 # prints absolutely identically to m

c.o <- capture.output
cm <- c.o(m)
stopifnot(exprs = {
  m == m1; m == m2; m == m3; m == m4
  identical(cm, c.o(m1)); identical(cm, c.o(m2))
  identical(cm, c.o(m3)); identical(cm, c.o(m4))
})

hasNoDimnames <- function(.) is.null.DN(dimnames(.))
stopifnot(exprs = {
  hasNoDimnames(m)
  hasNoDimnames(m1); hasNoDimnames(m2)
  hasNoDimnames(m3); hasNoDimnames(m4)
  hasNoDimnames(Matrix(m) -> M)
  hasNoDimnames(as(M, "sparseMatrix"))
})
```

isSymmetric-methods *Methods for Function 'isSymmetric' in Package 'Matrix'*

Description

`isSymmetric` tests whether its argument is a symmetric square matrix, by default tolerating some numerical fuzz and requiring symmetric `[dD]imnames` in addition to symmetry in the mathematical sense. `isSymmetric` is a generic function in **base**, which has a `method` for traditional matrices of implicit class `"matrix"`. Methods are defined here for various proper and virtual classes in **Matrix**, so that `isSymmetric` works for all objects inheriting from virtual class `"Matrix"`.

Usage

```
## S4 method for signature 'denseMatrix'
isSymmetric(object, checkDN = TRUE, ...)
## S4 method for signature 'CsparseMatrix'
isSymmetric(object, checkDN = TRUE, ...)
## S4 method for signature 'RsparseMatrix'
isSymmetric(object, checkDN = TRUE, ...)
## S4 method for signature 'TsparseMatrix'
isSymmetric(object, checkDN = TRUE, ...)
## S4 method for signature 'diagonalMatrix'
isSymmetric(object, checkDN = TRUE, ...)
## S4 method for signature 'indMatrix'
isSymmetric(object, checkDN = TRUE, ...)
## S4 method for signature 'dgeMatrix'
isSymmetric(object, checkDN = TRUE, tol = 100 * .Machine$double.eps, tol1 = 8 * tol, ...)
## S4 method for signature 'dgcMatrix'
isSymmetric(object, checkDN = TRUE, tol = 100 * .Machine$double.eps, ...)
```

Arguments

object	a "Matrix".
checkDN	a logical indicating whether symmetry of the Dimnames slot of object should be checked.
tol, tol1	numerical tolerances allowing <i>approximate</i> symmetry of numeric (rather than logical) matrices. See also isSymmetric.matrix .
...	further arguments passed to methods (typically methods for all.equal).

Details

The Dimnames **slot** of object, say dn, is considered to be symmetric if and only if

- dn[[1]] and dn[[2]] are identical *or* one is NULL; *and*
- ndn <- names(dn) is NULL *or* ndn[1] and ndn[2] are identical *or* one is the empty string "".

Hence list(a=nms, a=nms) is considered to be *symmetric*, and so too are list(a=nms, NULL) and list(NULL, a=nms).

Note that this definition is *looser* than that employed by [isSymmetric.matrix](#), which requires dn[1] and dn[2] to be identical, where dn is the dimnames **attribute** of a traditional matrix.

Value

A **logical**, either TRUE or FALSE (never NA).

See Also

[forceSymmetric](#); [symmpart](#) and [skewpart](#); virtual class "symmetricMatrix" and its subclasses.

Examples

```

isSymmetric(Diagonal(4)) # TRUE of course
M <- Matrix(c(1,2,2,1), 2,2)
isSymmetric(M) # TRUE (*and* of formal class "dsyMatrix")
isSymmetric(as(M, "generalMatrix")) # still symmetric, even if not "formally"
isSymmetric(triu(M)) # FALSE

## Look at implementations:
showMethods("isSymmetric", includeDefs = TRUE) # includes S3 generic from base

```

isTriangular-methods *Test whether a Matrix is Triangular or Diagonal*

Description

isTriangular and isDiagonal test whether their argument is a triangular or diagonal matrix, respectively. Unlike the analogous `isSymmetric`, these two functions are generically from **Matrix** rather than base. Hence **Matrix** defines methods for traditional matrices of implicit class `"matrix"` in addition to matrices inheriting from virtual class `"Matrix"`.

By our definition, triangular and diagonal matrices are *square*, i.e., they have the same number of rows and columns.

Usage

```

isTriangular(object, upper = NA, ...)

isDiagonal(object)

```

Arguments

object	an R object, typically a matrix.
upper	a logical , either TRUE or FALSE, in which case TRUE is returned only for upper or lower triangular object; or otherwise NA (the default), in which case TRUE is returned for any triangular object.
...	further arguments passed to methods (currently unused by Matrix).

Value

A [logical](#), either TRUE or FALSE (never NA).

If object is triangular and upper is NA, then isTriangular returns TRUE with an [attribute](#) kind, either "U" or "L", indicating that object is upper or lower triangular, respectively. Users should not rely on how kind is determined for diagonal matrices, which are both upper and lower triangular.

See Also

[isSymmetric](#); virtual classes `"triangularMatrix"` and `"diagonalMatrix"` and their subclasses.

Examples

```

isTriangular(Diagonal(4))
## is TRUE: a diagonal matrix is also (both upper and lower) triangular
(M <- Matrix(c(1,2,0,1), 2,2))
isTriangular(M) # TRUE (*and* of formal class "dtrMatrix")
isTriangular(as(M, "generalMatrix")) # still triangular, even if not "formally"
isTriangular(crossprod(M)) # FALSE

isDiagonal(matrix(c(2,0,0,1), 2,2)) # TRUE

## Look at implementations:
showMethods("isTriangular", includeDefs = TRUE)
showMethods("isDiagonal", includeDefs = TRUE)

```

KhatriRao

Khatri-Rao Matrix Product

Description

Computes Khatri-Rao products for any kind of matrices.

The Khatri-Rao product is a column-wise Kronecker product. Originally introduced by Khatri and Rao (1968), it has many different applications, see Liu and Trenkler (2008) for a survey. Notably, it is used in higher-dimensional tensor decompositions, see Bader and Kolda (2008).

Usage

```
KhatriRao(X, Y = X, FUN = "*", sparseY = TRUE, make.dimnames = FALSE)
```

Arguments

X, Y	matrices of with the same number of columns.
FUN	the (name of the) function to be used for the column-wise Kronecker products, see kronecker , defaulting to the usual multiplication.
sparseY	logical specifying if Y should be coerced and treated as sparseMatrix . Set this to FALSE, e.g., to distinguish structural zeros from zero entries.
make.dimnames	logical indicating if the result should inherit dimnames from X and Y in a simple way.

Value

a "[CsparseMatrix](#)", say R, the Khatri-Rao product of X ($n \times k$) and Y ($m \times k$), is of dimension $(n \cdot m) \times k$, where the j-th column, $R[, j]$ is the kronecker product [kronecker](#)($X[, j]$, $Y[, j]$).

Note

The current implementation is efficient for large sparse matrices.

Author(s)

Original by Michael Cysouw, Univ. Marburg; minor tweaks, bug fixes etc, by Martin Maechler.

References

Khatri, C. G., and Rao, C. Radhakrishna (1968) Solutions to Some Functional Equations and Their Applications to Characterization of Probability Distributions. *Sankhya: Indian J. Statistics, Series A* **30**, 167–180.

Bader, Brett W, and Tamara G Kolda (2008) Efficient MATLAB Computations with Sparse and Factored Tensors. *SIAM J. Scientific Computing* **30**, 205–231.

See Also

[kronecker](#).

Examples

```
## Example with very small matrices:
m <- matrix(1:12,3,4)
d <- diag(1:4)
KhatriRao(m,d)
KhatriRao(d,m)
dimnames(m) <- list(LETTERS[1:3], letters[1:4])
KhatriRao(m,d, make.dimnames=TRUE)
KhatriRao(d,m, make.dimnames=TRUE)
dimnames(d) <- list(NULL, paste0("D", 1:4))
KhatriRao(m,d, make.dimnames=TRUE)
KhatriRao(d,m, make.dimnames=TRUE)
dimnames(d) <- list(paste0("d", 10*1:4), paste0("D", 1:4))
(Kmd <- KhatriRao(m,d, make.dimnames=TRUE))
(Kdm <- KhatriRao(d,m, make.dimnames=TRUE))

nm <- as(m, "nsparseMatrix")
nd <- as(d, "nsparseMatrix")
KhatriRao(nm,nd, make.dimnames=TRUE)
KhatriRao(nd,nm, make.dimnames=TRUE)

stopifnot(dim(KhatriRao(m,d)) == c(nrow(m)*nrow(d), ncol(d)))
## border cases / checks:
zm <- nm; zm[] <- FALSE # all FALSE matrix
stopifnot(all(K1 <- KhatriRao(nd, zm) == 0), identical(dim(K1), c(12L, 4L)),
          all(K2 <- KhatriRao(zm, nd) == 0), identical(dim(K2), c(12L, 4L)))

d0 <- d; d0[] <- 0; m0 <- Matrix(d0[-1,])
stopifnot(all(K3 <- KhatriRao(d0, m) == 0), identical(dim(K3), dim(Kdm)),
          all(K4 <- KhatriRao(m, d0) == 0), identical(dim(K4), dim(Kmd)),
          all(KhatriRao(d0, d0) == 0), all(KhatriRao(m0, d0) == 0),
          all(KhatriRao(d0, m0) == 0), all(KhatriRao(m0, m0) == 0),
          identical(dimnames(KhatriRao(m, d0, make.dimnames=TRUE)), dimnames(Kmd)))

## a matrix with "structural" and non-structural zeros:
```

```

m01 <- new("dgCMatrix", i = c(0L, 2L, 0L, 1L), p = c(0L, 0L, 0L, 2L, 4L),
          Dim = 3:4, x = c(1, 0, 1, 0))
D4 <- Diagonal(4, x=1:4) # "as" d
DU <- Diagonal(4)# unit-diagonal: uplo="U"
(K5 <- KhatriRao( d, m01))
K5d <- KhatriRao( d, m01, sparseY=FALSE)
K5Dd <- KhatriRao(D4, m01, sparseY=FALSE)
K5Ud <- KhatriRao(DU, m01, sparseY=FALSE)
(K6 <- KhatriRao(diag(3), t(m01)))
K6D <- KhatriRao(Diagonal(3), t(m01))
K6d <- KhatriRao(diag(3), t(m01), sparseY=FALSE)
K6Dd <- KhatriRao(Diagonal(3), t(m01), sparseY=FALSE)
stopifnot(exprs = {
  all(K5 == K5d)
  identical(cbind(c(7L, 10L), c(3L, 4L)),
            which(K5 != 0, arr.ind = TRUE, useNames=FALSE))
  identical(K5d, K5Dd)
  identical(K6, K6D)
  all(K6 == K6d)
  identical(cbind(3:4, 1L),
            which(K6 != 0, arr.ind = TRUE, useNames=FALSE))
  identical(K6d, K6Dd)
})

```

 KNex

Koenker-Ng Example Sparse Model Matrix and Response Vector

Description

A model matrix `mm` and corresponding response vector `y` used in an example by Koenker and Ng. The matrix `mm` is a sparse matrix with 1850 rows and 712 columns but only 8758 non-zero entries. It is a "dgCMatrix" object. The vector `y` is just `numeric` of length 1850.

Usage

```
data(KNex)
```

References

Roger Koenker and Pin Ng (2003). SparseM: A sparse matrix package for R; *J. of Statistical Software*, **8** (6), doi:[10.18637/jss.v008.i06](https://doi.org/10.18637/jss.v008.i06)

Examples

```

data(KNex, package = "Matrix")
class(KNex$mm)
dim(KNex$mm)
image(KNex$mm)
str(KNex)

```

```

system.time( # a fraction of a second
  sparse.sol <- with(KNex, solve(crossprod(mm), crossprod(mm, y))))

head(round(sparse.sol,3))

## Compare with QR-based solution ("more accurate, but slightly slower"):
system.time(
  sp.sol2 <- with(KNex, qr.coef(qr(mm), y) ) )

all.equal(sparse.sol, sp.sol2, tolerance = 1e-13) # TRUE

```

kronecker-methods *Methods for Function 'kronecker()' in Package 'Matrix'*

Description

Computes Kronecker products for objects inheriting from "Matrix".

In order to preserve sparseness, we treat $0 * NA$ as 0 , not as NA as usually in R (and as used for the **base** function `kronecker`).

Methods

```

kronecker signature(X = "Matrix", Y = "ANY") .....
kronecker signature(X = "ANY", Y = "Matrix") .....
kronecker signature(X = "diagonalMatrix", Y = "ANY") .....
kronecker signature(X = "sparseMatrix", Y = "ANY") .....
kronecker signature(X = "TsparseMatrix", Y = "TsparseMatrix") .....
kronecker signature(X = "dgTMatrix", Y = "dgTMatrix") .....
kronecker signature(X = "dtTMatrix", Y = "dtTMatrix") .....
kronecker signature(X = "indMatrix", Y = "indMatrix") .....

```

Examples

```

(t1 <- spMatrix(5,4, x= c(3,2,-7,11), i= 1:4, j=4:1)) # 5 x 4
(t2 <- kronecker(Diagonal(3, 2:4), t1)) # 15 x 12

## should also work with special-cased logical matrices
l3 <- upper.tri(matrix(,3,3))
M <- Matrix(l3)
(N <- as(M, "nsparseMatrix")) # "ntCMatrix" (upper triangular)
N2 <- as(N, "generalMatrix") # (lost "t"riangularity)
MM <- kronecker(M,M)
NN <- kronecker(N,N) # "dtTMatrix" i.e. did keep
NN2 <- kronecker(N2,N2)
stopifnot(identical(NN,MM),
  is(NN2, "sparseMatrix"), all(NN2 == NN),
  is(NN, "triangularMatrix"))

```

 ldenseMatrix-class *Virtual Class "ldenseMatrix" of Dense Logical Matrices*

Description

ldenseMatrix is the virtual class of all dense logical (S4) matrices. It extends both [denseMatrix](#) and [lMatrix](#) directly.

Slots

x: logical vector containing the entries of the matrix.

Dim, Dimnames: see [Matrix](#).

Extends

Class "lMatrix", directly. Class "denseMatrix", directly. Class "Matrix", by class "lMatrix".
Class "Matrix", by class "denseMatrix".

Methods

as.vector signature(x = "ldenseMatrix", mode = "missing"): ...

which signature(x = "ndenseMatrix"), semantically equivalent to **base** function [which](#)(x, arr.ind);
for details, see the [lMatrix](#) class documentation.

See Also

Class [lgeMatrix](#) and the other subclasses.

Examples

```
showClass("ldenseMatrix")
```

```
as(diag(3) > 0, "ldenseMatrix")
```

 ldiMatrix-class *Class "ldiMatrix" of Diagonal Logical Matrices*

Description

The class "ldiMatrix" of logical diagonal matrices.

Objects from the Class

Objects can be created by calls of the form `new("ldiMatrix", ...)` but typically rather via [Diagonal](#).

Slots

x: "logical" vector.
diag: "character" string, either "U" or "N", see [ddiMatrix](#).
Dim,Dimnames: matrix dimension and [dimnames](#), see the [Matrix](#) class description.

Extends

Class "[diagonalMatrix](#)" and class "[lMatrix](#)", directly.
 Class "[sparseMatrix](#)", by class "[diagonalMatrix](#)".

See Also

Classes [ddiMatrix](#) and [diagonalMatrix](#); function [Diagonal](#).

Examples

```
(lM <- Diagonal(x = c(TRUE,FALSE,FALSE)))
str(lM)#> gory details (slots)

crossprod(lM) # numeric
(nM <- as(lM, "nMatrix"))
crossprod(nM) # pattern sparse
```

lgeMatrix-class

Class "lgeMatrix" of General Dense Logical Matrices

Description

This is the class of general dense [logical](#) matrices.

Slots

x: Object of class "logical". The logical values that constitute the matrix, stored in column-major order.
Dim,Dimnames: The dimension (a length-2 "integer") and corresponding names (or NULL), see the [Matrix](#) class.
factors: Object of class "list". A named list of factorizations that have been computed for the matrix.

Extends

Class "[ldenseMatrix](#)", directly. Class "[lMatrix](#)", by class "[ldenseMatrix](#)". Class "[denseMatrix](#)", by class "[ldenseMatrix](#)". Class "[Matrix](#)", by class "[ldenseMatrix](#)". Class "[Matrix](#)", by class "[ldenseMatrix](#)".

Methods

Currently, mainly `t()` and coercion methods (for `as(.)`); use, e.g., `showMethods(class="lgeMatrix")` for details.

See Also

Non-general logical dense matrix classes such as `ltrMatrix`, or `lsyMatrix`; *sparse* logical classes such as `lgMatrix`.

Examples

```
showClass("lgeMatrix")
str(new("lgeMatrix"))
set.seed(1)
(lM <- Matrix(matrix(rnorm(28), 4,7) > 0))# a simple random lgeMatrix
set.seed(11)
(lC <- Matrix(matrix(rnorm(28), 4,7) > 0))# a simple random lgCMatrix
as(lM, "CsparseMatrix")
```

lsparseMatrix-class *Sparse logical matrices*

Description

The `lsparseMatrix` class is a virtual class of logical sparse matrices, i.e., sparse matrices with entries TRUE, FALSE, or NA.

These can be stored in the “triplet” form (class `TsparseMatrix`, subclasses `lgTMatrix`, `lsTMatrix`, and `ltTMatrix`) or in compressed column-oriented form (class `CsparseMatrix`, subclasses `lgCMatrix`, `lsCMatrix`, and `ltCMatrix`) or—rarely—in compressed row-oriented form (class `RsparseMatrix`, subclasses `lgRMatrix`, `lsRMatrix`, and `ltRMatrix`). The second letter in the name of these non-virtual classes indicates general, symmetric, or triangular.

Details

Note that triplet stored (`TsparseMatrix`) matrices such as `lgTMatrix` may contain duplicated pairs of indices (i, j) as for the corresponding numeric class `dgTMatrix` where for such pairs, the corresponding x slot entries are added. For logical matrices, the x entries corresponding to duplicated index pairs (i, j) are “added” as well if the addition is defined as logical *or*, i.e., “TRUE + TRUE |→ TRUE” and “TRUE + FALSE |→ TRUE”. Note the use of `asUniqueT()` for getting an internally unique representation without duplicated (i, j) entries.

Objects from the Class

Objects can be created by calls of the form `new("lgCMatrix", ...)` and so on. More frequently objects are created by coercion of a numeric sparse matrix to the logical form, e.g. in an expression `x != 0`.

The logical form is also used in the symbolic analysis phase of an algorithm involving sparse matrices. Such algorithms often involve two phases: a symbolic phase wherein the positions of the non-zeros in the result are determined and a numeric phase wherein the actual results are calculated. During the symbolic phase only the positions of the non-zero elements in any operands are of interest, hence any numeric sparse matrices can be treated as logical sparse matrices.

Slots

- x**: Object of class "logical", i.e., either TRUE, NA, or FALSE.
- uplo**: Object of class "character". Must be either "U", for upper triangular, and "L", for lower triangular. Present in the triangular and symmetric classes but not in the general class.
- diag**: Object of class "character". Must be either "U", for unit triangular (diagonal is all ones), or "N" for non-unit. The implicit diagonal elements are not explicitly stored when diag is "U". Present in the triangular classes only.
- p**: Object of class "integer" of pointers, one for each column (row), to the initial (zero-based) index of elements in the column. Present in compressed column-oriented and compressed row-oriented forms only.
- i**: Object of class "integer" of length nnzero (number of non-zero elements). These are the row numbers for each TRUE element in the matrix. All other elements are FALSE. Present in triplet and compressed column-oriented forms only.
- j**: Object of class "integer" of length nnzero (number of non-zero elements). These are the column numbers for each TRUE element in the matrix. All other elements are FALSE. Present in triplet and compressed row-oriented forms only.
- Dim**: Object of class "integer" - the dimensions of the matrix.

Methods

- coerce** signature(from = "dgMatrix", to = "lgMatrix")
- t** signature(x = "lgMatrix"): returns the transpose of x
- which** signature(x = "lsparseMatrix"), semantically equivalent to **base** function **which**(x, arr.ind); for details, see the **lMatrix** class documentation.

See Also

the class [dgMatrix](#) and [dgTMatrix](#)

Examples

```
(m <- Matrix(c(0,0,2:0), 3,5, dimnames=list(LETTERS[1:3],NULL)))
(lm <- (m > 1)) # lgC
!lm          # no longer sparse
stopifnot(is(lm,"lsparseMatrix"),
           identical(!lm, m <= 1))

data(KNex, package = "Matrix")
str(mmG.1 <- (KNex $ mm) > 0.1)# "lgC..."
table(mmG.1@x)# however with many ``non-structural zeros''
## from logical to nz_pattern -- okay when there are no NA's :
```

```

nmG.1 <- as(mmG.1, "nMatrix") # <<< has "TRUE" also where mmG.1 had FALSE
## from logical to "double"
dmG.1 <- as(mmG.1, "dMatrix") # has '0' and back:
lmG.1 <- as(dmG.1, "lMatrix")
stopifnot(identical(nmG.1, as((KNex $ mm) != 0, "nMatrix")),
          validObject(lmG.1),
          identical(lmG.1, mmG.1))

class(xnx <- crossprod(nmG.1))# "nsC.."
class(xlx <- crossprod(mmG.1))# "dsC.." : numeric
is0 <- (xlx == 0)
mean(as.vector(is0))# 99.3% zeros: quite sparse, but
table(xlx@x == 0)# more than half of the entries are (non-structural!) 0
stopifnot(isSymmetric(xlx), isSymmetric(xnx),
          ## compare xnx and xlx : have the *same* non-structural 0s :
          sapply(slotNames(xnx),
                 function(n) identical(slot(xnx, n), slot(xlx, n))))

```

lsyMatrix-class

Symmetric Dense Logical Matrices

Description

The "lsyMatrix" class is the class of symmetric, dense logical matrices in non-packed storage and "lspMatrix" is the class of these in packed storage. In the packed form, only the upper triangle or the lower triangle is stored.

Objects from the Class

Objects can be created by calls of the form `new("lsyMatrix", ...)`.

Slots

uplo: Object of class "character". Must be either "U", for upper triangular, and "L", for lower triangular.

x: Object of class "logical". The logical values that constitute the matrix, stored in column-major order.

Dim,Dimnames: The dimension (a length-2 "integer") and corresponding names (or NULL), see the [Matrix](#) class.

factors: Object of class "list". A named list of factorizations that have been computed for the matrix.

Extends

Both extend classes "[ldenseMatrix](#)" and "[symmetricMatrix](#)", directly; further, class "[Matrix](#)" and others, *indirectly*. Use `showClass("lsyMatrix")`, e.g., for details.

Methods

Currently, mainly `t()` and coercion methods (for `as(.)`); use, e.g., `showMethods(class="ltyMatrix")` for details.

See Also

[lgeMatrix](#), [Matrix](#), [t](#)

Examples

```
(M2 <- Matrix(c(TRUE, NA, FALSE, FALSE), 2, 2)) # logical dense (ltr)
str(M2)
# can
(sM <- M2 | t(M2)) # "lge"
as(sM, "symmetricMatrix")
str(sM <- as(sM, "packedMatrix")) # packed symmetric
```

ltrMatrix-class

Triangular Dense Logical Matrices

Description

The "ltrMatrix" class is the class of triangular, dense, logical matrices in nonpacked storage. The "ltpMatrix" class is the same except in packed storage.

Slots

- x:** Object of class "logical". The logical values that constitute the matrix, stored in column-major order.
- uplo:** Object of class "character". Must be either "U", for upper triangular, and "L", for lower triangular.
- diag:** Object of class "character". Must be either "U", for unit triangular (diagonal is all ones), or "N"; see [triangularMatrix](#).
- Dim,Dimnames:** The dimension (a length-2 "integer") and corresponding names (or NULL), see the [Matrix](#) class.
- factors:** Object of class "list". A named list of factorizations that have been computed for the matrix.

Extends

Both extend classes "[ldenseMatrix](#)" and "[triangularMatrix](#)", directly; further, class "[Matrix](#)", "[lMatrix](#)" and others, *indirectly*. Use `showClass("ltrMatrix")`, e.g., for details.

Methods

Currently, mainly `t()` and coercion methods (for `as(.)`); use, e.g., `showMethods(class="ltrMatrix")` for details.

See Also

Classes [lgeMatrix](#), [Matrix](#); function [t](#)

Examples

```
showClass("ltrMatrix")

str(new("ltpMatrix"))
(lutr <- as(upper.tri(matrix(, 4, 4)), "ldenseMatrix"))
str(lutp <- pack(lutr)) # packed matrix: only 10 = 4*(4+1)/2 entries
!lutp # the logical negation (is *not* logical triangular !)
## but this one is:
stopifnot(all.equal(lutp, pack(!!lutp)))
```

lu-methods

Methods for LU Factorization

Description

Computes the pivoted LU factorization of an $m \times n$ real matrix A , which has the general form

$$P_1 A P_2 = LU$$

or (equivalently)

$$A = P_1' L U P_2'$$

where P_1 is an $m \times m$ permutation matrix, P_2 is an $n \times n$ permutation matrix, L is an $m \times \min(m, n)$ unit lower trapezoidal matrix, and U is a $\min(m, n) \times n$ upper trapezoidal matrix.

Methods for [denseMatrix](#) are built on LAPACK routine `dgetrf`, which does not permute columns, so that P_2 is an identity matrix.

Methods for [sparseMatrix](#) are built on CXSparse routine `cs_lu`, which requires $m = n$, so that L and U are triangular matrices.

Usage

```
lu(x, ...)
## S4 method for signature 'dgeMatrix'
lu(x, warnSing = TRUE, ...)
## S4 method for signature 'dgCMatrix'
lu(x, errSing = TRUE, order = NA_integer_,
   tol = 1, ...)
## S4 method for signature 'dsyMatrix'
lu(x, cache = TRUE, ...)
## S4 method for signature 'dsCMatrix'
lu(x, cache = TRUE, ...)
## S4 method for signature 'matrix'
lu(x, ...)
```

Arguments

x	a finite matrix or Matrix to be factorized, which must be square if sparse.
warnSing	a logical indicating if a warning should be signaled for singular x. Used only by methods for dense matrices.
errSing	a logical indicating if an error should be signaled for singular x. Used only by methods for sparse matrices.
order	an integer in 0:3 passed to CXSparse routine cs_sqr, indicating a strategy for choosing the column permutation P_2 . 0 means no column permutation. 1, 2, and 3 indicate a fill-reducing ordering of $A + A'$, $\tilde{A}'\tilde{A}$, and $A'A$, where \tilde{A} is A with “dense” rows removed. NA (the default) is equivalent to 2 if tol == 1 and 1 otherwise. Do not set to 0 unless you know that the column order of A is already sensible.
tol	a number. The original pivot element is used if its absolute value exceeds tol * a, where a is the maximum in absolute value of the other possible pivot elements. Set tol < 1 only if you know what you are doing.
cache	a logical indicating if the result should be cached in x@factors[["LU"]]. Note that caching is experimental and that only methods for classes extending generalMatrix or symmetricMatrix will have this argument.
...	further arguments passed to or from methods.

Details

What happens when x is determined to be near-singular differs by method. The method for class **dgeMatrix** completes the factorization, warning if warnSing = TRUE and in any case returning a valid **denseLU** object. Users of this method can detect singular x with a suitable warning handler; see **tryCatch**. In contrast, the method for class **dgCMatrix** abandons further computation, throwing an error if errSing = TRUE and otherwise returning NA. Users of this method can detect singular x with an error handler or by setting errSing = FALSE and testing for a formal result with `is(., "sparseLU")`.

Value

An object representing the factorization, inheriting from virtual class **LU**. The specific class is **denseLU** unless x inherits from virtual class **sparseMatrix**, in which case it is **sparseLU**.

References

The LAPACK source code, including documentation; see <https://netlib.org/lapack/double/dgetrf.f>.

Davis, T. A. (2006). *Direct methods for sparse linear systems*. Society for Industrial and Applied Mathematics. doi:10.1137/1.9780898718881

Golub, G. H., & Van Loan, C. F. (2013). *Matrix computations* (4th ed.). Johns Hopkins University Press. doi:10.56021/9781421407944

See Also

Classes [denseLU](#) and [sparseLU](#) and their methods.

Classes [dgeMatrix](#) and [dgCMatrix](#).

Generic functions [expand1](#) and [expand2](#), for constructing matrix factors from the result.

Generic functions [Cholesky](#), [BunchKaufman](#), [Schur](#), and [qr](#), for computing other factorizations.

Examples

```
showMethods("lu", inherited = FALSE)
set.seed(0)

## ---- Dense -----

(A1 <- Matrix(rnorm(9L), 3L, 3L))
(lu.A1 <- lu(A1))

(A2 <- round(10 * A1[, -3L]))
(lu.A2 <- lu(A2))

## A ~ P1' L U in floating point
str(e.lu.A2 <- expand2(lu.A2), max.level = 2L)
stopifnot(all.equal(A2, Reduce(`%*%`, e.lu.A2)))

## ---- Sparse -----

A3 <- as(readMM(system.file("external/pores_1.mtx", package = "Matrix")),
         "CsparseMatrix")
(lu.A3 <- lu(A3))

## A ~ P1' L U P2' in floating point
str(e.lu.A3 <- expand2(lu.A3), max.level = 2L)
stopifnot(all.equal(A3, Reduce(`%*%`, e.lu.A3)))
```

mat2triplet

Map Matrix to its Triplet Representation

Description

From an R object coercible to "[TsparseMatrix](#)", typically a (sparse) matrix, produce its triplet representation which may collapse to a "Duplet" in the case of binary aka pattern, such as "[nMatrix](#)" objects.

Usage

```
mat2triplet(x, uniqT = FALSE)
```

Arguments

- `x` any R object for which `as(x, "TsparseMatrix")` works; typically a `matrix` of one of the **Matrix** package matrices.
- `uniqT` `logical` indicating if the triplet representation should be 'unique' in the sense of `asUniqueT(byrow=FALSE)`.

Value

A `list`, typically with three components,

- `i` vector of row indices for all non-zero entries of `x`
- `j` vector of columns indices for all non-zero entries of `x`
- `x` vector of all non-zero entries of `x`; exists **only** when `as(x, "TsparseMatrix")` is **not** a `"nsparseMatrix"`.

Note that the `order` of the entries is determined by the coercion to `"TsparseMatrix"` and hence typically with increasing `j` (and increasing `i` within ties of `j`).

Note

The `mat2triplet()` utility was created to be a more efficient and more predictable substitute for `summary(<sparseMatrix>)`. Users have wrongly expected the latter to return a data frame with columns `i` and `j` which however is wrong for a `"diagonalMatrix"`.

See Also

The `summary()` method for `"sparseMatrix"`, `summary,sparseMatrix-method`.

`mat2triplet()` is conceptually the *inverse* function of `spMatrix` and (one case of) `sparseMatrix`.

Examples

```
mat2triplet # simple definition

i <- c(1,3:8); j <- c(2,9,6:10); x <- 7 * (1:7)
(Ax <- sparseMatrix(i, j, x = x)) ## 8 x 10 "dgCMatrix"
str(trA <- mat2triplet(Ax))
stopifnot(i == sort(trA$i), sort(j) == trA$j, x == sort(trA$x))

D <- Diagonal(x=4:2)
summary(D)
str(mat2triplet(D))
```

Description

The basic matrix product, `%%` is implemented for all our `Matrix` and also for `sparseVector` classes, fully analogously to R's base matrix and vector objects.

The functions `crossprod` and `tcrossprod` are matrix products or “cross products”, ideally implemented efficiently without computing `t(.)`'s unnecessarily. They also return `symmetricMatrix` classed matrices when easily detectable, e.g., in `crossprod(m)`, the one argument case.

`tcrossprod()` takes the cross-product of the transpose of a matrix. `tcrossprod(x)` is formally equivalent to, but faster than, the call `x %% t(x)`, and so is `tcrossprod(x, y)` instead of `x %% t(y)`.

Boolean matrix products are computed via either `%%` or `boolArith = TRUE`.

Usage

```
## S4 method for signature 'CsparseMatrix,diagonalMatrix'
x %% y

## S4 method for signature 'CsparseMatrix,diagonalMatrix'
crossprod(x, y = NULL, boolArith = NA, ...)
## ... and for many more signatures

## S4 method for signature 'TsparseMatrix,missing'
tcrossprod(x, y = NULL, boolArith = NA, ...)
## ... and for many more signatures
```

Arguments

<code>x</code>	a matrix-like object
<code>y</code>	a matrix-like object, or for <code>[t]crossprod()</code> NULL (by default); the latter case is formally equivalent to <code>y = x</code> .
<code>boolArith</code>	logical, i.e., NA, TRUE, or FALSE. If true the result is (coerced to) a pattern matrix, i.e., “ <code>nMatrix</code> ”, unless there are NA entries and the result will be a “ <code>lMatrix</code> ”. If false the result is (coerced to) numeric. When NA, currently the default, the result is a pattern matrix when <code>x</code> and <code>y</code> are “ <code>nsparseMatrix</code> ” and numeric otherwise.
<code>...</code>	potentially more arguments passed to and from methods.

Details

For some classes in the `Matrix` package, such as `dgCMatrix`, it is much faster to calculate the cross-product of the transpose directly instead of calculating the transpose first and then its cross-product. `boolArith = TRUE` for regular (“non cross”) matrix products, `%%` cannot be specified. Instead, we provide the `%%` operator for *boolean* matrix products.

Value

A *Matrix* object, in the one argument case of an appropriate *symmetric* matrix class, i.e., inheriting from `symmetricMatrix`.

Methods

`%*%` signature(x = "dgeMatrix", y = "dgeMatrix"): Matrix multiplication; ditto for several other signature combinations, see `showMethods("%*%", class = "dgeMatrix")`.

`%*%` signature(x = "dtrMatrix", y = "matrix") and other signatures (use `showMethods("%*%", class="dtrMatrix")`): matrix multiplication. Multiplication of (matching) triangular matrices now should remain triangular (in the sense of class `triangularMatrix`).

crossprod signature(x = "dgeMatrix", y = "dgeMatrix"): ditto for several other signatures, use `showMethods("crossprod", class = "dgeMatrix")`, matrix crossproduct, an efficient version of `t(x) %*% y`.

crossprod signature(x = "CsparseMatrix", y = "missing") returns `t(x) %*% x` as an `dsCMatrix` object.

crossprod signature(x = "TsparseMatrix", y = "missing") returns `t(x) %*% x` as an `dsCMatrix` object.

crossprod, tcrossprod signature(x = "dtrMatrix", y = "matrix") and other signatures, see `"%*%"` above.

Note

`boolArith = TRUE, FALSE` or `NA` has been newly introduced for **Matrix** 1.2.0 (March 2015). Its implementation has still not been tested extensively. Notably the behaviour for sparse matrices with `x` slots containing extra zeros had not been documented previously, see the `%&%` help page.

Currently, `boolArith = TRUE` is implemented via `CsparseMatrix` coercions which may be quite inefficient for dense matrices. Contributions for efficiency improvements are welcome.

See Also

`tcrossprod` in R's base, and `crossprod` and `%*%`. **Matrix** package `%&%` for boolean matrix product methods.

Examples

```
## A random sparse "incidence" matrix :
m <- matrix(0, 400, 500)
set.seed(12)
m[runif(314, 0, length(m))] <- 1
mm <- as(m, "CsparseMatrix")
object.size(m) / object.size(mm) # smaller by a factor of > 200

## tcrossprod() is very fast:
system.time(tCmm <- tcrossprod(mm))# 0 (PIII, 933 MHz)
system.time(cm <- crossprod(t(m))) # 0.16
system.time(cm. <- tcrossprod(m)) # 0.02
```

```
stopifnot(cm == as(tCmm, "matrix"))

## show sparse sub matrix
tCmm[1:16, 1:30]
```

Matrix *Construct a Classed Matrix*

Description

Construct a Matrix of a class that inherits from Matrix.

Usage

```
Matrix(data=NA, nrow=1, ncol=1, byrow=FALSE, dimnames=NULL,
        sparse = NULL, doDiag = TRUE, forceCheck = FALSE)
```

Arguments

data	an optional numeric data vector or matrix.
nrow	when data is not a matrix, the desired number of rows
ncol	when data is not a matrix, the desired number of columns
byrow	logical. If FALSE (the default) the matrix is filled by columns, otherwise the matrix is filled by rows.
dimnames	a <code>dimnames</code> attribute for the matrix: a list of two character components. They are set if not <code>NULL</code> (as per default).
sparse	logical or <code>NULL</code> , specifying if the result should be sparse or not. By default, it is made sparse when more than half of the entries are 0.
doDiag	logical indicating if a <code>diagonalMatrix</code> object should be returned when the resulting matrix is diagonal (<i>mathematically</i>). As class <code>diagonalMatrix</code> extends <code>sparseMatrix</code> , this is a natural default for all values of <code>sparse</code> . Otherwise, if <code>doDiag</code> is false, a dense or sparse (depending on <code>sparse</code>) <i>symmetric</i> matrix will be returned.
forceCheck	logical indicating if the checks for structure should even happen when data is already a "Matrix" object.

Details

If either of `nrow` or `ncol` is not given, an attempt is made to infer it from the length of `data` and the other parameter. Further, `Matrix()` makes efforts to keep `logical` matrices logical, i.e., inheriting from class `lMatrix`, and to determine specially structured matrices such as symmetric, triangular or diagonal ones. Note that a *symmetric* matrix also needs symmetric `dimnames`, e.g., by specifying `dimnames = list(NULL, NULL)`, see the examples.

Most of the time, the function works via a traditional (*full*) `matrix`. However, `Matrix(0, nrow, ncol)` directly constructs an "empty" `sparseMatrix`, as does `Matrix(FALSE, *)`.

Although it is sometime possible to mix unclassed matrices (created with `matrix`) with ones of class "Matrix", it is much safer to always use carefully constructed ones of class "Matrix".

Value

Returns matrix of a class that inherits from "Matrix". Only if data is not a `matrix` and does not already inherit from class `Matrix` are the arguments `nrow`, `ncol` and `byrow` made use of.

See Also

The classes `Matrix`, `symmetricMatrix`, `triangularMatrix`, and `diagonalMatrix`; further, `matrix`.

Special matrices can be constructed, e.g., via `sparseMatrix` (sparse), `bdiag` (block-diagonal), `bandSparse` (banded sparse), or `Diagonal`.

Examples

```
Matrix(0, 3, 2)           # 3 by 2 matrix of zeros -> sparse
Matrix(0, 3, 2, sparse=FALSE)# -> 'dense'

## 4 cases - 3 different results :
Matrix(0, 2, 2)           # diagonal !
Matrix(0, 2, 2, sparse=FALSE)# (ditto)
Matrix(0, 2, 2,          doDiag=FALSE)# -> sparse symm. "dsCMatrix"
Matrix(0, 2, 2, sparse=FALSE, doDiag=FALSE)# -> dense symm. "dsyMatrix"

Matrix(1:6, 3, 2)        # a 3 by 2 matrix (+ integer warning)
Matrix(1:6 + 1, nrow=3)

## logical ones:
Matrix(diag(4) > 0) # -> "ldiMatrix" with diag = "U"
Matrix(diag(4) > 0, sparse=TRUE) # (ditto)
Matrix(diag(4) >= 0) # -> "lsyMatrix" (of all 'TRUE')
## triangular
l3 <- upper.tri(matrix(,3,3))
(M <- Matrix(l3)) # -> "ltCMatrix"
Matrix(! l3)     # -> "ltrMatrix"
as(l3, "CsparseMatrix")# "lgCMatrix"

Matrix(1:9, nrow=3,
      dimnames = list(c("a", "b", "c"), c("A", "B", "C")))
(I3 <- Matrix(diag(3)))# identity, i.e., unit "diagonalMatrix"
str(I3) # note 'diag = "U"' and the empty 'x' slot

(A <- cbind(a=c(2,1), b=1:2))# symmetric *apart* from dimnames
Matrix(A)                   # hence 'dgeMatrix'
(As <- Matrix(A, dimnames = list(NULL,NULL)))# -> symmetric
forceSymmetric(A) # also symmetric, w/ symm. dimnames
stopifnot(is(As, "symmetricMatrix"),
          is(Matrix(0, 3,3), "sparseMatrix"),
          is(Matrix(FALSE, 1,1), "sparseMatrix"))
```

Matrix-class

Virtual Class "Matrix" of Matrices

Description

The Matrix class is a class contained by all actual classes in the **Matrix** package. It is a “virtual” class.

Slots

Dim an integer vector of length 2 giving the dimensions of the matrix.

Dimnames a list of length 2. Each element must be NULL or a character vector of length equal to the corresponding element of **Dim**.

Methods

determinant signature(x = "Matrix", logarithm = "missing"): and

determinant signature(x = "Matrix", logarithm = "logical"): compute the (log) determinant of x. The method chosen depends on the actual Matrix class of x. Note that **det** also works for all our matrices, calling the appropriate **determinant()** method. The **Matrix::det** is an exact copy of **base::det**, but in the correct namespace, and hence calling the S4-aware version of **determinant()**.

diff signature(x = "Matrix"): As **diff()** for traditional matrices, i.e., applying **diff()** to each column.

dim signature(x = "Matrix"): extract matrix dimensions **dim**.

dim<- signature(x = "Matrix", value = "ANY"): where value is integer of length 2. Allows to *reshape* Matrix objects, but only when **prod(value) == prod(dim(x))**.

dimnames signature(x = "Matrix"): extract **dimnames**.

dimnames<- signature(x = "Matrix", value = "list"): set the dimnames to a **list** of length 2, see **dimnames<-**.

length signature(x = "Matrix"): simply defined as **prod(dim(x))** (and hence of mode "double").

show signature(object = "Matrix"): **show** method for **printing**. For printing *sparse* matrices, see **printSpMatrix**.

zapsmall signature(x = "Matrix"): typically used for "**dMatrix**": **round()** matrix entries such that (relatively) very small entries become zero exactly.

image signature(object = "Matrix"): draws an **image** of the matrix entries, using **levelplot()** from package **lattice**.

head signature(object = "Matrix"): return only the "*head*", i.e., the first few rows.

tail signature(object = "Matrix"): return only the "*tail*", i.e., the last few rows of the respective matrix.

as.matrix, as.array signature(x = "Matrix"): the same as **as(x, "matrix")**; see also the note below.

as.vector signature($x = \text{"Matrix"}$, $\text{mode} = \text{"missing"}$): `as.vector(m)` should be identical to `as.vector(as(m, "matrix"))`, implemented more efficiently for some subclasses.

as(x, "vector"), **as(x, "numeric")** etc, similarly.

coerce signature($\text{from} = \text{"ANY"}$, $\text{to} = \text{"Matrix"}$): This relies on a correct `as.matrix()` method for `from`.

There are many more methods that (conceptually should) work for all "Matrix" objects, e.g., `colSums`, `rowMeans`. Even **base** functions may work automatically (if they first call `as.matrix()` on their principal argument), e.g., `apply`, `eigen`, `svd` or `kappa` all do work via coercion to a "traditional" (dense) `matrix`.

Note

Loading the Matrix namespace "overloads" `as.matrix` and `as.array` in the **base** namespace by the equivalent of `function(x) as(x, "matrix")`. Consequently, `as.matrix(m)` or `as.array(m)` will properly work when `m` inherits from the "Matrix" class — *also* for functions in package **base** and other packages. E.g., `apply` or `outer` can therefore be applied to "Matrix" matrices.

Author(s)

Douglas Bates <bates@stat.wisc.edu> and Martin Maechler

See Also

the classes `dgeMatrix`, `dgCMatrix`, and function `Matrix` for construction (and examples).

Methods, e.g., for `kronecker`.

Examples

```
slotNames("Matrix")

cl <- getClass("Matrix")
names(cl@subclasses) # more than 40 ..

showClass("Matrix")#> output with slots and all subclasses

(M <- Matrix(c(0,1,0,0), 6, 4))
dim(M)
diag(M)
cm <- M[1:4,] + 10*Diagonal(4)
diff(M)
## can reshape it even :
dim(M) <- c(2, 12)
M
stopifnot(identical(M, Matrix(c(0,1,0,0), 2,12)),
          all.equal(det(cm),
                    determinant(as(cm, "matrix"), log=FALSE)$modulus,
                    check.attributes=FALSE))
```

 Matrix-notyet

Virtual Classes Not Yet Really Implemented and Used

Description

iMatrix is the virtual class of all integer (S4) matrices. It extends the [Matrix](#) class directly.

zMatrix is the virtual class of all [complex](#) (S4) matrices. It extends the [Matrix](#) class directly.

Examples

```
showClass("iMatrix")
showClass("zMatrix")
```

 MatrixClass

The Matrix (Super-) Class of a Class

Description

Return the (maybe super-)class of class `cl` from package **Matrix**, returning `character(0)` if there is none.

Usage

```
MatrixClass(cl, cld = getClassDef(cl), ...Matrix = TRUE,
            dropVirtual = TRUE, ...)
```

Arguments

<code>cl</code>	string, class name
<code>cld</code>	its class definition
<code>...Matrix</code>	logical indicating if the result must be of pattern "[dlniz]..Matrix" where the first letter "[dlniz]" denotes the content kind.
<code>dropVirtual</code>	logical indicating if virtual classes are included or not.
<code>...</code>	further arguments are passed to <code>.selectSuperClasses()</code> .

Value

a [character](#) string

Author(s)

Martin Maechler, 24 Mar 2009

See Also

[Matrix](#), the mother of all **Matrix** classes.

Examples

```
mkA <- setClass("A", contains="dgCMatrix")
(A <- mkA())
stopifnot(identical(
  MatrixClass("A"),
  "dgCMatrix"))
```

MatrixFactorization-class

Virtual Class "MatrixFactorization" of Matrix Factorizations

Description

MatrixFactorization is the virtual class of factorizations of $m \times n$ matrices A , having the general form

$$P_1 A P_2 = A_1 \cdots A_p$$

or (equivalently)

$$A = P_1' A_1 \cdots A_p P_2'$$

where P_1 and P_2 are permutation matrices. Factorizations requiring symmetric A have the constraint $P_2 = P_1'$, and factorizations without row or column pivoting have the constraints $P_1 = I_m$ and $P_2 = I_n$, where I_m and I_n are the $m \times m$ and $n \times n$ identity matrices.

CholeskyFactorization, BunchKaufmanFactorization, SchurFactorization, LU, and QR are the virtual subclasses of MatrixFactorization containing all Cholesky, Bunch-Kaufman, Schur, LU, and QR factorizations, respectively.

Slots

Dim an integer vector of length 2 giving the dimensions of the factorized matrix.

Dimnames a list of length 2 preserving the dimnames of the factorized matrix. Each element must be NULL or a character vector of length equal to the corresponding element of Dim.

Methods

determinant signature(x = "MatrixFactorization", logarithm = "missing"): sets logarithm = TRUE and recalls the generic function.

dim signature(x = "MatrixFactorization"): returns x@Dim.

dimnames signature(x = "MatrixFactorization"): returns x@Dimnames.

dimnames<- signature(x = "MatrixFactorization", value = "NULL"): returns x with x@Dimnames set to list(NULL, NULL).

dimnames<- signature(x = "MatrixFactorization", value = "list"): returns x with x@Dimnames set to value.

length signature(x = "MatrixFactorization"): returns prod(x@Dim).

show signature(object = "MatrixFactorization"): prints the internal representation of the factorization using [str](#).

solve signature(a = "MatrixFactorization", b = .): see [solve-methods](#).

unname signature(obj = "MatrixFactorization"): returns obj with obj@Dimnames set to list(NULL, NULL).

See Also

Classes extending CholeskyFactorization, namely [Cholesky](#), [pCholesky](#), and [CHMfactor](#).

Classes extending BunchKaufmanFactorization, namely [BunchKaufman](#) and [pBunchKaufman](#).

Classes extending SchurFactorization, namely [Schur](#).

Classes extending LU, namely [denseLU](#) and [sparseLU](#).

Classes extending QR, namely [sparseQR](#).

Generic functions [Cholesky](#), [BunchKaufman](#), [Schur](#), [lu](#), and [qr](#) for *computing* factorizations.

Generic functions [expand1](#) and [expand2](#) for constructing matrix factors from MatrixFactorization objects.

Examples

```
showClass("MatrixFactorization")
```

ndenseMatrix-class *Virtual Class "ndenseMatrix" of Dense Logical Matrices*

Description

ndenseMatrix is the virtual class of all dense logical (S4) matrices. It extends both [denseMatrix](#) and [lMatrix](#) directly.

Slots

x: logical vector containing the entries of the matrix.

Dim, Dimnames: see [Matrix](#).

Extends

Class "nMatrix", directly. Class "denseMatrix", directly. Class "Matrix", by class "nMatrix".
 Class "Matrix", by class "denseMatrix".

Methods

```

%% signature(x = "nsparseMatrix", y = "ndenseMatrix"): ...
%% signature(x = "ndenseMatrix", y = "nsparseMatrix"): ...
crossprod signature(x = "nsparseMatrix", y = "ndenseMatrix"): ...
crossprod signature(x = "ndenseMatrix", y = "nsparseMatrix"): ...
as.vector signature(x = "ndenseMatrix", mode = "missing"): ...
diag signature(x = "ndenseMatrix"): extracts the diagonal as for all matrices, see the generic diag\(\).
which signature(x = "ndenseMatrix"), semantically equivalent to base function which\(x, arr.ind\); for details, see the lMatrix class documentation.

```

See Also

Class [ngeMatrix](#) and the other subclasses.

Examples

```

showClass("ndenseMatrix")

as(diag(3) > 0, "ndenseMatrix")# -> "nge"

```

nearPD

Nearest Positive Definite Matrix

Description

Compute the nearest positive definite matrix to an approximate one, typically a correlation or variance-covariance matrix.

Usage

```

nearPD(x, corr = FALSE, keepDiag = FALSE, base.matrix = FALSE,
       do2eigen = TRUE, doSym = FALSE,
       doDykstra = TRUE, only.values = FALSE,
       ensureSymmetry = !isSymmetric(x),
       eig.tol = 1e-06, conv.tol = 1e-07, posd.tol = 1e-08,
       maxit = 100, conv.norm.type = "I", trace = FALSE)

```

Arguments

x	numeric $n \times n$ approximately positive definite matrix, typically an approximation to a correlation or covariance matrix. If x is not symmetric (and <code>ensureSymmetry</code> is not false), symmpart(x) is used.
corr	logical indicating if the matrix should be a <i>correlation</i> matrix.

keepDiag	logical, generalizing corr: if TRUE, the resulting matrix should have the same diagonal (<code>diag(x)</code>) as the input matrix.
base.matrix	logical indicating if the resulting mat component should be a base matrix or (by default) a Matrix of class <code>dpoMatrix</code> .
do2eigen	logical indicating if a <code>posdefify()</code> eigen step should be applied to the result of the Higham algorithm.
doSym	logical indicating if $X \leftarrow (X + t(X))/2$ should be done, after $X \leftarrow t\text{crossprod}(Qd, Q)$; some doubt if this is necessary.
doDykstra	logical indicating if Dykstra's correction should be used; true by default. If false, the algorithm is basically the direct fixpoint iteration $Y_k = P_U(P_S(Y_{k-1}))$.
only.values	logical; if TRUE, the result is just the vector of eigenvalues of the approximating matrix.
ensureSymmetry	logical; by default, <code>symmpart(x)</code> is used whenever <code>isSymmetric(x)</code> is not true. The user can explicitly set this to TRUE or FALSE, saving the symmetry test. <i>Beware</i> however that setting it FALSE for an asymmetric input x, is typically nonsense!
eig.tol	defines relative positiveness of eigenvalues compared to largest one, λ_1 . Eigenvalues λ_k are treated as if zero when $\lambda_k/\lambda_1 \leq \text{eig.tol}$.
conv.tol	convergence tolerance for Higham algorithm.
posd.tol	tolerance for enforcing positive definiteness (in the final <code>posdefify</code> step when <code>do2eigen</code> is TRUE).
maxit	maximum number of iterations allowed.
conv.norm.type	convergence norm type (<code>norm(*, type)</code>) used for Higham algorithm. The default is "I" (infinity), for reasons of speed (and back compatibility); using "F" is more in line with Higham's proposal.
trace	logical or integer specifying if convergence monitoring should be traced.

Details

This implements the algorithm of Higham (2002), and then (if `do2eigen` is true) forces positive definiteness using code from `posdefify`. The algorithm of Knol and ten Berge (1989) (not implemented here) is more general in that it allows constraints to (1) fix some rows (and columns) of the matrix and (2) force the smallest eigenvalue to have a certain value.

Note that setting `corr = TRUE` just sets `diag(.) <- 1` within the algorithm.

Higham (2002) uses Dykstra's correction, but the version by Jens Oehlschlägel did not use it (accidentally), and still gave reasonable results; this simplification, now only used if `doDykstra = FALSE`, was active in `nearPD()` up to Matrix version 0.999375-40.

Value

If `only.values = TRUE`, a numeric vector of eigenvalues of the approximating matrix; Otherwise, as by default, an S3 object of class "nearPD", basically a list with components

mat	a matrix of class <code>dpoMatrix</code> , the computed positive-definite matrix.
eigenvalues	numeric vector of eigenvalues of mat.

corr	logical, just the argument corr.
normF	the Frobenius norm (<code>norm(x-X, "F")</code>) of the difference between the original and the resulting matrix.
iterations	number of iterations needed.
converged	logical indicating if iterations converged.

Author(s)

Jens Oehlschlägel donated a first version. Subsequent changes by the Matrix package authors.

References

- Cheng, Sheung Hun and Higham, Nick (1998) A Modified Cholesky Algorithm Based on a Symmetric Indefinite Factorization; *SIAM J. Matrix Anal. Appl.*, **19**, 1097–1110.
- Knol DL, ten Berge JMF (1989) Least-squares approximation of an improper correlation matrix by a proper one. *Psychometrika* **54**, 53–61.
- Higham, Nick (2002) Computing the nearest correlation matrix - a problem from finance; *IMA Journal of Numerical Analysis* **22**, 329–343.

See Also

A first version of this (with non-optional `corr=TRUE`) has been available as `nearcor()`; and more simple versions with a similar purpose `posdefify()`, both from package `sfsmisc`.

Examples

```
## Higham(2002), p.334f - simple example
A <- matrix(1, 3,3); A[1,3] <- A[3,1] <- 0
n.A <- nearPD(A, corr=TRUE, do2eigen=FALSE)
n.A[c("mat", "normF")]
n.A.m <- nearPD(A, corr=TRUE, do2eigen=FALSE, base.matrix=TRUE)$mat
stopifnot(exprs = { #=-----
  all.equal(n.A$mat[1,2], 0.760689917)
  all.equal(n.A$normF, 0.52779033, tolerance=1e-9)
  all.equal(n.A.m, unname(as.matrix(n.A$mat)), tolerance = 1e-15)# seen rel.d.= 1.46e-16
})
set.seed(27)
m <- matrix(round(rnorm(25),2), 5, 5)
m <- m + t(m)
diag(m) <- pmax(0, diag(m)) + 1
(m <- round(cov2cor(m), 2))

str(near.m <- nearPD(m, trace = TRUE))
round(near.m$mat, 2)
norm(m - near.m$mat) # 1.102 / 1.08

if(requireNamespace("sfsmisc")) {
  m2 <- sfsmisc::posdefify(m) # a simpler approach
  norm(m - m2) # 1.185, i.e., slightly "less near"
}
```

```

round(nearPD(m, only.values=TRUE), 9)

## A longer example, extended from Jens' original,
## showing the effects of some of the options:

pr <- Matrix(c(1,      0.477, 0.644, 0.478, 0.651, 0.826,
              0.477, 1,      0.516, 0.233, 0.682, 0.75,
              0.644, 0.516, 1,      0.599, 0.581, 0.742,
              0.478, 0.233, 0.599, 1,      0.741, 0.8,
              0.651, 0.682, 0.581, 0.741, 1,      0.798,
              0.826, 0.75,  0.742, 0.8,   0.798, 1),
            nrow = 6, ncol = 6)

nc. <- nearPD(pr, conv.tol = 1e-7) # default
nc.$iterations # 2
nc.1 <- nearPD(pr, conv.tol = 1e-7, corr = TRUE)
nc.1$iterations # 11 / 12 (!)
ncr <- nearPD(pr, conv.tol = 1e-15)
str(ncr)# still 2 iterations
ncr.1 <- nearPD(pr, conv.tol = 1e-15, corr = TRUE)
ncr.1 $ iterations # 27 / 30 !

ncF <- nearPD(pr, conv.tol = 1e-15, conv.norm = "F")
stopifnot(all.equal(ncr, ncF))# norm type does not matter at all in this example

## But indeed, the 'corr = TRUE' constraint did ensure a better solution;
## cov2cor() does not just fix it up equivalently :
norm(pr - cov2cor(ncr$mat)) # = 0.09994
norm(pr -      ncr.1$mat) # = 0.08746 / 0.08805

### 3) a real data example from a 'systemfit' model (3 eq.):
(load(system.file("external", "symW.rda", package="Matrix"))) # "symW"
dim(symW) # 24 x 24
class(symW)# "dsCMatrix": sparse symmetric
if(dev.interactive()) image(symW)
EV <- eigen(symW, only=TRUE)$values
summary(EV) ## looking more closely {EV sorted decreasingly}:
tail(EV)# all 6 are negative
EV2 <- eigen(sWpos <- nearPD(symW)$mat, only=TRUE)$values
stopifnot(EV2 > 0)
if(requireNamespace("sfsmisc")) {
  plot(pmax(1e-3,EV), EV2, type="o", log="xy", xaxt="n", yaxt="n")
  for(side in 1:2) sfsmisc::eaxis(side)
} else
  plot(pmax(1e-3,EV), EV2, type="o", log="xy")
abline(0, 1, col="red3", lty=2)

```

Description

This is the class of general dense nonzero-pattern matrices, see [nMatrix](#).

Slots

x: Object of class "logical". The logical values that constitute the matrix, stored in column-major order.

Dim,Dimnames: The dimension (a length-2 "integer") and corresponding names (or NULL), see the [Matrix](#) class.

factors: Object of class "list". A named list of factorizations that have been computed for the matrix.

Extends

Class "ndenseMatrix", directly. Class "lMatrix", by class "ndenseMatrix". Class "denseMatrix", by class "ndenseMatrix". Class "Matrix", by class "ndenseMatrix". Class "Matrix", by class "ndenseMatrix".

Methods

Currently, mainly [t\(\)](#) and coercion methods (for [as\(.\)](#)); use, e.g., [showMethods\(class="ngeMatrix"\)](#) for details.

See Also

Non-general logical dense matrix classes such as [ntrMatrix](#), or [nsyMatrix](#); *sparse* logical classes such as [ngCMatrix](#).

Examples

```
showClass("ngeMatrix")
## "lgeMatrix" is really more relevant
```

nMatrix-class

Class "nMatrix" of Non-zero Pattern Matrices

Description

The nMatrix class is the virtual "mother" class of all *non-zero pattern* (or simply *pattern*) matrices in the **Matrix** package.

Slots

Common to *all* matrix object in the package:

Dim: Object of class "integer" - the dimensions of the matrix - must be an integer vector with exactly two non-negative values.

Dimnames: list of length two; each component containing NULL or a [character](#) vector length equal the corresponding Dim element.

Methods

coerce signature(from = "matrix", to = "nMatrix"): Note that these coercions (must) coerce NAs to non-zero, hence conceptually TRUE. This is particularly important when `sparseMatrix` objects are coerced to "nMatrix" and hence to `nsparseMatrix`.

— — —
Additional methods contain group methods, such as

Ops signature(e1 = "nMatrix", e2 = "..."),...

Arith signature(e1 = "nMatrix", e2 = "..."),...

Compare signature(e1 = "nMatrix", e2 = "..."),...

Logic signature(e1 = "nMatrix", e2 = "..."),...

Summary signature(x = "nMatrix", "..."),...

See Also

The classes `lMatrix`, `nsparseMatrix`, and the mother class, `Matrix`.

Examples

```
getClass("nMatrix")

L3 <- Matrix(upper.tri(diag(3)))
L3 # an "ltCMatrix"
as(L3, "nMatrix") # -> ntC*

## similar, not using Matrix()
as(upper.tri(diag(3)), "nMatrix")# currently "ngTMatrix"
```

nnzero-methods

The Number of Non-Zero Values of a Matrix

Description

Returns the number of non-zero values of a numeric-like R object, and in particular an object x inheriting from class `Matrix`.

Usage

```
nnzero(x, na.counted = NA)
```

Arguments

- x** an R object, typically inheriting from class `Matrix` or `numeric`.
- na.counted** a `logical` describing how `NA`s should be counted. There are three possible settings for `na.counted`:
- TRUE** `NA`s are counted as non-zero (since “they are not zero”).
 - NA** (default) the result will be `NA` if there are `NA`’s in `x` (since “`NA`’s are not known, i.e., *may be zero*”).
 - FALSE** `NA`s are *omitted* from `x` before the non-zero entries are counted.
- For sparse matrices, you may often want to use `na.counted = TRUE`.

Value

the number of non zero entries in `x` (typically `integer`).

Note that for a *symmetric* sparse matrix `S` (i.e., inheriting from class `symmetricMatrix`), `nnzero(S)` is typically *twice* the `length(S@x)`.

Methods

- `signature(x = "ANY")` the default method for non-`Matrix` class objects, simply counts the number of 0s in `x`, counting `NA`’s depending on the `na.counted` argument, see above.
- `signature(x = "denseMatrix")` conceptually the same as for traditional `matrix` objects, care has to be taken for “`symmetricMatrix`” objects.
- `signature(x = "diagonalMatrix")`, **and** `signature(x = "indMatrix")` fast simple methods for these special “`sparseMatrix`” classes.
- `signature(x = "sparseMatrix")` typically, the most interesting method, also carefully taking “`symmetricMatrix`” objects into account.

See Also

The `Matrix` class also has a `length` method; typically, `length(M)` is much larger than `nnzero(M)` for a sparse matrix `M`, and the latter is a better indication of the *size* of `M`.
[drop0](#), [zapsmall](#).

Examples

```
m <- Matrix(0+1:28, nrow = 4)
m[-3,c(2,4:5,7)] <- m[ 3, 1:4] <- m[1:3, 6] <- 0
(mT <- as(m, "TsparseMatrix"))
nnzero(mT)
(S <- crossprod(mT))
nnzero(S)
str(S) # slots are smaller than nnzero()
stopifnot(nnzero(S) == sum(as.matrix(S) != 0))# failed earlier

data(KNex, package = "Matrix")
M <- KNex$mm
class(M)
```

```

dim(M)
length(M); stopifnot(length(M) == prod(dim(M)))
nnzero(M) # more relevant than length
## the above are also visible from
str(M)

```

norm-methods

*Matrix Norms***Description**

Computes a matrix norm of x , using Lapack for dense matrices. The norm can be the one ("0", or "1") norm, the infinity ("I") norm, the Frobenius ("F") norm, the maximum modulus ("M") among elements of a matrix, or the spectral norm or 2-norm ("2"), as determined by the value of `type`.

Usage

```
norm(x, type, ...)
```

Arguments

<code>x</code>	a real or complex matrix.
<code>type</code>	A character indicating the type of norm desired. "0", "o" or "1" specifies the one norm, (maximum absolute column sum); "I" or "i" specifies the infinity norm (maximum absolute row sum); "F" or "f" specifies the Frobenius norm (the Euclidean norm of x treated as if it were a vector); "M" or "m" specifies the maximum modulus of all the elements in x ; and "2" specifies the "spectral norm" aka "2-norm", which is the largest singular value (svd) of x . The default is "0". Only the first character of <code>type[1]</code> is used.
<code>...</code>	further arguments passed to or from other methods.

Details

For dense matrices, the methods eventually call the Lapack functions `dlange`, `dlansy`, `dlantr`, `zlange`, `zlansy`, and `zlantr`.

Value

A numeric value of class "norm", representing the quantity chosen according to `type`.

References

Anderson, E., et al. (1994). *LAPACK User's Guide*, 2nd edition, SIAM, Philadelphia.

See Also

`onenormest()`, an *approximate* randomized estimate of the 1-norm condition number, efficient for large sparse matrices.

The `norm()` function from R's **base** package.

Examples

```
x <- Hilbert(9)
norm(x)# = "0" = "1"
stopifnot(identical(norm(x), norm(x, "1")))
norm(x, "I")# the same, because 'x' is symmetric

allnorms <- function(x) {
  ## norm(NA, "2") did not work until R 4.0.0
  do2 <- getRversion() >= "4.0.0" || !anyNA(x)
  vapply(c("1", "I", "F", "M", if(do2) "2"), norm, 0, x = x)
}
allnorms(x)
allnorms(Hilbert(10))

i <- c(1,3:8); j <- c(2,9,6:10); x <- 7 * (1:7)
A <- sparseMatrix(i, j, x = x) ## 8 x 10 "dgCMatrix"
(sA <- sparseMatrix(i, j, x = x, symmetric = TRUE)) ## 10 x 10 "dsCMatrix"
(tA <- sparseMatrix(i, j, x = x, triangular= TRUE)) ## 10 x 10 "dtCMatrix"
(allnorms(A) -> nA)
allnorms(sA)
allnorms(tA)
stopifnot(all.equal(nA, allnorms(as(A, "matrix"))),
  all.equal(nA, allnorms(tA))) # because tA == rbind(A, 0, 0)
A. <- A; A.[1,3] <- NA
stopifnot(is.na(allnorms(A.))) # gave error
```

nsparseMatrix-class *Sparse "pattern" Matrices*

Description

The `nsparseMatrix` class is a virtual class of sparse “*pattern*” matrices, i.e., binary matrices conceptually with TRUE/FALSE entries. Only the positions of the elements that are TRUE are stored.

These can be stored in the “triplet” form (`TsparseMatrix`, subclasses `ngTMatrix`, `nsTMatrix`, and `ntTMatrix` which really contain pairs, not triplets) or in compressed column-oriented form (class `CsparseMatrix`, subclasses `ngCMatrix`, `nsCMatrix`, and `ntCMatrix`) or—*rarely*—in compressed row-oriented form (class `RsparseMatrix`, subclasses `ngRMatrix`, `nsRMatrix`, and `ntRMatrix`). The second letter in the name of these non-virtual classes indicates general, symmetric, or triangular.

Objects from the Class

Objects can be created by calls of the form `new("ngCMatrix", ...)` and so on. More frequently objects are created by coercion of a numeric sparse matrix to the pattern form for use in the symbolic analysis phase of an algorithm involving sparse matrices. Such algorithms often involve two phases: a symbolic phase wherein the positions of the non-zeros in the result are determined and a numeric phase wherein the actual results are calculated. During the symbolic phase only the positions of the non-zero elements in any operands are of interest, hence numeric sparse matrices can be treated as sparse pattern matrices.

Slots

uplo: Object of class "character". Must be either "U", for upper triangular, and "L", for lower triangular. Present in the triangular and symmetric classes but not in the general class.

diag: Object of class "character". Must be either "U", for unit triangular (diagonal is all ones), or "N" for non-unit. The implicit diagonal elements are not explicitly stored when diag is "U". Present in the triangular classes only.

p: Object of class "integer" of pointers, one for each column (row), to the initial (zero-based) index of elements in the column. Present in compressed column-oriented and compressed row-oriented forms only.

i: Object of class "integer" of length nnzero (number of non-zero elements). These are the row numbers for each TRUE element in the matrix. All other elements are FALSE. Present in triplet and compressed column-oriented forms only.

j: Object of class "integer" of length nnzero (number of non-zero elements). These are the column numbers for each TRUE element in the matrix. All other elements are FALSE. Present in triplet and compressed row-oriented forms only.

Dim: Object of class "integer" - the dimensions of the matrix.

Methods

coerce signature(`from = "dgCMatrix"`, `to = "ngCMatrix"`), and many similar ones; typically you should coerce to "nsparseMatrix" (or "nMatrix"). Note that coercion to a sparse pattern matrix records all the potential non-zero entries, i.e., explicit ("non-structural") zeroes are coerced to TRUE, not FALSE, see the example.

t signature(`x = "ngCMatrix"`): returns the transpose of `x`

which signature(`x = "lsparseMatrix"`), semantically equivalent to **base** function `which(x, arr.ind)`; for details, see the `lMatrix` class documentation.

See Also

the class `dgCMatrix`

Examples

```
(m <- Matrix(c(0,0,2:0), 3,5, dimnames=list(LETTERS[1:3],NULL)))
## ``extract the nonzero-pattern of (m) into an nMatrix'':
nm <- as(m, "nsparseMatrix") ## -> will be a "ngCMatrix"
str(nm) # no 'x' slot
```

```

nnm <- !nm # no longer sparse
## consistency check:
stopifnot(xor(as( nm, "matrix"),
              as(nnm, "matrix")))

## low-level way of adding "non-structural zeros" :
nnm <- as(nnm, "lsparseMatrix") # "lgMatrix"
nnm@x[2:4] <- c(FALSE, NA, NA)
nnm
as(nnm, "nMatrix") # NAs *and* non-structural 0 |---> 'TRUE'

data(KNex, package = "Matrix")
nmm <- as(KNex $ mm, "nMatrix")
str(xlx <- crossprod(nmm))# "nsMatrix"
stopifnot(isSymmetric(xlx))
image(xlx, main=paste("crossprod(nmm) : Sparse", class(xlx)))

```

nsyMatrix-class

Symmetric Dense Nonzero-Pattern Matrices

Description

The "nsyMatrix" class is the class of symmetric, dense nonzero-pattern matrices in non-packed storage and "nspMatrix" is the class of these in packed storage. Only the upper triangle or the lower triangle is stored.

Objects from the Class

Objects can be created by calls of the form `new("nsyMatrix", ...)`.

Slots

uplo: Object of class "character". Must be either "U", for upper triangular, and "L", for lower triangular.

x: Object of class "logical". The logical values that constitute the matrix, stored in column-major order.

Dim,Dimnames: The dimension (a length-2 "integer") and corresponding names (or NULL), see the [Matrix](#) class.

factors: Object of class "list". A named list of factorizations that have been computed for the matrix.

Extends

"nsyMatrix" extends class "ngeMatrix", directly, whereas

"nspMatrix" extends class "ndenseMatrix", directly.

Both extend class "symmetricMatrix", directly, and class "Matrix" and others, *indirectly*, use `showClass("nsyMatrix")`, e.g., for details.

Methods

Currently, mainly `t()` and coercion methods (for `as(.)`); use, e.g., `showMethods(class="nsyMatrix")` for details.

See Also

[ngeMatrix](#), [Matrix](#), [t](#)

Examples

```
(s0 <- new("nsyMatrix"))

(M2 <- Matrix(c(TRUE, NA, FALSE, FALSE), 2, 2)) # logical dense (ltr)
(sM <- M2 & t(M2))                             # -> "lge"
class(sM <- as(sM, "nMatrix"))                 # -> "nge"
      (sM <- as(sM, "symmetricMatrix"))         # -> "nsy"
str(sM <- as(sM, "packedMatrix")) # -> "nsp", i.e., packed symmetric
```

ntrMatrix-class

Triangular Dense Logical Matrices

Description

The "ntrMatrix" class is the class of triangular, dense, logical matrices in nonpacked storage. The "ntpMatrix" class is the same except in packed storage.

Slots

x: Object of class "logical". The logical values that constitute the matrix, stored in column-major order.

uplo: Object of class "character". Must be either "U", for upper triangular, and "L", for lower triangular.

diag: Object of class "character". Must be either "U", for unit triangular (diagonal is all ones), or "N"; see [triangularMatrix](#).

Dim,Dimnames: The dimension (a length-2 "integer") and corresponding names (or NULL), see the [Matrix](#) class.

factors: Object of class "list". A named list of factorizations that have been computed for the matrix.

Extends

"ntrMatrix" extends class "ngeMatrix", directly, whereas
 "ntpMatrix" extends class "ndenseMatrix", directly.

Both extend Class "triangularMatrix", directly, and class "denseMatrix", "lMatrix" and others, indirectly, use `showClass("nsyMatrix")`, e.g., for details.

Methods

Currently, mainly `t()` and coercion methods (for `as(.)`); use, e.g., `showMethods(class="ntrMatrix")` for details.

See Also

Classes `ngeMatrix`, `Matrix`; function `t`

Examples

```
showClass("ntrMatrix")

str(new("ntpMatrix"))
(nutr <- as(upper.tri(matrix(, 4, 4)), "ndenseMatrix"))
str(nutp <- pack(nutr)) # packed matrix: only 10 = 4*(4+1)/2 entries
!nutp # the logical negation (is *not* logical triangular !)
## but this one is:
stopifnot(all.equal(nutp, pack(!!nutp)))
```

 pack-methods

Representation of Packed and Unpacked Dense Matrices

Description

`pack()` coerces dense symmetric and dense triangular matrices from unpacked format (storing the full matrix) to packed format (storing only one of the upper and lower triangles). `unpack()` performs the reverse coercion. The two formats are formalized by the virtual classes "`packedMatrix`" and "`unpackedMatrix`".

Usage

```
pack(x, ...)
## S4 method for signature 'dgeMatrix'
pack(x, symmetric = NA, upperTri = NA, ...)
## S4 method for signature 'lgeMatrix'
pack(x, symmetric = NA, upperTri = NA, ...)
## S4 method for signature 'ngeMatrix'
pack(x, symmetric = NA, upperTri = NA, ...)
## S4 method for signature 'matrix'
pack(x, symmetric = NA, upperTri = NA, ...)

unpack(x, ...)
```

Arguments

x	A dense symmetric or dense triangular matrix. For pack(): typically an "unpackedMatrix" or a standard "matrix", though "packedMatrix" are allowed and returned unchanged. For unpack(): typically a "packedMatrix", though "unpackedMatrix" are allowed and returned unchanged.
symmetric	logical (including NA) optionally indicating whether x is symmetric (or triangular).
upperTri	(for triangular x only) logical (including NA) indicating whether x is upper (or lower) triangular.
...	further arguments passed to or from other methods.

Details

pack(x) checks matrices x *not* inheriting from one of the virtual classes "symmetricMatrix" "triangularMatrix" for symmetry (via `isSymmetric()`) then for upper and lower triangularity (via `isTriangular()`) in order to identify a suitable coercion. Setting one or both of symmetric and upperTri to TRUE or FALSE rather than NA allows skipping of irrelevant tests for large matrices known to be symmetric or (upper or lower) triangular.

Users should *not* assume that pack() and unpack() are inverse operations. Specifically, `y <- unpack(pack(x))` may not reproduce an "unpackedMatrix" x in the sense of `identical()`. See the examples.

Value

For pack(): a "packedMatrix" giving the condensed representation of x.

For unpack(): an "unpackedMatrix" giving the full storage representation of x.

Examples

```
showMethods("pack")
(s <- crossprod(matrix(sample(15), 5,3))) # traditional symmetric matrix
(sp <- pack(s))
mt <- as.matrix(tt <- tril(s))
(pt <- pack(mt))
stopifnot(identical(pt, pack(tt)),
  dim(s) == dim(sp), all(s == sp),
  dim(mt) == dim(pt), all(mt == pt), all(mt == tt))

showMethods("unpack")
(cp4 <- chol(Hilbert(4))) # is triangular
tp4 <- pack(cp4) # [t]riangular [p]acked
str(tp4)
(unpack(tp4))
stopifnot(identical(tp4, pack(unpack(tp4))))

z1 <- new("dsyMatrix", Dim = c(2L, 2L), x = as.double(1:4), uplo = "U")
z2 <- unpack(pack(z1))
```

```
stopifnot(!identical(z1, z2), # _not_ identical
          all(z1 == z2)) # but mathematically equal
cbind(z1@x, z2@x) # (unused!) lower triangle is "lost" in translation
```

packedMatrix-class *Virtual Class "packedMatrix" of Packed Dense Matrices*

Description

Class "packedMatrix" is the *virtual* class of dense symmetric or triangular matrices in "packed" format, storing only the $\text{choose}(n+1, 2) = n*(n+1)/2$ elements of the upper or lower triangle of an n -by- n matrix. It is used to define common methods for efficient subsetting, transposing, etc. of its *proper* subclasses: currently "[dln]spMatrix" (packed symmetric), "[dln]tpMatrix" (packed triangular), and subclasses of these, such as "dppMatrix".

Slots

uplo: "character"; either "U", for upper triangular, and "L", for lower.
Dim, Dimnames: as all [Matrix](#) objects.

Extends

Class "[denseMatrix](#)", directly. Class "[Matrix](#)", by class "denseMatrix", distance 2.

Methods

```
pack signature(x = "packedMatrix"): ...
unpack signature(x = "packedMatrix"): ...
isSymmetric signature(object = "packedMatrix"): ...
isTriangular signature(object = "packedMatrix"): ...
isDiagonal signature(object = "packedMatrix"): ...
t signature(x = "packedMatrix"): ...
diag signature(x = "packedMatrix"): ...
diag<- signature(x = "packedMatrix"): ...
```

Author(s)

Mikael Jagan

See Also

[pack](#) and [unpack](#); its virtual "complement" "[unpackedMatrix](#)"; its proper subclasses "[dspMatrix](#)", "[ltpMatrix](#)", etc.

Examples

```
showClass("packedMatrix")
showMethods(classes = "packedMatrix")
```

pMatrix-class

Permutation matrices

Description

The pMatrix class is the class of *permutation* matrices, stored as 1-based integer permutation vectors. A permutation matrix is a square matrix whose rows *and* columns are all standard unit vectors. It follows that permutation matrices are a special case of *index* matrices (hence pMatrix is defined as a direct subclass of indMatrix).

Multiplying a matrix on the left by a permutation matrix is equivalent to permuting its rows. Analogously, multiplying a matrix on the right by a permutation matrix is equivalent to permuting its columns. Indeed, such products are implemented in **Matrix** as indexing operations; see ‘Details’ below.

Details

By definition, a permutation matrix is both a row index matrix and a column index matrix. However, the perm slot of a pMatrix cannot be used interchangeably as a row index vector and column index vector. If margin=1, then perm is a row index vector, and the corresponding column index vector can be computed as invPerm(perm), i.e., by inverting the permutation. Analogously, if margin=2, then perm and invPerm(perm) are column and row index vectors, respectively.

Given an n-by-n row permutation matrix P with perm slot p and a matrix M with conformable dimensions, we have

$$\begin{array}{llll}
 PM & = & P \% \% M & = & M[p,] \\
 MP & = & M \% \% P & = & M[, i(p)] \\
 P'M & = & \text{crossprod}(P, M) & = & M[i(p),] \\
 MP' & = & \text{tcrossprod}(M, P) & = & M[, p] \\
 P'P & = & \text{crossprod}(P) & = & \text{Diagonal}(n) \\
 PP' & = & \text{tcrossprod}(P) & = & \text{Diagonal}(n)
 \end{array}$$

where $i := \text{invPerm}$.

Objects from the Class

Objects can be created explicitly with calls of the form new("pMatrix", ...), but they are more commonly created by coercing 1-based integer index vectors, with calls of the form as(., "pMatrix"); see ‘Methods’ below.

Slots

margin, perm inherited from superclass indMatrix. Here, perm is an integer vector of length Dim[1] and a permutation of 1:Dim[1].

Dim, Dimnames inherited from virtual superclass Matrix.

Extends

Class `"indMatrix"`, directly.

Methods

`%%` signature(x = "pMatrix", y = "Matrix") and others listed by `showMethods("%*%", classes = "pMatrix")`: matrix products implemented where appropriate as indexing operations.

`coerce` signature(from = "numeric", to = "pMatrix"): supporting typical pMatrix construction from a vector of positive integers, specifically a permutation of 1:n. Row permutation is assumed.

`t` signature(x = "pMatrix"): the transpose, which is a pMatrix with identical perm but opposite margin. Coincides with the inverse, as permutation matrices are orthogonal.

`solve` signature(a = "pMatrix", b = "missing"): the inverse permutation matrix, which is a pMatrix with identical perm but opposite margin. Coincides with the transpose, as permutation matrices are orthogonal. See `showMethods("solve", classes = "pMatrix")` for more signatures.

`determinant` signature(x = "pMatrix", logarithm = "logical"): always returning 1 or -1, as permutation matrices are orthogonal. In fact, the result is exactly the *sign* of the permutation.

See Also

Superclass `indMatrix` of index matrices, for many inherited methods; `invPerm`, for computing inverse permutation vectors.

Examples

```
(pm1 <- as(as.integer(c(2,3,1)), "pMatrix"))
t(pm1) # is the same as
solve(pm1)
pm1 %% t(pm1) # check that the transpose is the inverse
stopifnot(all(diag(3) == as(pm1 %% t(pm1), "matrix")),
           is.logical(as(pm1, "matrix")))

set.seed(11)
## random permutation matrix :
(p10 <- as(sample(10), "pMatrix"))

## Permute rows / columns of a numeric matrix :
(mm <- round(array(rnorm(3 * 3), c(3, 3)), 2))
mm %% pm1
pm1 %% mm
try(as(as.integer(c(3,3,1)), "pMatrix"))# Error: not a permutation

as(pm1, "TsparseMatrix")
p10[1:7, 1:4] # gives an "ngTMatrix" (most economic!)

## row-indexing of a <pMatrix> keeps it as an <indMatrix>:
p10[1:3, ]
```

printSpMatrix

Format and Print Sparse Matrices Flexibly

Description

Format and print sparse matrices flexibly. These are the “workhorses” used by the `format`, `show` and `print` methods for sparse matrices. If `x` is large, `printSpMatrix2(x)` calls `printSpMatrix()` twice, namely, for the first and the last few rows, suppressing those in between, and also suppresses columns when `x` is too wide.

`printSpMatrix()` basically prints the result of `formatSpMatrix()`.

Usage

```
formatSpMatrix(x, digits = NULL, maxp = 1e9,
               cld = getClassDef(class(x)), zero.print = ".",
               col.names, note.dropping.colnames = TRUE, uniDiag = TRUE,
               align = c("fancy", "right"), ...)

printSpMatrix(x, digits = NULL, maxp = max(100L, getOption("max.print")),
              cld = getClassDef(class(x)),
              zero.print = ".", col.names, note.dropping.colnames = TRUE,
              uniDiag = TRUE, col.trailer = "",
              align = c("fancy", "right"), ...)

printSpMatrix2(x, digits = NULL, maxp = max(100L, getOption("max.print")),
               zero.print = ".", col.names, note.dropping.colnames = TRUE,
               uniDiag = TRUE, suppRows = NULL, suppCols = NULL,
               col.trailer = if(suppCols) "....." else "",
               align = c("fancy", "right"),
               width = getOption("width"), fitWidth = TRUE, ...)
```

Arguments

<code>x</code>	an R object inheriting from class <code>sparseMatrix</code> .
<code>digits</code>	significant digits to use for printing, see <code>print.default</code> , the default, <code>NULL</code> , corresponds to using <code>getOption("digits")</code> .
<code>maxp</code>	integer, default from <code>options(max.print)</code> , influences how many entries of large matrices are printed at all. Typically should not be smaller than around 1000; values smaller than 100 are silently “rounded up” to 100.
<code>cld</code>	the class definition of <code>x</code> ; must be equivalent to <code>getClassDef(class(x))</code> and exists mainly for possible speedup.
<code>zero.print</code>	character which should be printed for <i>structural</i> zeroes. The default <code>."</code> may occasionally be replaced by <code>" "</code> (blank); using <code>"0"</code> would look almost like <code>print()</code> ing of non-sparse matrices.

<code>col.names</code>	logical or string specifying if and how column names of <code>x</code> should be printed, possibly abbreviated. The default is taken from <code>options("sparse.colnames")</code> if that is set, otherwise FALSE unless there are less than ten columns. When TRUE the full column names are printed. When <code>col.names</code> is a string beginning with "abb" or "sub" and ending with an integer <code>n</code> (i.e., of the form "abb... <n>"), the column names are <code>abbreviate()</code> or <code>substring()</code> ed to (target) length <code>n</code> , see the examples.
<code>note.dropping.colnames</code>	logical specifying, when <code>col.names</code> is FALSE if the dropping of the column names should be noted, TRUE by default.
<code>uniDiag</code>	logical indicating if the diagonal entries of a sparse unit triangular or unit-diagonal matrix should be formatted as "I" instead of "1" (to emphasize that the 1's are "structural").
<code>col.trailer</code>	a string to be appended to the right of each column; this is typically made use of by <code>show(<sparseMatrix>)</code> only, when suppressing columns.
<code>suppRows, suppCols</code>	logicals or NULL, for <code>printSpMatrix2()</code> specifying if rows or columns should be suppressed in printing. If NULL, sensible defaults are determined from <code>dim(x)</code> and <code>options(c("width", "max.print"))</code> . Setting both to FALSE may be a very bad idea.
<code>align</code>	a string specifying how the <code>zero.print</code> codes should be aligned, i.e., padded as strings. The default, "fancy", takes some effort to align the typical <code>zero.print = "."</code> with the position of 0, i.e., the first decimal (one left of decimal point) of the numbers printed, whereas <code>align = "right"</code> just makes use of <code>print(*, right = TRUE)</code> .
<code>width</code>	number, a positive integer, indicating the approximately desired (line) width of the output, see also <code>fitWidth</code> .
<code>fitWidth</code>	logical indicating if some effort should be made to match the desired width or temporarily enlarge that if deemed necessary.
<code>...</code>	unused optional arguments.

Details

formatSpMatrix: If `x` is large, only the first rows making up the approximately first `maxp` entries is used, otherwise all of `x`. `.formatSparseSimple()` is applied to (a dense version of) the matrix. Then, `formatSparseM` is used, unless in trivial cases or for sparse matrices without `x` slot.

Value

`formatSpMatrix()`
returns a character matrix with possibly empty column names, depending on `col.names` etc, see above.

`printSpMatrix*()`
return `x` invisibly, see `invisible`.

Author(s)

Martin Maechler

See Also

the virtual class [sparseMatrix](#) and the classes extending it; maybe [sparseMatrix](#) or [spMatrix](#) as simple constructors of such matrices.

The underlying utilities [formatSparseM](#) and [.formatSparseSimple\(\)](#) (on the same page).

Examples

```
f1 <- gl(5, 3, labels = LETTERS[1:5])
X <- as(f1, "sparseMatrix")
X ## <==> show(X) <==> print(X)
t(X) ## shows column names, since only 5 columns

X2 <- as(gl(12, 3, labels = paste(LETTERS[1:12], "c", sep=".")),
        "sparseMatrix")
X2
## less nice, but possible:
print(X2, col.names = TRUE) # use [,1] [,2] .. => does not fit

## Possibilities with column names printing:
      t(X2) # suppressing column names
print(t(X2), col.names=TRUE)
print(t(X2), zero.print = "", col.names="abbr. 1")
print(t(X2), zero.print = "-", col.names="substring 2")
```

qr-methods

Methods for QR Factorization

Description

Computes the pivoted QR factorization of an $m \times n$ real matrix A , which has the general form

$$P_1 A P_2 = QR$$

or (equivalently)

$$A = P_1' Q R P_2'$$

where P_1 and P_2 are permutation matrices, $Q = \prod_{j=1}^n H_j$ is an $m \times m$ orthogonal matrix equal to the product of n Householder matrices H_j , and R is an $m \times n$ upper trapezoidal matrix.

[denseMatrix](#) use the default method implemented in **base**, namely [qr.default](#). It is built on LINPACK routine dqrdc and LAPACK routine dgeqp3, which do not pivot rows, so that P_1 is an identity matrix.

Methods for [sparseMatrix](#) are built on CXSparse routines `cs_sqr` and `cs_qr`, which require $m \geq n$.

Usage

```
qr(x, ...)
## S4 method for signature 'dgMatrix'
qr(x, order = 3L, ...)
```

Arguments

x a **finite** matrix or **Matrix** to be factorized, satisfying `nrow(x) >= ncol(x)` if sparse.

order an integer in `0:3` passed to CXSparse routine `cs_sqr`, indicating a strategy for choosing the column permutation P_2 . 0 means no column permutation. 1, 2, and 3 indicate a fill-reducing ordering of $A + A'$, $\tilde{A}'\tilde{A}$, and $A'A$, where \tilde{A} is A with “dense” rows removed. Do not set to 0 unless you know that the column order of A is already sensible.

... further arguments passed to or from methods.

Details

If x is sparse and structurally rank deficient, having structural rank $r < n$, then x is augmented with $(n - r)$ rows of (partly non-structural) zeros, such that the augmented matrix has structural rank n . This augmented matrix is factorized as described above:

$$P_1 A P_2 = P_1 \begin{bmatrix} A_0 \\ 0 \end{bmatrix} P_2 = Q R$$

where A_0 denotes the original, user-supplied $(m - (n - r)) \times n$ matrix.

Value

An object representing the factorization, inheriting from virtual S4 class **QR** or S3 class **qr**. The specific class is **qr** unless x inherits from virtual class **sparseMatrix**, in which case it is **sparseQR**.

References

Davis, T. A. (2006). *Direct methods for sparse linear systems*. Society for Industrial and Applied Mathematics. doi:10.1137/1.9780898718881

Golub, G. H., & Van Loan, C. F. (2013). *Matrix computations* (4th ed.). Johns Hopkins University Press. doi:10.56021/9781421407944

See Also

Class **sparseQR** and its methods.

Class **dgMatrix**.

Generic function **qr** from **base**, whose default method `qr.default` “defines” the S3 class **qr** of dense QR factorizations.

Generic functions **expand1** and **expand2**, for constructing matrix factors from the result.

Generic functions **Cholesky**, **BunchKaufman**, **Schur**, and **lu**, for computing other factorizations.

Examples

```

showMethods("qr", inherited = FALSE)

## Rank deficient: columns 3 {b2} and 6 {c3} are "extra"
M <- as(cbind(a1 = 1,
              b1 = rep(c(1, 0), each = 3L),
              b2 = rep(c(0, 1), each = 3L),
              c1 = rep(c(1, 0, 0), 2L),
              c2 = rep(c(0, 1, 0), 2L),
              c3 = rep(c(0, 0, 1), 2L)),
        "CsparseMatrix")
rownames(M) <- paste0("r", seq_len(nrow(M)))
b <- 1:6
eps <- .Machine$double.eps

## .... [1] full rank .....
## ==> a least squares solution of A x = b exists
##      and is unique _in exact arithmetic_

(A1 <- M[, -c(3L, 6L)])
(qr.A1 <- qr(A1))

stopifnot(exprs = {
  rankMatrix(A1) == ncol(A1)
  { d1 <- abs(diag(qr.A1@R)); sum(d1 < max(d1) * eps) == 0L }
  rcond(crossprod(A1)) >= eps
  all.equal(qr.coef(qr.A1, b), drop(solve(crossprod(A1), crossprod(A1, b))))
  all.equal(qr.fitted(qr.A1, b) + qr.resid(qr.A1, b), b)
})

## .... [2] numerically rank deficient with full structural rank .....
## ==> a least squares solution of A x = b does not
##      exist or is not unique _in exact arithmetic_

(A2 <- M)
(qr.A2 <- qr(A2))

stopifnot(exprs = {
  rankMatrix(A2) == ncol(A2) - 2L
  { d2 <- abs(diag(qr.A2@R)); sum(d2 < max(d2) * eps) == 2L }
  rcond(crossprod(A2)) < eps

  ## 'qr.coef' computes unique least squares solution of "nearby" problem
  ## Z x = b for some full rank Z ~ A, currently without warning {FIXME} !
  tryCatch({ qr.coef(qr.A2, b); TRUE }, condition = function(x) FALSE)

  all.equal(qr.fitted(qr.A2, b) + qr.resid(qr.A2, b), b)
})

## .... [3] numerically and structurally rank deficient .....
## ==> factorization of _augmented_ matrix with
##      full structural rank proceeds as in [2]

```

```

## NB: implementation details are subject to change; see (*) below

A3 <- M
A3[, c(3L, 6L)] <- 0
A3
(qr.A3 <- qr(A3)) # with a warning ... "additional 2 row(s) of zeros"

stopifnot(exprs = {
  ## sparseQR object preserves the unaugmented dimensions (*)
  dim(qr.A3 ) == dim(A3)
  dim(qr.A3@V) == dim(A3) + c(2L, 0L)
  dim(qr.A3@R) == dim(A3) + c(2L, 0L)

  ## The augmented matrix remains numerically rank deficient
  rankMatrix(A3) == ncol(A3) - 2L
  { d3 <- abs(diag(qr.A3@R)); sum(d3 < max(d3) * eps) == 2L }
  rcond(crossprod(A3)) < eps
})

## Auxiliary functions accept and return a vector or matrix
## with dimensions corresponding to the unaugmented matrix (*),
## in all cases with a warning
qr.coef (qr.A3, b)
qr.fitted(qr.A3, b)
qr.resid (qr.A3, b)

## .... [4] yet more examples .....

## By disabling column pivoting, one gets the "vanilla" factorization
##  $A = Q^{\sim} R$ , where  $Q^{\sim} := P1' Q$  is orthogonal because P1 and Q are

(qr.A1.pp <- qr(A1, order = 0L)) # partial pivoting

ae1 <- function(a, b, ...) all.equal(as(a, "matrix"), as(b, "matrix"), ...)
ae2 <- function(a, b, ...) ae1(unname(a), unname(b), ...)

stopifnot(exprs = {
  length(qr.A1 @q) == ncol(A1)
  length(qr.A1.pp@q) == 0L # indicating no column pivoting
  ae2(A1[, qr.A1@q + 1L], qr.Q(qr.A1 ) %*% qr.R(qr.A1 ))
  ae2(A1 , qr.Q(qr.A1.pp) %*% qr.R(qr.A1.pp))
})

```

rankMatrix

*Rank of a Matrix***Description**

Compute ‘the’ matrix rank, a well-defined functional in theory(*), somewhat ambiguous in practice. We provide several methods, the default corresponding to Matlab’s definition.

(*) The rank of a $n \times m$ matrix A , $rk(A)$, is the maximal number of linearly independent columns (or rows); hence $rk(A) \leq \min(n, m)$.

Usage

```
rankMatrix(x, tol = NULL,
           method = c("tolNorm2", "qr.R", "qrLINPACK", "qr",
                    "useGrad", "maybeGrad"),
           sval = svd(x, 0, 0)$d, warn.t = TRUE, warn.qr = TRUE)

qr2rankMatrix(qr, tol = NULL, isBqr = is.qr(qr), do.warn = TRUE)
```

Arguments

x	numeric matrix, of dimension $n \times m$, say.
tol	nonnegative number specifying a (relative, “scalefree”) tolerance for testing of “practically zero” with specific meaning depending on method; by default, $\max(\dim(x)) * .Machine\$double.eps$ is according to Matlab’s default (for its only method which is our method=“tolNorm2”).
method	a character string specifying the computational method for the rank, can be abbreviated: “tolNorm2”: the number of singular values $\geq \text{tol} * \max(\text{sval})$; “qrLINPACK”: for a dense matrix, this is the rank of <code>qr(x, tol, LAPACK=FALSE)</code> (which is <code>qr(...)\$rank</code>); This (“qr*”, dense) version used to be <i>the</i> recommended way to compute a matrix rank for a while in the past. For sparse x, this is equivalent to “qr.R”. “qr.R”: this is the rank of triangular matrix R , where <code>qr()</code> uses LAPACK or a “sparseQR” method (see qr-methods) to compute the decomposition QR . The rank of R is then defined as the number of “non-zero” diagonal entries d_i of R , and “non-zero”’s fulfill $ d_i \geq \text{tol} \cdot \max(d_i)$. “qr”: is for back compatibility; for dense x, it corresponds to “qrLINPACK”, whereas for sparse x, it uses “qr.R”. For all the “qr*” methods, singular values <code>sval</code> are not used, which may be crucially important for a large sparse matrix x, as in that case, when <code>sval</code> is not specified, the default, computing <code>svd()</code> currently coerces x to a dense matrix. “useGrad”: considering the “gradient” of the (decreasing) singular values, the index of the <i>smallest</i> gap. “maybeGrad”: choosing method “useGrad” only when that seems <i>reasonable</i> ; otherwise using “tolNorm2”.
sval	numeric vector of non-increasing singular values of x; typically unspecified and computed from x when needed, i.e., unless method = “qr”.
warn.t	logical indicating if <code>rankMatrix()</code> should warn when it needs <code>t(x)</code> instead of x. Currently, for method = “qr” only, gives a warning by default because the caller often could have passed <code>t(x)</code> directly, more efficiently.

warn.qr	in the <i>QR</i> cases (i.e., if method starts with "qr"), rankMatrix() calls qr2rankMatrix(..., do.warn = warn.qr), see below.
qr	an R object resulting from qr(x, ...), i.e., typically inheriting from class "qr" or "sparseQR".
isBqr	logical indicating if qr is resulting from base qr(). (Otherwise, it is typically from Matrix package sparse qr.)
do.warn	logical; if true, warn about non-finite diagonal entries in the <i>R</i> matrix of the <i>QR</i> decomposition. Do not change lightly!

Details

qr2rankMatrix() is typically called from rankMatrix() for the "qr"* methods, but can be used directly - much more efficiently in case the qr-decomposition is available anyway.

Value

If x is a matrix of all 0 (or of zero dimension), the rank is zero; otherwise, typically a positive integer in 1:min(dim(x)) with attributes detailing the method used.

There are rare cases where the sparse *QR* decomposition "fails" in so far as the diagonal entries of *R*, the d_i (see above), end with non-finite, typically NaN entries. Then, a warning is signalled (unless warn.qr / do.warn is not true) and NA (specifically, NA_integer_) is returned.

Note

For large sparse matrices x, unless you can specify sval yourself, currently method = "qr" may be the only feasible one, as the others need sval and call svd() which currently coerces x to a denseMatrix which may be very slow or impossible, depending on the matrix dimensions.

Note that in the case of sparse x, method = "qr", all non-strictly zero diagonal entries d_i where counted, up to including Matrix version 1.1-0, i.e., that method implicitly used tol = 0, see also the set.seed(42) example below.

Author(s)

Martin Maechler; for the "*Grad" methods building on suggestions by Ravi Varadhan.

See Also

qr, svd.

Examples

```
rankMatrix(cbind(1, 0, 1:3)) # 2

(meths <- eval(formals(rankMatrix)$method))

## a "border" case:
H12 <- Hilbert(12)
rankMatrix(H12, tol = 1e-20) # 12; but 11 with default method & tol.
sapply(meths, function(.m.) rankMatrix(H12, method = .m.))
```

```

## tolNorm2  qr.R  qrLINPACK  qr  useGrad  maybeGrad
##      11      11          12  12      11      11
## The meaning of 'tol' for method="qrLINPACK" and *dense* x is not entirely "scale free"
rMQL <- function(ex, M) rankMatrix(M, method="qrLINPACK", tol = 10^-ex)
rMQR <- function(ex, M) rankMatrix(M, method="qr.R",      tol = 10^-ex)
sapply(5:15, rMQL, M = H12) # result is platform dependent
## 7 7 8 10 10 11 11 11 12 12 12 {x86_64}
sapply(5:15, rMQL, M = 1000 * H12) # not identical unfortunately
## 7 7 8 10 11 11 12 12 12 12 12
sapply(5:15, rMQR, M = H12)
## 5 6 7 8 8 9 9 10 10 11 11
sapply(5:15, rMQR, M = 1000 * H12) # the *same*

## "sparse" case:
M15 <- kronecker(diag(x=c(100,1,10)), Hilbert(5))
sapply(meths, function(.m.) rankMatrix(M15, method = .m.))
#--> all 15, but 'useGrad' has 14.
sapply(meths, function(.m.) rankMatrix(M15, method = .m., tol = 1e-7)) # all 14

## "large" sparse
n <- 250000; p <- 33; nnz <- 10000
L <- sparseMatrix(i = sample.int(n, nnz, replace=TRUE),
                  j = sample.int(p, nnz, replace=TRUE),
                  x = rnorm(nnz))
(st1 <- system.time(r1 <- rankMatrix(L))) # warning+ ~1.5 sec (2013)
(st2 <- system.time(r2 <- rankMatrix(L, method = "qr"))) # considerably faster!
r1[[1]] == print(r2[[1]]) ## --> ( 33 TRUE )

## another sparse-"qr" one, which ``failed'' till 2013-11-23:
set.seed(42)
f1 <- factor(sample(50, 1000, replace=TRUE))
f2 <- factor(sample(50, 1000, replace=TRUE))
f3 <- factor(sample(50, 1000, replace=TRUE))
D <- t(do.call(rbind, lapply(list(f1,f2,f3), as, 'sparseMatrix')))
dim(D); nnzero(D) ## 1000 x 150 // 3000 non-zeros (= 2%)
stopifnot(rankMatrix(D, method='qr') == 148,
           rankMatrix(crossprod(D),method='qr') == 148)

## zero matrix has rank 0 :
stopifnot(sapply(meths, function(.m.)
                 rankMatrix(matrix(0, 2, 2), method = .m.)) == 0)

```

Description

Estimate the reciprocal of the condition number of a matrix.

This is a generic function with several methods, as seen by `showMethods(rcond)`.

Usage

```
rcond(x, norm, ...)
```

```
## S4 method for signature 'sparseMatrix,character'
rcond(x, norm, useInv=FALSE, ...)
```

Arguments

x	an R object that inherits from the <code>Matrix</code> class.
norm	character string indicating the type of norm to be used in the estimate. The default is "0" for the 1-norm ("0" is equivalent to "1"). For sparse matrices, when <code>useInv=TRUE</code> , <code>norm</code> can be any of the kinds allowed for <code>norm</code> ; otherwise, the other possible value is "I" for the infinity norm, see also <code>norm</code> .
useInv	logical (or "Matrix" containing <code>solve(x)</code>). If not false, compute the reciprocal condition number as $1/(\ x\ \cdot \ x^{-1}\)$, where x^{-1} is the inverse of x , <code>solve(x)</code> . This may be an efficient alternative (only) in situations where <code>solve(x)</code> is fast (or known), e.g., for (very) sparse or triangular matrices. Note that the <i>result</i> may differ depending on <code>useInv</code> , as per default, when it is false, an <i>approximation</i> is computed.
...	further arguments passed to or from other methods.

Value

An estimate of the reciprocal condition number of x .

BACKGROUND

The condition number of a regular (square) matrix is the product of the `norm` of the matrix and the norm of its inverse (or pseudo-inverse).

More generally, the condition number is defined (also for non-square matrices A) as

$$\kappa(A) = \frac{\max_{\|v\|=1} \|Av\|}{\min_{\|v\|=1} \|Av\|}.$$

Whenever x is *not* a square matrix, in our method definitions, this is typically computed via `rcond(qr.R(qr(X)), ...)` where X is x or $t(x)$.

The condition number takes on values between 1 and infinity, inclusive, and can be viewed as a factor by which errors in solving linear systems with this matrix as coefficient matrix could be magnified.

`rcond()` computes the *reciprocal* condition number $1/\kappa$ with values in $[0, 1]$ and can be viewed as a scaled measure of how close a matrix is to being rank deficient (aka "singular").

Condition numbers are usually estimated, since exact computation is costly in terms of floating-point operations. An (over) estimate of reciprocal condition number is given, since by doing so overflow is avoided. Matrices are well-conditioned if the reciprocal condition number is near 1 and ill-conditioned if it is near zero.

References

Golub, G., and Van Loan, C. F. (1989). *Matrix Computations*, 2nd edition, Johns Hopkins, Baltimore.

See Also

`norm`, `kappa()` from package **base** computes an *approximate* condition number of a “traditional” matrix, even non-square ones, with respect to the $p = 2$ (Euclidean) `norm.solve`.

`condest`, a newer *approximate* estimate of the (1-norm) condition number, particularly efficient for large sparse matrices.

Examples

```
x <- Matrix(rnorm(9), 3, 3)
rcond(x)
## typically "the same" (with more computational effort):
1 / (norm(x) * norm(solve(x)))
rcond(Hilbert(9)) # should be about 9.1e-13

## For non-square matrices:
rcond(x1 <- cbind(1,1:10))# 0.05278
rcond(x2 <- cbind(x1, 2:11))# practically 0, since x2 does not have full rank

## sparse
(S1 <- Matrix(rbind(0:1,0, diag(3:-2))))
rcond(S1)
m1 <- as(S1, "denseMatrix")
all.equal(rcond(S1), rcond(m1))

## wide and sparse
rcond(Matrix(cbind(0, diag(2:-1))))

## Large sparse example -----
m <- Matrix(c(3,0:2), 2,2)
M <- bdiag(kronecker(Diagonal(2), m), kronecker(m,m))
36*(iM <- solve(M)) # still sparse
MM <- kronecker(Diagonal(10), kronecker(Diagonal(5),kronecker(m,M)))
dim(M3 <- kronecker(bdiag(M,M),MM)) # 12'800 ^ 2
if(interactive()) ## takes about 2 seconds if you have >= 8 GB RAM
  system.time(r <- rcond(M3))
## whereas this is *fast* even though it computes solve(M3)
system.time(r. <- rcond(M3, useInv=TRUE))
if(interactive()) ## the values are not the same
  c(r, r.) # 0.05555 0.013888
## for all 4 norms available for sparseMatrix :
cbind(rr <- sapply(c("1","I","F","M"),
  function(N) rcond(M3, norm=N, useInv=TRUE)))
```

rep2abI	<i>Replicate Vectors into 'abIndex' Result</i>
---------	--

Description

rep2abI(x, times) conceptually computes `rep.int(x, times)` but with an `abIndex` class result.

Usage

```
rep2abI(x, times)
```

Arguments

x	numeric vector
times	integer (valued) scalar: the number of repetitions

Value

a vector of `class abIndex`

See Also

`rep.int()`, the base function; `abIseq`, `abIndex`.

Examples

```
(ab <- rep2abI(2:7, 4))
stopifnot(identical(as(ab, "numeric"),
  rep(2:7, 4)))
```

rleDiff-class	<i>Class "rleDiff" of rle(diff(.)) Stored Vectors</i>
---------------	---

Description

Class "rleDiff" is for compactly storing long vectors which mainly consist of *linear* stretches. For such a vector x, `diff(x)` consists of *constant* stretches and is hence well compressable via `rle()`.

Objects from the Class

Objects can be created by calls of the form `new("rleDiff", ...)`.

Currently experimental, see below.

Slots

first: A single number (of class "numLike", a class union of "numeric" and "logical").

rle: Object of class "rle", basically a `list` with components "lengths" and "values", see `rle()`. As this is used to encode potentially huge index vectors, lengths may be of type `double` here.

Methods

There is a simple `show` method only.

Note

This is currently an *experimental* auxiliary class for the class `abIndex`, see there.

See Also

`rle`, `abIndex`.

Examples

```
showClass("rleDiff")

ab <- c(abIseq(2, 100), abIseq(20, -2))
ab@rleD # is "rleDiff"
```

rsparsematrix

Random Sparse Matrix

Description

Generate a random sparse matrix efficiently. The default has rounded gaussian non-zero entries, and `rand.x = NULL` generates random pattern matrices, i.e. inheriting from `nsparseMatrix`.

Usage

```
rsparsematrix(nrow, ncol, density, nnz = round(density * maxE),
              symmetric = FALSE,
              rand.x = function(n) signif(rnorm(n), 2), ...)
```

Arguments

<code>nrow, ncol</code>	number of rows and columns, i.e., the matrix dimension (<code>dim</code>).
<code>density</code>	optional number in $[0, 1]$, the density is the proportion of non-zero entries among all matrix entries. If specified it determines the default for <code>nnz</code> , otherwise <code>nnz</code> needs to be specified.
<code>nnz</code>	number of non-zero entries, for a sparse matrix typically considerably smaller than <code>nrow*ncol</code> . Must be specified if <code>density</code> is not.

symmetric	logical indicating if result should be a matrix of class <code>symmetricMatrix</code> . Note that in the symmetric case, <code>nnz</code> denotes the number of non zero entries of the upper (or lower) part of the matrix, including the diagonal.
rand.x	<code>NULL</code> or the random number generator for the <code>x</code> slot, a <code>function</code> such that <code>rand.x(n)</code> generates a numeric vector of length <code>n</code> . Typical examples are <code>rand.x = rnorm</code> , or <code>rand.x = runif</code> ; the default is nice for didactical purposes.
...	optionally further arguments passed to <code>sparseMatrix()</code> , notably <code>repr</code> .

Details

The algorithm first samples “encoded” (i, j) s without replacement, via one dimensional indices, if not symmetric `sample.int(nrow*ncol, nnz)`, then—if `rand.x` is not `NULL`—gets `x <- rand.x(nnz)` and calls `sparseMatrix(i=i, j=j, x=x, ...)`. When `rand.x=NULL`, `sparseMatrix(i=i, j=j, ...)` will return a pattern matrix (i.e., inheriting from `nsparseMatrix`).

Value

a `sparseMatrix`, say `M` of dimension $(nrow, ncol)$, i.e., with `dim(M) == c(nrow, ncol)`, if `symmetric` is not true, with `nzM <- nnzero(M)` fulfilling `nzM <= nnz` and typically, `nzM == nnz`.

Author(s)

Martin Maechler

Examples

```
set.seed(17)# to be reproducible
M <- rsparsematrix(8, 12, nnz = 30) # small example, not very sparse
M
M1 <- rsparsematrix(1000, 20, nnz = 123, rand.x = runif)
summary(M1)

## a random *symmetric* Matrix
(S9 <- rsparsematrix(9, 9, nnz = 10, symmetric=TRUE)) # dsCMatrix
nnzero(S9)# ~ 20: as 'nnz' only counts one "triangle"

## a random patter*n* aka boolean Matrix (no 'x' slot):
(n7 <- rsparsematrix(5, 12, nnz = 10, rand.x = NULL))

## a [T]riplet representation sparseMatrix:
T2 <- rsparsematrix(40, 12, nnz = 99, repr = "T")
head(T2)
```

RsparseMatrix-class *Class "RsparseMatrix" of Sparse Matrices in Row-compressed Form*

Description

The "RsparseMatrix" class is the virtual class of all sparse matrices coded in sorted compressed row-oriented form. Since it is a virtual class, no objects may be created from it. See `showClass("RsparseMatrix")` for its subclasses.

Slots

j: Object of class "integer" of length `nnzero` (number of non-zero elements). These are the row numbers for each non-zero element in the matrix.

p: Object of class "integer" of pointers, one for each row, to the initial (zero-based) index of elements in the row.

Dim, Dimnames: inherited from the superclass, see [sparseMatrix](#).

Extends

Class "sparseMatrix", directly. Class "Matrix", by class "sparseMatrix".

Methods

Originally, **few** methods were defined on purpose, as we rather use the [CsparseMatrix](#) in **Matrix**. Then, more methods were added but *beware* that these typically do *not* return "RsparseMatrix" results, but rather Csparse* or Tsparse* ones; e.g., `R[i, j] <- v` for an "RsparseMatrix" R works, but after the assignment, R is a (triplet) "TsparseMatrix".

t signature(x = "RsparseMatrix"): ...

coerce signature(from = "RsparseMatrix", to = "CsparseMatrix"): ...

coerce signature(from = "RsparseMatrix", to = "TsparseMatrix"): ...

See Also

its superclass, [sparseMatrix](#), and, e.g., class [dgRMatrix](#) for the links to other classes.

Examples

```
showClass("RsparseMatrix")
```


Description

Schur is the class of Schur factorizations of $n \times n$ real matrices A , having the general form

$$A = QTQ'$$

where Q is an orthogonal matrix and T is a block upper triangular matrix with 1×1 or 2×2 diagonal blocks specifying the real and complex conjugate eigenvalues of A . The column vectors of Q are the Schur vectors of A , and T is the Schur form of A .

The Schur factorization generalizes the spectral decomposition of normal matrices A , whose Schur form is block diagonal, to arbitrary square matrices.

Details

The matrix A and its Schur form T are *similar* and thus have the same spectrum. The eigenvalues are computed trivially as the eigenvalues of the diagonal blocks of T .

Slots

`Dim`, `Dimnames` inherited from virtual class [MatrixFactorization](#).

`Q` an orthogonal matrix, inheriting from virtual class [Matrix](#).

`T` a block upper triangular matrix, inheriting from virtual class [Matrix](#). The diagonal blocks have dimensions 1-by-1 or 2-by-2.

`EValues` a numeric or complex vector containing the eigenvalues of the diagonal blocks of `T`, which are the eigenvalues of `T` and consequently of the factorized matrix.

Extends

Class [SchurFactorization](#), directly. Class [MatrixFactorization](#), by class [SchurFactorization](#), distance 2.

Instantiation

Objects can be generated directly by calls of the form `new("Schur", ...)`, but they are more typically obtained as the value of `Schur(x)` for `x` inheriting from [Matrix](#) (often [dgeMatrix](#)).

Methods

`determinant` signature(`from = "Schur"`, `logarithm = "logical"`): computes the determinant of the factorized matrix A or its logarithm.

`expand1` signature(`x = "Schur"`): see [expand1-methods](#).

`expand2` signature(`x = "Schur"`): see [expand2-methods](#).

`solve` signature(`a = "Schur"`, `b = .`): see [solve-methods](#).

References

The LAPACK source code, including documentation; see <https://netlib.org/lapack/double/dgees.f>.

Golub, G. H., & Van Loan, C. F. (2013). *Matrix computations* (4th ed.). Johns Hopkins University Press. doi:10.56021/9781421407944

See Also

Class `dgeMatrix`.

Generic functions `Schur`, `expand1` and `expand2`.

Examples

```
showClass("Schur")
set.seed(0)

n <- 4L
(A <- Matrix(rnorm(n * n), n, n))

## With dimnames, to see that they are propagated :
dimnames(A) <- list(paste0("r", seq_len(n)),
                   paste0("c", seq_len(n)))

(sch.A <- Schur(A))
str(e.sch.A <- expand2(sch.A), max.level = 2L)

## A ~ Q T Q' in floating point
stopifnot(exprs = {
  identical(names(e.sch.A), c("Q", "T", "Q."))
  all.equal(A, with(e.sch.A, Q %*% T %*% Q.))
})

## Factorization handled as factorized matrix
b <- rnorm(n)
stopifnot(all.equal(det(A), det(sch.A)),
          all.equal(solve(A, b), solve(sch.A, b)))

## One of the non-general cases:
Schur(Diagonal(6L))
```

Schur-methods

Methods for Schur Factorization

Description

Computes the Schur factorization of an $n \times n$ real matrix A , which has the general form

$$A = QTQ'$$

where Q is an orthogonal matrix and T is a block upper triangular matrix with 1×1 and 2×2 diagonal blocks specifying the real and complex conjugate eigenvalues of A . The column vectors of Q are the Schur vectors of A , and T is the Schur form of A .

Methods are built on LAPACK routine dgees.

Usage

```
Schur(x, vectors = TRUE, ...)
```

Arguments

<code>x</code>	a finite square matrix or Matrix to be factorized.
<code>vectors</code>	a logical. If TRUE (the default), then Schur vectors are computed in addition to the Schur form.
<code>...</code>	further arguments passed to or from methods.

Value

An object representing the factorization, inheriting from virtual class **SchurFactorization** if `vectors = TRUE`. Currently, the specific class is always **Schur** in that case. An exception is if `x` is a traditional matrix, in which case the result is a named list containing `Q`, `T`, and `EValues` slots of the **Schur** object.

If `vectors = FALSE`, then the result is the same named list but without `Q`.

References

The LAPACK source code, including documentation; see <https://netlib.org/lapack/double/dgees.f>.

Golub, G. H., & Van Loan, C. F. (2013). *Matrix computations* (4th ed.). Johns Hopkins University Press. doi:10.56021/9781421407944

See Also

Class **Schur** and its methods.

Class **dgeMatrix**.

Generic functions **expand1** and **expand2**, for constructing matrix factors from the result.

Generic functions **Cholesky**, **BunchKaufman**, **lu**, and **qr**, for computing other factorizations.

Examples

```
showMethods("Schur", inherited = FALSE)
set.seed(0)

Schur(Hilbert(9L)) # real eigenvalues

(A <- Matrix(round(rnorm(25L, sd = 100)), 5L, 5L))
(sch.A <- Schur(A)) # complex eigenvalues
```

```

## A ~ Q T Q' in floating point
str(e.sch.A <- expand2(sch.A), max.level = 2L)
stopifnot(all.equal(A, Reduce(`%*%`, e.sch.A)))

(e1 <- eigen(sch.A@T, only.values = TRUE)$values)
(e2 <- eigen(  A  , only.values = TRUE)$values)
(e3 <- sch.A@EValues)

stopifnot(exprs = {
  all.equal(e1, e2, tolerance = 1e-13)
  all.equal(e1, e3[order(Mod(e3), decreasing = TRUE)], tolerance = 1e-13)
  identical(Schur(A, vectors = FALSE),
            list(T = sch.A@T, EValues = e3))
  identical(Schur(as(A, "matrix"),
                  list(Q = as(sch.A@Q, "matrix"),
                       T = as(sch.A@T, "matrix"), EValues = e3))
            ))
})

```

solve-methods

*Methods in Package **Matrix** for Function solve*

Description

Methods for generic function `solve` for solving linear systems of equations, i.e., for X in $AX = B$, where A is a square matrix and X and B are matrices with dimensions consistent with A .

Usage

```

solve(a, b, ...)

## S4 method for signature 'dgeMatrix,ANY'
solve(a, b, tol = .Machine$double.eps, ...)

## S4 method for signature 'dgCMatrix,missing'
solve(a, b, sparse = TRUE, ...)
## S4 method for signature 'dgCMatrix,matrix'
solve(a, b, sparse = FALSE, ...)
## S4 method for signature 'dgCMatrix,denseMatrix'
solve(a, b, sparse = FALSE, ...)
## S4 method for signature 'dgCMatrix,sparseMatrix'
solve(a, b, sparse = TRUE, ...)

## S4 method for signature 'denseLU,dgeMatrix'
solve(a, b, ...)
## S4 method for signature 'BunchKaufman,dgeMatrix'
solve(a, b, ...)
## S4 method for signature 'Cholesky,dgeMatrix'
solve(a, b, ...)

```

```
## S4 method for signature 'sparseLU,dgCMatrix'
solve(a, b, tol = .Machine$double.eps, ...)
## S4 method for signature 'sparseQR,dgCMatrix'
solve(a, b, ...)
## S4 method for signature 'CHMfactor,dgCMatrix'
solve(a, b, system = c("A", "LDLt", "LD", "DLt", "L", "Lt", "D", "P", "Pt"), ...)
```

Arguments

a	a finite square matrix or Matrix containing the coefficients of the linear system, or otherwise a MatrixFactorization , in which case methods behave (by default) as if the factorized matrix were specified.
b	a vector, sparseVector , matrix, or Matrix satisfying <code>NROW(b) == nrow(a)</code> , giving the right-hand side(s) of the linear system. Vectors b are treated as <code>length(b)-by-1</code> matrices. If b is missing, then methods take b to be an identity matrix.
tol	a non-negative number. For a inheriting from denseMatrix , an error is signaled if the reciprocal one-norm condition number (see rcond) of a is less than tol, indicating that a is near-singular. For a of class sparseLU , an error is signaled if the ratio <code>min(d)/max(d)</code> is less than tol, where <code>d = abs(diag(a@U))</code> . (Interpret with care, as this ratio is a cheap heuristic and <i>not</i> in general equal to or even proportional to the reciprocal one-norm condition number.) Setting <code>tol = 0</code> disables the test.
sparse	a logical indicating if the result should be formally sparse, i.e., if the result should inherit from virtual class sparseMatrix . Only methods for sparse a and missing or matrix b have this argument. Methods for missing or sparse b use <code>sparse = TRUE</code> by default. Methods for dense b use <code>sparse = FALSE</code> by default.
system	a string specifying a linear system to be solved. Only methods for a inheriting from CHMfactor have this argument. See ‘Details’.
...	further arguments passed to or from methods.

Details

Methods for general and symmetric matrices a compute a triangular factorization (LU, Bunch-Kaufman, or Cholesky) and call the method for the corresponding factorization class. The factorization is sparse if a is. Methods for sparse, symmetric matrices a attempt a Cholesky factorization and perform an LU factorization only if that fails (typically because a is not positive definite).

Triangular, diagonal, and permutation matrices do not require factorization (they are already “factors”), hence methods for those are implemented directly. For triangular a, solutions are obtained by forward or backward substitution; for diagonal a, they are obtained by scaling the rows of b; and for permutations a, they are obtained by permuting the rows of b.

Methods for dense a are built on 14 LAPACK routines: class `d.Matrix`, where `..=(ge|tr|tp|sy|sp|po|pp)`, uses routines `d..tri` and `d..trs` for missing and non-missing b, respectively. A corollary is that these methods always give a dense result.

Methods for sparse a are built on CXSparse routines `cs_lsolve`, `cs_usolve`, and `cs_spsolve` and CHOLMOD routines `cholmod_solve` and `cholmod_spsolve`. By default, these methods give a

vector result if b is a vector, a sparse matrix result if b is missing or a sparse matrix, and a dense matrix result if b is a dense matrix. One can override this behaviour by setting the `sparse` argument, where available, but that should be done with care. Note that a sparse result may be sparse only in the formal sense and not at all in the mathematical sense, depending on the nonzero patterns of a and b . Furthermore, whereas dense results are fully preallocated, sparse results must be “grown” in a loop over the columns of b .

Methods for a of class `sparseQR` are simple wrappers around `qr.coef`, giving the *least squares* solution in overdetermined cases.

Methods for a inheriting from `CHMfactor` can solve systems other than the default one $AX = B$. The correspondence between its `system` argument the system actually solved is outlined in the table below. See `CHMfactor-class` for a definition of notation.

system	<code>isLDL(a)=TRUE</code>	<code>isLDL(a)=FALSE</code>
"A"	$AX = B$	$AX = B$
"LDLt"	$L_1DL_1'X = B$	$LL'X = B$
"LD"	$L_1DX = B$	$LX = B$
"DLt"	$DL_1'X = B$	$L'X = B$
"L"	$L_1X = B$	$LX = B$
"Lt"	$L_1'X = B$	$L'X = B$
"D"	$DX = B$	$X = B$
"P"	$X = P_1B$	$X = P_1B$
"Pt"	$X = P_1'B$	$X = P_1'B$

See Also

Virtual class `MatrixFactorization` and its subclasses.

Generic functions `Cholesky`, `BunchKaufman`, `Schur`, `lu`, and `qr` for *computing* factorizations.

Generic function `solve` from `base`.

Function `qr.coef` from `base` for computing least squares solutions of overdetermined linear systems.

Examples

```
## A close to symmetric example with "quite sparse" inverse:
n1 <- 7; n2 <- 3
dd <- data.frame(a = gl(n1,n2), b = gl(n2,1,n1*n2))# balanced 2-way
X <- sparse.model.matrix(~ -1+ a + b, dd)# no intercept --> even sparser
XXt <- tcrossprod(X)
diag(XXt) <- rep(c(0,0,1,0), length.out = nrow(XXt))

n <- nrow(ZZ <- kronecker(XXt, Diagonal(x=c(4,1))))
image(a <- 2*Diagonal(n) + ZZ %*% Diagonal(x=c(10, rep(1, n-1))))
isSymmetric(a) # FALSE
image(drop0(skewpart(a)))
image(ia0 <- solve(a, tol = 0)) # checker board, dense [but really, a is singular!]
try(solve(a, sparse=TRUE))##-> error [ TODO: assertError ]
ia. <- solve(a, sparse=TRUE, tol = 1e-19)##-> *no* error
if(R.version$arch == "x86_64")
  ## Fails on 32-bit [Fedora 19, R 3.0.2] from Matrix 1.1-0 on [FIXME ??] only
```

```

    stopifnot(all.equal(as.matrix(ia.), as.matrix(ia0)))
a <- a + Diagonal(n)
iad <- solve(a)
ias <- solve(a, sparse=FALSE)
stopifnot(all.equal(as(iad,"denseMatrix"), ias, tolerance=1e-14))
I. <- iad %*% a      ; image(I.)
I0 <- drop0(zapsmall(I.)); image(I0)
.I <- a %*% iad
.I0 <- drop0(zapsmall(.I))
stopifnot( all.equal(as(I0, "diagonalMatrix"), Diagonal(n)),
           all.equal(as(.I0,"diagonalMatrix"), Diagonal(n)) )

```

sparse.model.matrix *Construct Sparse Design / Model Matrices*

Description

Construct a sparse model or “design” matrix, from a formula and data frame (`sparse.model.matrix`) or a single factor (`fac2sparse`).

The `fac2[Ss]parse()` functions are utilities, also used internally in the principal user level function `sparse.model.matrix()`.

Usage

```

sparse.model.matrix(object, data = environment(object),
  contrasts.arg = NULL, xlev = NULL, transpose = FALSE,
  drop.unused.levels = FALSE, row.names = TRUE,
  sep = "", verbose = FALSE, ...)

fac2sparse(from, to = c("d", "1", "n"),
  drop.unused.levels = TRUE, repr = c("C", "R", "T"), giveCsparse)
fac2Sparse(from, to = c("d", "1", "n"),
  drop.unused.levels = TRUE, repr = c("C", "R", "T"), giveCsparse,
  factorPatt12, contrasts.arg = NULL)

```

Arguments

object	an object of an appropriate class. For the default method, a model formula or terms object.
data	a data frame created with <code>model.frame</code> . If another sort of object, <code>model.frame</code> is called first.
contrasts.arg	<p>for <code>sparse.model.matrix()</code>: A list, whose entries are contrasts suitable for input to the <code>contrasts</code> replacement function and whose names are the names of columns of data containing <code>factors</code>.</p> <p>for <code>fac2Sparse()</code>: character string or NULL or (coercable to) <code>"sparseMatrix"</code>, specifying the contrasts to be applied to the factor levels.</p>

xlev	to be used as argument of <code>model.frame</code> if data has no "terms" attribute.
transpose	logical indicating if the <i>transpose</i> should be returned; if the transposed is used anyway, setting <code>transpose = TRUE</code> is more efficient.
drop.unused.levels	should factors have unused levels dropped? The default for <code>sparse.model.matrix</code> has been changed to <code>FALSE</code> , 2010-07, for compatibility with R's standard (<code>dense.model.matrix()</code>).
row.names	logical indicating if row names should be used.
sep	<code>character</code> string passed to <code>paste()</code> when constructing column names from the variable name and its levels.
verbose	logical or integer indicating if (and how much) progress output should be printed.
...	further arguments passed to or from other methods.
from	(for <code>fac2sparse()</code> ;) a <code>factor</code> .
to	a character indicating the "kind" of sparse matrix to be returned. The default, "d" is for <code>double</code> .
giveCsparse	deprecated , replaced with <code>repr</code> ; logical indicating if the result must be a <code>CsparseMatrix</code> .
repr	<code>character</code> string, one of "C", "T", or "R", specifying the sparse <i>representation</i> to be used for the result, i.e., one from the super classes <code>CsparseMatrix</code> , <code>TsparseMatrix</code> , or <code>RsparseMatrix</code> .
factorPatt12	logical vector, say <code>fp</code> , of length two; when <code>fp[1]</code> is true, return "contrasted" <code>t(X)</code> ; when <code>fp[2]</code> is true, the original ("dummy") <code>t(X)</code> , i.e, the result of <code>fac2sparse()</code> .

Value

a sparse matrix, extending `CsparseMatrix` (for `fac2sparse()` if `repr = "C"` as per default; a `TsparseMatrix` or `RsparseMatrix`, otherwise).

For `fac2Sparse()`, a `list` of length two, both components with the corresponding transposed model matrix, where the corresponding `factorPatt12` is true.

`fac2sparse()`, the basic workhorse of `sparse.model.matrix()`, returns the *transpose* (`t`) of the model matrix.

Note

`model.Matrix(sparse = TRUE)` from package **MatrixModels** may be nowadays be preferable to `sparse.model.matrix`, as `model.Matrix` returns an object of class `modelMatrix` with additional slots `assign` and `contrasts` relating to the model variables.

Author(s)

Doug Bates and Martin Maechler, with initial suggestions from Tim Hesterberg.

See Also

`model.matrix` in package **stats**, part of base R.

`model.Matrix` in package **MatrixModels**; see 'Note'.

`as(f, "sparseMatrix")` (see `coerce(from = "factor", ...)` in the class doc `sparseMatrix`) produces the *transposed* sparse model matrix for a single factor `f` (and *no* contrasts).

Examples

```

dd <- data.frame(a = gl(3,4), b = gl(4,1,12))# balanced 2-way
options("contrasts") # the default: "contr.treatment"
sparse.model.matrix(~ a + b, dd)
sparse.model.matrix(~ -1+ a + b, dd)# no intercept --> even sparser
sparse.model.matrix(~ a + b, dd, contrasts = list(a="contr.sum"))
sparse.model.matrix(~ a + b, dd, contrasts = list(b="contr.SAS"))

## Sparse method is equivalent to the traditional one :
stopifnot(all(sparse.model.matrix(~ a + b, dd) ==
  Matrix(model.matrix(~ a + b, dd), sparse=TRUE)),
  all(sparse.model.matrix(~0 + a + b, dd) ==
  Matrix(model.matrix(~0 + a + b, dd), sparse=TRUE)))

(ff <- gl(3,4,, c("X","Y", "Z")))
fac2sparse(ff) # 3 x 12 sparse Matrix of class "dgCMatrix"
##
## X 1 1 1 1 . . . . .
## Y . . . . 1 1 1 1 . . . .
## Z . . . . . 1 1 1 1

## can also be computed via sparse.model.matrix():
f30 <- gl(3,0 )
f12 <- gl(3,0, 12)
stopifnot(
  all.equal(t( fac2sparse(ff) ),
    sparse.model.matrix(~ 0+ff),
    tolerance = 0, check.attributes=FALSE),
  is(M <- fac2sparse(f30, drop= TRUE),"CsparseMatrix"), dim(M) == c(0, 0),
  is(M <- fac2sparse(f30, drop=FALSE),"CsparseMatrix"), dim(M) == c(3, 0),
  is(M <- fac2sparse(f12, drop= TRUE),"CsparseMatrix"), dim(M) == c(0,12),
  is(M <- fac2sparse(f12, drop=FALSE),"CsparseMatrix"), dim(M) == c(3,12)
)

```

sparseLU-class

*Sparse LU Factorizations***Description**

sparseLU is the class of sparse, row- and column-pivoted LU factorizations of $n \times n$ real matrices A , having the general form

$$P_1 A P_2 = LU$$

or (equivalently)

$$A = P_1' L U P_2'$$

where P_1 and P_2 are permutation matrices, L is a unit lower triangular matrix, and U is an upper triangular matrix.

Slots

Dim, Dimnames inherited from virtual class [MatrixFactorization](#).

L an object of class [dtCMatrix](#), the unit lower triangular L factor.

U an object of class [dtCMatrix](#), the upper triangular U factor.

p, q 0-based integer vectors of length Dim[1], specifying the permutations applied to the rows and columns of the factorized matrix. q of length 0 is valid and equivalent to the identity permutation, implying no column pivoting. Using R syntax, the matrix P_1AP_2 is precisely $A[p+1, q+1]$ ($A[p+1,]$ when q has length 0).

Extends

Class [LU](#), directly. Class [MatrixFactorization](#), by class [LU](#), distance 2.

Instantiation

Objects can be generated directly by calls of the form `new("sparseLU", ...)`, but they are more typically obtained as the value of `lu(x)` for x inheriting from [sparseMatrix](#) (often [dgCMatrix](#)).

Methods

determinant signature(from = "sparseLU", logarithm = "logical"): computes the determinant of the factorized matrix A or its logarithm.

expand signature(x = "sparseLU"): see [expand-methods](#).

expand1 signature(x = "sparseLU"): see [expand1-methods](#).

expand2 signature(x = "sparseLU"): see [expand2-methods](#).

solve signature(a = "sparseLU", b = .): see [solve-methods](#).

References

Davis, T. A. (2006). *Direct methods for sparse linear systems*. Society for Industrial and Applied Mathematics. doi:10.1137/1.9780898718881

Golub, G. H., & Van Loan, C. F. (2013). *Matrix computations* (4th ed.). Johns Hopkins University Press. doi:10.56021/9781421407944

See Also

Class [denseLU](#) for dense LU factorizations.

Class [dgCMatrix](#).

Generic functions [lu](#), [expand1](#) and [expand2](#).

Examples

```

showClass("sparseLU")
set.seed(2)

A <- as(readMM(system.file("external", "pores_1.mtx", package = "Matrix")),
        "CsparseMatrix")
(n <- A@Dim[1L])

## With dimnames, to see that they are propagated :
dimnames(A) <- dn <- list(paste0("r", seq_len(n)),
                        paste0("c", seq_len(n)))

(lu.A <- lu(A))
str(e.lu.A <- expand2(lu.A), max.level = 2L)

ae1 <- function(a, b, ...) all.equal(as(a, "matrix"), as(b, "matrix"), ...)
ae2 <- function(a, b, ...) ae1(unname(a), unname(b), ...)

## A ~ P1' L U P2' in floating point
stopifnot(exprs = {
  identical(names(e.lu.A), c("P1.", "L", "U", "P2."))
  identical(e.lu.A[["P1."],
            new("pMatrix", Dim = c(n, n), Dimnames = c(dn[1L], list(NULL)),
              margin = 1L, perm = invertPerm(lu.A@p, 0L, 1L)))
  identical(e.lu.A[["P2."],
            new("pMatrix", Dim = c(n, n), Dimnames = c(list(NULL), dn[2L]),
              margin = 2L, perm = invertPerm(lu.A@q, 0L, 1L)))
  identical(e.lu.A[["L"]], lu.A@L)
  identical(e.lu.A[["U"]], lu.A@U)
  ae1(A, with(e.lu.A, P1. %*% L %*% U %*% P2.))
  ae2(A[lu.A@p + 1L, lu.A@q + 1L], with(e.lu.A, L %*% U))
})

## Factorization handled as factorized matrix
b <- rnorm(n)
stopifnot(identical(det(A), det(lu.A)),
          identical(solve(A, b), solve(lu.A, b)))

```

sparseMatrix

*General Sparse Matrix Construction from Nonzero Entries***Description**

User-friendly construction of sparse matrices (inheriting from virtual [class CsparseMatrix](#), [RsparseMatrix](#), or [TsparseMatrix](#)) from the positions and values of their nonzero entries.

This interface is recommended over direct construction via calls such as `new(".[CRT]Matrix", ...)`.

Usage

```
sparseMatrix(i, j, p, x, dims, dimnames,
             symmetric = FALSE, triangular = FALSE, index1 = TRUE,
             repr = c("C", "R", "T"), giveCsparse,
             check = TRUE, use.last.ij = FALSE)
```

Arguments

<code>i, j</code>	integer vectors of equal length specifying the positions (row and column indices) of the nonzero (or non-TRUE) entries of the matrix. Note that, when <code>x</code> is non-missing, the x_k corresponding to <i>repeated</i> pairs (i_k, j_k) are <i>added</i> , for consistency with the definition of class <code>TsparseMatrix</code> , unless <code>use.last.ij</code> is TRUE, in which case only the <i>last</i> such x_k is used.
<code>p</code>	integer vector of pointers, one for each column (or row), to the initial (zero-based) index of elements in the column (or row). Exactly one of <code>i</code> , <code>j</code> , and <code>p</code> must be missing.
<code>x</code>	optional, typically nonzero values for the matrix entries. If specified, then the length must equal that of <code>i</code> (or <code>j</code>) or equal 1, in which case <code>x</code> is recycled as necessary. If missing, then the result is a nonzero pattern matrix, i.e., inheriting from class <code>nsparseMatrix</code> .
<code>dims</code>	optional length-2 integer vector of matrix dimensions. If missing, then <code>!index1+c(max(i), max(j))</code> is used.
<code>dimnames</code>	optional list of <code>dimnames</code> ; if missing, then <code>NULL</code> ones are used.
<code>symmetric</code>	logical indicating if the resulting matrix should be symmetric. In that case, (i, j, p) should specify only one triangle (upper or lower).
<code>triangular</code>	logical indicating if the resulting matrix should be triangular. In that case, (i, j, p) should specify only one triangle (upper or lower).
<code>index1</code>	logical. If TRUE (the default), then <code>i</code> and <code>j</code> are interpreted as 1-based indices, following the R convention. That is, counting of rows and columns starts at 1. If FALSE, then they are interpreted as 0-based indices.
<code>repr</code>	character string, one of "C", "R", and "T", specifying the representation of the sparse matrix result, i.e., specifying one of the virtual classes <code>CsparseMatrix</code> , <code>RsparseMatrix</code> , and <code>TsparseMatrix</code> .
<code>giveCsparse</code>	(deprecated, replaced by repr) logical indicating if the result should inherit from <code>CsparseMatrix</code> or <code>TsparseMatrix</code> . Note that operations involving <code>CsparseMatrix</code> are very often (but not always) more efficient.
<code>check</code>	logical indicating whether to check that the result is formally valid before returning. Do not set to FALSE unless you know what you are doing!
<code>use.last.ij</code>	logical indicating if, in the case of repeated (duplicated) pairs (i_k, j_k) , only the last pair should be used. FALSE (the default) is consistent with the definition of class <code>TsparseMatrix</code> .

Details

Exactly one of the arguments `i`, `j` and `p` must be missing.

In typical usage, `p` is missing, `i` and `j` are vectors of positive integers and `x` is a numeric vector. These three vectors, which must have the same length, form the triplet representation of the sparse matrix.

If `i` or `j` is missing then `p` must be a non-decreasing integer vector whose first element is zero. It provides the compressed, or “pointer” representation of the row or column indices, whichever is missing. The expanded form of `p`, `rep(seq_along(dp), dp)` where `dp <- diff(p)`, is used as the (1-based) row or column indices.

You cannot set both `singular` and `triangular` to `true`; rather use `Diagonal()` (or its alternatives, see there).

The values of `i`, `j`, `p` and `index1` are used to create 1-based index vectors `i` and `j` from which a `TsparseMatrix` is constructed, with numerical values given by `x`, if non-missing. Note that in that case, when some pairs (i_k, j_k) are repeated (aka “duplicated”), the corresponding x_k are *added*, in consistency with the definition of the `TsparseMatrix` class, unless `use.last.ij` is set to `true`.

By default, when `repr = "C"`, the `CsparseMatrix` derived from this triplet form is returned, where `repr = "R"` now allows to directly get an `RsparseMatrix` and `repr = "T"` leaves the result as `TsparseMatrix`.

The reason for returning a `CsparseMatrix` object instead of the triplet format by default is that the compressed column form is easier to work with when performing matrix operations. In particular, if there are no zeros in `x` then a `CsparseMatrix` is a unique representation of the sparse matrix.

Value

A sparse matrix, by default in compressed sparse column format and (formally) without symmetric or triangular structure, i.e., by default inheriting from both `CsparseMatrix` and `generalMatrix`.

Note

You *do* need to use `index1 = FALSE` (or add + 1 to `i` and `j`) if you want use the 0-based `i` (and `j`) slots from existing sparse matrices.

See Also

`Matrix(*, sparse=TRUE)` for the constructor of such matrices from a *dense* matrix. That is easier in small sample, but much less efficient (or impossible) for large matrices, where something like `sparseMatrix()` is needed. Further `bdiag` and `Diagonal` for (block-)diagonal and `bandSparse` for banded sparse matrix constructors.

Random sparse matrices via `rsparsematrix()`.

The standard `Rxtabs(*, sparse=TRUE)`, for sparse tables and `sparse.model.matrix()` for building sparse model matrices.

Consider `CsparseMatrix` and similar class definition help files.

Examples

```
## simple example
i <- c(1,3:8); j <- c(2,9,6:10); x <- 7 * (1:7)
(A <- sparseMatrix(i, j, x = x))          ## 8 x 10 "dgCMatrix"
summary(A)
```

```

str(A) # note that *internally* 0-based row indices are used

(sA <- sparseMatrix(i, j, x = x, symmetric = TRUE)) ## 10 x 10 "dsCMatrix"
(tA <- sparseMatrix(i, j, x = x, triangular= TRUE)) ## 10 x 10 "dtCMatrix"
stopifnot( all(sA == tA + t(tA)) ,
           identical(sA, as(tA + t(tA), "symmetricMatrix")))

## dims can be larger than the maximum row or column indices
(AA <- sparseMatrix(c(1,3:8), c(2,9,6:10), x = 7 * (1:7), dims = c(10,20)))
summary(AA)

## i, j and x can be in an arbitrary order, as long as they are consistent
set.seed(1); (perm <- sample(1:7))
(A1 <- sparseMatrix(i[perm], j[perm], x = x[perm]))
stopifnot(identical(A, A1))

## The slots are 0-index based, so
try( sparseMatrix(i=A@i, p=A@p, x= seq_along(A@x)) )
## fails and you should say so: 1-indexing is FALSE:
    sparseMatrix(i=A@i, p=A@p, x= seq_along(A@x), index1 = FALSE)

## the (i,j) pairs can be repeated, in which case the x's are summed
(args <- data.frame(i = c(i, 1), j = c(j, 2), x = c(x, 2)))
(Aa <- do.call(sparseMatrix, args))
## explicitly ask for elimination of such duplicates, so
## that the last one is used:
(A. <- do.call(sparseMatrix, c(args, list(use.last.ij = TRUE))))
stopifnot(Aa[1,2] == 9, # 2+7 == 9
          A.[1,2] == 2) # 2 was *after* 7

## for a pattern matrix, of course there is no "summing":
(nA <- do.call(sparseMatrix, args[c("i","j")]))

dn <- list(LETTERS[1:3], letters[1:5])
## pointer vectors can be used, and the (i,x) slots are sorted if necessary:
m <- sparseMatrix(i = c(3,1, 3:2, 2:1), p= c(0:2, 4,4,6), x = 1:6, dimnames = dn)
m
str(m)
stopifnot(identical(dimnames(m), dn))

sparseMatrix(x = 2.72, i=1:3, j=2:4) # recycling x
sparseMatrix(x = TRUE, i=1:3, j=2:4) # recycling x, |--> "lgCMatrix"

## no 'x' --> patter*n* matrix:
(n <- sparseMatrix(i=1:6, j=rev(2:7)))# -> ngCMatrix

## an empty sparse matrix:
(e <- sparseMatrix(dims = c(4,6), i={}, j={}))

## a symmetric one:
(sy <- sparseMatrix(i= c(2,4,3:5), j= c(4,7:5,5), x = 1:5,
                    dims = c(7,7), symmetric=TRUE))
stopifnot(isSymmetric(sy),

```

```

        identical(sy, ## switch i <-> j {and transpose }
t( sparseMatrix(j= c(2,4,3:5), i= c(4,7:5,5), x = 1:5,
              dims = c(7,7), symmetric=TRUE))))

## rsparsematrix() calls sparseMatrix() :
M1 <- rsparsematrix(1000, 20, nnz = 200)
summary(M1)

## pointers example in converting from other sparse matrix representations.
if(requireNamespace("SparseM") &&
  packageVersion("SparseM") >= "0.87" &&
  nzchar(dfil <- system.file("extdata", "rua_32_ax.rua", package = "SparseM"))) {
  X <- SparseM::model.matrix(SparseM::read.matrix.hb(dfil))
  XX <- sparseMatrix(j = X@ja, p = X@ia - 1L, x = X@ra, dims = X@dimension)
  validObject(XX)

  ## Alternatively, and even more user friendly :
  X. <- as(X, "Matrix") # or also
  X2 <- as(X, "sparseMatrix")
  stopifnot(identical(XX, X.), identical(X., X2))
}

```

sparseMatrix-class *Virtual Class "sparseMatrix" — Mother of Sparse Matrices*

Description

Virtual Mother Class of All Sparse Matrices

Slots

Dim: Object of class "integer" - the dimensions of the matrix - must be an integer vector with exactly two non-negative values.

Dimnames: a list of length two - inherited from class Matrix, see [Matrix](#).

Extends

Class "Matrix", directly.

Methods

show (object = "sparseMatrix"): The [show](#) method for sparse matrices prints "structural" zeroes as "." using [printSpMatrix\(\)](#) which allows further customization.

print signature(x = "sparseMatrix"), ...

The [print](#) method for sparse matrices by default is the same as [show\(\)](#) but can be called with extra optional arguments, see [printSpMatrix\(\)](#).

format signature(x = "sparseMatrix"), ...

The [format](#) method for sparse matrices, see [formatSpMatrix\(\)](#) for details such as the extra optional arguments.

summary (object = "sparseMatrix", uniqT=FALSE): Returns an object of S3 class "sparseSummary" which is basically a `data.frame` with columns (i, j, x) (or just (i, j) for `nsparseMatrix` class objects) with the stored (typically non-zero) entries. The `print` method resembles Matlab's way of printing sparse matrices, and also the MatrixMarket format, see `writeMM`.

cbind2 (x = *, y = *): several methods for binding matrices together, column-wise, see the basic `cbind` and `rbind` functions.

Note that the result will typically be sparse, even when one argument is dense and larger than the sparse one.

rbind2 (x = *, y = *): binding matrices together row-wise, see `cbind2` above.

determinant (x = "sparseMatrix", logarithm=TRUE): `determinant()` methods for sparse matrices typically work via `Cholesky` or `lu` decompositions.

diag (x = "sparseMatrix"): extracts the diagonal of a sparse matrix.

dim<- signature(x = "sparseMatrix", value = "ANY"): allows to *reshape* a sparse matrix to a sparse matrix with the same entries but different dimensions. `value` must be of length two and fulfill `prod(value) == prod(dim(x))`.

coerce signature(from = "factor", to = "sparseMatrix"): Coercion of a factor to "sparseMatrix" produces the matrix of indicator **rows** stored as an object of class "dgCMatrix". To obtain columns representing the interaction of the factor and a numeric covariate, replace the "x" slot of the result by the numeric covariate then take the transpose. Missing values (NA) from the factor are translated to columns of all 0s.

See also `colSums`, `norm`, ... for methods with separate help pages.

Note

In method selection for multiplication operations (i.e. `%*%` and the two-argument form of `crossprod`) the `sparseMatrix` class takes precedence in the sense that if one operand is a sparse matrix and the other is any type of dense matrix then the dense matrix is coerced to a `dgeMatrix` and the appropriate sparse matrix method is used.

See Also

`sparseMatrix`, and its references, such as `xtabs(*, sparse=TRUE)`, or `sparse.model.matrix()`, for constructing sparse matrices.

`T2graph` for conversion of "graph" objects (package **graph**) to and from sparse matrices.

Examples

```
showClass("sparseMatrix") ## and look at the help() of its subclasses
M <- Matrix(0, 10000, 100)
M[1,1] <- M[2,3] <- 3.14
M ## show(.) method suppresses printing of the majority of rows

data(CAex, package = "Matrix")
dim(CAex) # 72 x 72 matrix
determinant(CAex) # works via sparse lu(.)

## factor -> t( <sparse design matrix> ) :
(fact <- gl(5, 3, 30, labels = LETTERS[1:5]))
```



```
(Xt <- as(fact, "sparseMatrix")) # indicator rows

## missing values --> all-0 columns:
f.mis <- fact
i.mis <- c(3:5, 17)
is.na(f.mis) <- i.mis
Xt != (X. <- as(f.mis, "sparseMatrix")) # differ only in columns 3:5,17
stopifnot(all(X.[,i.mis] == 0), all(Xt[,-i.mis] == X.[,-i.mis]))
```

 sparseQR-class

Sparse QR Factorizations

Description

sparseQR is the class of sparse, row- and column-pivoted QR factorizations of $m \times n$ ($m \geq n$) real matrices, having the general form

$$P_1 A P_2 = Q R = \begin{bmatrix} Q_1 & Q_2 \end{bmatrix} \begin{bmatrix} R_1 \\ 0 \end{bmatrix} = Q_1 R_1$$

or (equivalently)

$$A = P_1' Q R P_2' = P_1' \begin{bmatrix} Q_1 & Q_2 \end{bmatrix} \begin{bmatrix} R_1 \\ 0 \end{bmatrix} P_2' = P_1' Q_1 R_1 P_2'$$

where P_1 and P_2 are permutation matrices, $Q = \prod_{j=1}^n H_j$ is an $m \times m$ orthogonal matrix (Q_1 contains the first n column vectors) equal to the product of n Householder matrices H_j , and R is an $m \times n$ upper trapezoidal matrix (R_1 contains the first n row vectors and is upper *triangular*).

Usage

```
qrR(qr, complete = FALSE, backPermute = TRUE, row.names = TRUE)
```

Arguments

qr	an object of class <code>sparseQR</code> , almost always the result of a call to generic function <code>qr</code> with sparse <code>x</code> .
complete	a logical indicating if R should be returned instead of R_1 .
backPermute	a logical indicating if R or R_1 should be multiplied on the right by P_2' .
row.names	a logical indicating if <code>dimnames(qr)[1]</code> should be propagated unpermuted to the result. If <code>complete = FALSE</code> , then only the first n names are kept.

Details

The method for `qr.Q` does not return Q but rather the (also orthogonal) product $P_1'Q$. This behaviour is algebraically consistent with the **base** implementation (see `qr`), which can be seen by noting that `qr.default` in **base** does not pivot rows, constraining P_1 to be an identity matrix. It follows that `qr.Q(qr.default(x))` also returns $P_1'Q$.

Similarly, the methods for `qr.qy` and `qr.qty` multiply on the left by $P_1'Q$ and $Q'P_1$ rather than Q and Q' .

It is wrong to expect the values of `qr.Q` (or `qr.R`, `qr.qy`, `qr.qty`) computed from “equivalent” sparse and dense factorizations (say, `qr(x)` and `qr(as(x, "matrix"))`) for x of class `dgCMatrix` to compare equal. The underlying factorization algorithms are quite different, notably as they employ different pivoting strategies, and in general the factorization is not unique even for fixed P_1 and P_2 .

On the other hand, the values of `qr.X`, `qr.coef`, `qr.fitted`, and `qr.resid` are well-defined, and in those cases the sparse and dense computations *should* compare equal (within some tolerance).

The method for `qr.R` is a simple wrapper around `qrR`, but not back-permuting by default and never giving row names. It did not support `backPermute = TRUE` until **Matrix** 1.6-0, hence code needing the back-permuted result should call `qrR` if **Matrix** \geq 1.6-0 is not known.

Slots

`Dim`, `Dimnames` inherited from virtual class `MatrixFactorization`.

`beta` a numeric vector of length `Dim[2]`, used to construct Householder matrices; see V below.

V an object of class `dgCMatrix` with `Dim[2]` columns. The number of rows `nrow(V)` is at least `Dim[1]` and at most `Dim[1]+Dim[2]`. V is lower trapezoidal, and its column vectors generate the Householder matrices H_j that compose the orthogonal Q factor. Specifically, H_j is constructed as `diag(Dim[1]) - beta[j] * tcrossprod(V[, j])`.

R an object of class `dgCMatrix` with `nrow(V)` rows and `Dim[2]` columns. R is the upper trapezoidal R factor.

`p`, `q` 0-based integer vectors of length `nrow(V)` and `Dim[2]`, respectively, specifying the permutations applied to the rows and columns of the factorized matrix. `q` of length 0 is valid and equivalent to the identity permutation, implying no column pivoting. Using R syntax, the matrix P_1AP_2 is precisely `A[p+1, q+1]` (`A[p+1,]` when `q` has length 0).

Extends

Class `QR`, directly. Class `MatrixFactorization`, by class `QR`, distance 2.

Instantiation

Objects can be generated directly by calls of the form `new("sparseQR", ...)`, but they are more typically obtained as the value of `qr(x)` for x inheriting from `sparseMatrix` (often `dgCMatrix`).

Methods

`determinant` `signature(from = "sparseQR", logarithm = "logical")`: computes the determinant of the factorized matrix A or its logarithm.

`expand1` `signature(x = "sparseQR")`: see [expand1-methods](#).

- `expand2` signature(`x = "sparseQR"`): see [expand2-methods](#).
- `qr.Q` signature(`qr = "sparseQR"`): returns as a [dgeMatrix](#) either $P_1'Q$ or $P_1'Q_1$, depending on optional argument `complete`. The default is `FALSE`, indicating $P_1'Q_1$.
- `qr.R` signature(`qr = "sparseQR"`): `qrR` returns R , R_1 , RP_2' , or R_1P_2' , depending on optional arguments `complete` and `backPermute`. The default in both cases is `FALSE`, indicating R_1 , for compatibility with **base**. The class of the result in that case is [dtCMatrix](#). In the other three cases, it is [dgCMatrix](#).
- `qr.X` signature(`qr = "sparseQR"`): returns A as a [dgeMatrix](#), by default. If $m > n$ and optional argument `ncol` is greater than n , then the result is augmented with $P_1'QJ$, where J is composed of columns $(n + 1)$ through `ncol` of the $m \times m$ identity matrix.
- `qr.coef` signature(`qr = "sparseQR"`, `y = .`): returns as a [dgeMatrix](#) or vector the result of multiplying `y` on the left by $P_2R_1^{-1}Q_1'P_1$.
- `qr.fitted` signature(`qr = "sparseQR"`, `y = .`): returns as a [dgeMatrix](#) or vector the result of multiplying `y` on the left by $P_1'Q_1Q_1'P_1$.
- `qr.resid` signature(`qr = "sparseQR"`, `y = .`): returns as a [dgeMatrix](#) or vector the result of multiplying `y` on the left by $P_1'Q_2Q_2'P_1$.
- `qr.qty` signature(`qr = "sparseQR"`, `y = .`): returns as a [dgeMatrix](#) or vector the result of multiplying `y` on the left by $Q'P_1$.
- `qr.qy` signature(`qr = "sparseQR"`, `y = .`): returns as a [dgeMatrix](#) or vector the result of multiplying `y` on the left by $P_1'Q$.
- `solve` signature(`a = "sparseQR"`, `b = .`): see [solve-methods](#).

References

- Davis, T. A. (2006). *Direct methods for sparse linear systems*. Society for Industrial and Applied Mathematics. doi:10.1137/1.9780898718881
- Golub, G. H., & Van Loan, C. F. (2013). *Matrix computations* (4th ed.). Johns Hopkins University Press. doi:10.56021/9781421407944

See Also

- Class [dgCMatrix](#).
- Generic function `qr` from **base**, whose default method `qr.default` “defines” the S3 class `qr` of dense QR factorizations.
- [qr-methods](#) for methods defined in **Matrix**.
- Generic functions `expand1` and `expand2`.
- The many auxiliary functions for QR factorizations: [qr.Q](#), [qr.R](#), [qr.X](#), [qr.coef](#), [qr.fitted](#), [qr.resid](#), [qr.qty](#), [qr.qy](#), and [qr.solve](#).

Examples

```
showClass("sparseQR")
set.seed(2)

m <- 300L
```

```

n <- 60L
A <- rsparsematrix(m, n, 0.05)

## With dimnames, to see that they are propagated :
dimnames(A) <- dn <- list(paste0("r", seq_len(m)),
                          paste0("c", seq_len(n)))

(qr.A <- qr(A))
str(e.qr.A <- expand2(qr.A, complete = FALSE), max.level = 2L)
str(E.qr.A <- expand2(qr.A, complete = TRUE), max.level = 2L)

t(sapply(e.qr.A, dim))
t(sapply(E.qr.A, dim))

## Horribly inefficient, but instructive :
slowQ <- function(V, beta) {
  d <- dim(V)
  Q <- diag(d[1L])
  if(d[2L] > 0L) {
    for(j in d[2L]:1L) {
      cat(j, "\n", sep = "")
      Q <- Q - (beta[j] * tcrossprod(V[, j])) %*% Q
    }
  }
  Q
}

ae1 <- function(a, b, ...) all.equal(as(a, "matrix"), as(b, "matrix"), ...)
ae2 <- function(a, b, ...) ae1(unname(a), unname(b), ...)

##  $A \sim P1' Q R P2' \sim P1' Q1 R1 P2'$  in floating point
stopifnot(exprs = {
  identical(names(e.qr.A), c("P1.", "Q1", "R1", "P2.))
  identical(names(E.qr.A), c("P1.", "Q", "R", "P2.))
  identical(e.qr.A[["P1."]],
            new("pMatrix", Dim = c(m, m), Dimnames = c(dn[1L], list(NULL)),
              margin = 1L, perm = invertPerm(qr.A@p, 0L, 1L)))
  identical(e.qr.A[["P2."]],
            new("pMatrix", Dim = c(n, n), Dimnames = c(list(NULL), dn[2L]),
              margin = 2L, perm = invertPerm(qr.A@q, 0L, 1L)))
  identical(e.qr.A[["R1"]], triu(E.qr.A[["R"]][seq_len(n), ]))
  identical(e.qr.A[["Q1"]], E.qr.A[["Q"]][, seq_len(n)])
  identical(E.qr.A[["R"]], qr.A@R)
  ## ae1(E.qr.A[["Q"]], slowQ(qr.A@V, qr.A@beta))
  ae1(crossprod(E.qr.A[["Q"]], diag(m))
    ae1(A, with(e.qr.A, P1. %*% Q1 %*% R1 %*% P2.))
    ae1(A, with(E.qr.A, P1. %*% Q %*% R %*% P2.))
    ae2(A.perm <- A[qr.A@p + 1L, qr.A@q + 1L], with(e.qr.A, Q1 %*% R1))
    ae2(A.perm , with(E.qr.A, Q %*% R ))
})

## More identities
b <- rnorm(m)

```

```

stopifnot(exprs = {
  ae1(qrX <- qr.X      (qr.A  ), A)
  ae2(qrQ <- qr.Q      (qr.A  ), with(e.qr.A, P1. %*% Q1))
  ae2(      qr.R      (qr.A  ), with(e.qr.A, R1))
  ae2(qrc <- qr.coef  (qr.A, b), with(e.qr.A, solve(R1 %*% P2., t(qrQ)) %*% b))
  ae2(qrf <- qr.fitted(qr.A, b), with(e.qr.A, tcrossprod(qrQ) %*% b))
  ae2(qrr <- qr.resid (qr.A, b), b - qrf)
  ae2(qrq <- qr.qy    (qr.A, b), with(E.qr.A, P1. %*% Q %*% b))
  ae2(qr.qty(qr.A, qrq), b)
})

## Sparse and dense computations should agree here
qr.Am <- qr(as(A, "matrix")) # <=> qr.default(A)
stopifnot(exprs = {
  ae2(qrX, qr.X      (qr.Am  ))
  ae2(qrc, qr.coef  (qr.Am, b))
  ae2(qrf, qr.fitted(qr.Am, b))
  ae2(qrr, qr.resid (qr.Am, b))
})

```

sparseVector

Sparse Vector Construction from Nonzero Entries

Description

User friendly construction of sparse vectors, i.e., objects inheriting from [class sparseVector](#), from indices and values of its non-zero entries.

Usage

```
sparseVector(x, i, length)
```

Arguments

x	vector of the non zero entries; may be missing in which case a "nsparseVector" will be returned.
i	integer vector (of the same length as x) specifying the indices of the non-zero (or non-TRUE) entries of the sparse vector.
length	length of the sparse vector.

Details

zero entries in x are dropped automatically, analogously as [drop0\(\)](#) acts on sparse matrices.

Value

a sparse vector, i.e., inheriting from [class sparseVector](#).

Author(s)

Martin Maechler

See Also[sparseMatrix\(\)](#) constructor for sparse matrices; the class [sparseVector](#).**Examples**

```
str(sv <- sparseVector(x = 1:10, i = sample(999, 10), length=1000))

sx <- c(0,0,3, 3.2, 0,0,0,-3:1,0,0,2,0,0,5,0,0)
ss <- as(sx, "sparseVector")
stopifnot(identical(ss,
  sparseVector(x = c(2, -1, -2, 3, 1, -3, 5, 3.2),
    i = c(15L, 10:9, 3L,12L,8L,18L, 4L), length = 20L)))

(ns <- sparseVector(i= c(7, 3, 2), length = 10))
stopifnot(identical(ns,
  new("nsparseVector", length = 10, i = c(2, 3, 7))))
```

sparseVector-class *Sparse Vector Classes*

Description

Sparse Vector Classes: The virtual mother class "sparseVector" has the five actual daughter classes "dsparseVector", "isparseVector", "lsparseVector", "nsparseVector", and "zsparseVector", where we've mainly implemented methods for the d*, l* and n* ones.

Slots

length: class "numeric" - the [length](#) of the sparse vector. Note that "numeric" can be considerably larger than the maximal "integer", `.Machine$integer.max`, on purpose.

i: class "numeric" - the (1-based) indices of the non-zero entries. Must *not* be NA and strictly sorted increasingly.

Note that "integer" is "part of" "numeric", and can (and often will) be used for non-huge sparseVectors.

x: (for all but "nsparseVector"): the non-zero entries. This is of class "numeric" for class "dsparseVector", "logical" for class "lsparseVector", etc.

Methods

length signature(x = "sparseVector"): simply extracts the length slot.

show signature(object = "sparseVector"): The **show** method for sparse vectors prints “*structural*” zeroes as “.” using the non-exported `prSpVector` function which allows further customization such as replacing “.” by “ ” (blank).

Note that `options(max.print)` will influence how many entries of large sparse vectors are printed at all.

as.vector signature(x = "sparseVector", mode = "character") coerces sparse vectors to “regular”, i.e., atomic vectors. This is the same as `as(x, "vector")`.

as ..: see coerce below

coerce signature(from = "sparseVector", to = "sparseMatrix"), and

coerce signature(from = "sparseMatrix", to = "sparseVector"), etc: coercions to and from sparse matrices (`sparseMatrix`) are provided and work analogously as in standard R, i.e., a vector is coerced to a 1-column matrix.

dim<- signature(x = "sparseVector", value = "integer") coerces a sparse vector to a sparse Matrix, i.e., an object inheriting from `sparseMatrix`, of the appropriate dimension.

head signature(x = "sparseVector"): as with R’s (package `util`) `head`, `head(x, n)` (for $n \geq 1$) is equivalent to `x[1:n]`, but here can be much more efficient, see the example.

tail signature(x = "sparseVector"): analogous to `head`, see above.

toeplitz signature(x = "sparseVector"): as `toeplitz(x)`, produce the $n \times n$ Toeplitz matrix from `x`, where $n = \text{length}(x)$.

rep signature(x = "sparseVector") repeat `x`, with the same argument list (`x`, `times`, `length.out`, `each`, ...) as the default method for `rep()`.

which signature(x = "nsparseVector") and

which signature(x = "lsparseVector") return the indices of the non-zero entries (which is trivial for sparse vectors).

Ops signature(e1 = "sparseVector", e2 = "*"): define arithmetic, compare and logic operations, (see `Ops`).

Summary signature(x = "sparseVector"): define all the `Summary` methods.

is.na, is.finite, is.infinite (x = "sparseVector"), and

is.na, is.finite, is.infinite (x = "nsparseVector"): return `logical` or “nsparseVector” of the same length as `x`, indicating if/where `x` is `NA` (or `NaN`), finite or infinite, entirely analogously to the corresponding base R functions.

zapsmall signature(x = "sparseVectors"): typically used for numeric sparse vector: `round()` entries such that (relatively) very small entries become zero exactly.

`c.sparseVector()` is an S3 method for all “sparseVector”s, but automatic dispatch only happens for the first argument, so it is useful also as regular R function, see the examples.

See Also

`sparseVector()` for friendly construction of sparse vectors (apart from `as(*, "sparseVector")`).

Examples

```

getClass("sparseVector")
getClass("dsparseVector")

sx <- c(0,0,3, 3.2, 0,0,0,-3:1,0,0,2,0,0,5,0,0)
(ss <- as(sx, "sparseVector"))

ix <- as.integer(round(sx))
(is <- as(ix, "sparseVector")) ## an "isparseVector" (!)
(ns <- sparseVector(i= c(7, 3, 2), length = 10)) # "nsparseVector"
## rep() works too:
(ri <- rep(is, length.out= 25))

## Using `dim<-` as in base R :
r <- ss
dim(r) <- c(4,5) # becomes a sparse Matrix:
r
## or coercion (as as.matrix() in base R):
as(ss, "Matrix")
stopifnot(all(ss == print(as(ss, "CsparseMatrix"))))

## currently has "non-structural" FALSE -- printing as ":"
(lis <- is & FALSE)
(nn <- is[is == 0]) # all "structural" FALSE

## NA-case
sN <- sx; sN[4] <- NA
(svN <- as(sN, "sparseVector"))

v <- as(c(0,0,3, 3.2, rep(0,9),-3,0,-1, rep(0,20),5,0),
        "sparseVector")
v <- rep(rep(v, 50), 5000)
set.seed(1); v[sample(v@i, 1e6)] <- 0
str(v)
system.time(for(i in 1:4) hv <- head(v, 1e6))
## user system elapsed
## 0.033 0.000 0.032
system.time(for(i in 1:4) h2 <- v[1:1e6])
## user system elapsed
## 1.317 0.000 1.319

stopifnot(identical(hv, h2),
          identical(is | FALSE, is != 0),
          validObject(svN), validObject(lis), as.logical(is.na(svN[4])),
          identical(is^2 > 0, is & TRUE),
          all(!lis), !any(lis), length(nn@i) == 0, !any(nn), all(!nn),
          sum(lis) == 0, !prod(lis), range(lis) == c(0,0))

## create and use the t(.) method:
t(x20 <- sparseVector(c(9,3:1), i=c(1:2,4,7), length=20))
(T20 <- toeplitz(x20))
stopifnot(is(T20, "symmetricMatrix"), is(T20, "sparseMatrix"),

```



```

        identical(unnamed(as.matrix(T20)),
                  toeplitz(as.vector(x20))))

## c() method for "sparseVector" - also available as regular function
(c1 <- c(x20, 0,0,0, -10*x20))
(c2 <- c(ns, is, FALSE))
(c3 <- c(ns, !ns, TRUE, NA, FALSE))
(c4 <- c(ns, rev(ns)))
## here, c() would produce a list {not dispatching to c.sparseVector()}
(c5 <- c.sparseVector(0,0, x20))

## checking (consistency)
.v <- as.vector
.s <- function(v) as(v, "sparseVector")
stopifnot(exprs = {
  all.equal(c1, .s(c(.v(x20), 0,0,0, -10*.v(x20))), tol = 0)
  all.equal(c2, .s(c(.v(ns), .v(is), FALSE)), tol = 0)
  all.equal(c3, .s(c(.v(ns), !.v(ns), TRUE, NA, FALSE)), tol = 0)
  all.equal(c4, .s(c(.v(ns), rev(.v(ns)))), tol = 0,
             check.class = FALSE)
  all.equal(c5, .s(c(0,0, .v(x20))), tol = 0)
})

```

spMatrix

*Sparse Matrix Constructor From Triplet***Description**

User friendly construction of a sparse matrix (inheriting from class `TsparseMatrix`) from the triplet representation.

This is much less flexible than `sparseMatrix()` and hence somewhat *deprecated*.

Usage

```
spMatrix(nrow, ncol, i = integer(0L), j = integer(0L), x = double(0L))
```

Arguments

nrow, ncol	integers specifying the desired number of rows and columns.
i, j	integer vectors of the same length specifying the locations of the non-zero (or non-TRUE) entries of the matrix.
x	atomic vector of the same length as i and j, specifying the values of the non-zero entries.

Value

A sparse matrix in triplet form, as an R object inheriting from both `TsparseMatrix` and `generalMatrix`.

The matrix M will have $M[i[k], j[k]] == x[k]$, for $k = 1, 2, \dots, n$, where $n = \text{length}(i)$ and $M[i', j'] == 0$ for all other pairs (i', j') .

See Also

`Matrix(*, sparse=TRUE)` for the more usual constructor of such matrices. Then, `sparseMatrix` is more general and flexible than `spMatrix()` and by default returns a `CsparseMatrix` which is often slightly more desirable. Further, `bdiag` and `Diagonal` for (block-)diagonal matrix constructors.

Consider `TsparseMatrix` and similar class definition help files.

Examples

```
## simple example
A <- spMatrix(10,20, i = c(1,3:8),
              j = c(2,9,6:10),
              x = 7 * (1:7))
A # a "dgTMatrix"
summary(A)
str(A) # note that *internally* 0-based indices (i,j) are used

L <- spMatrix(9, 30, i = rep(1:9, 3), 1:27,
             (1:27) %% 4 != 1)
L # an "lgTMatrix"

## A simplified predecessor of Matrix' rsparsematrix() function :

rSpMatrix <- function(nrow, ncol, nnz,
                     rand.x = function(n) round(rnorm(nnz), 2))
{
  ## Purpose: random sparse matrix
  ## -----
  ## Arguments: (nrow,ncol): dimension
  ##           nnz : number of non-zero entries
  ##           rand.x: random number generator for 'x' slot
  ## -----
  ## Author: Martin Maechler, Date: 14.-16. May 2007
  stopifnot((nnz <- as.integer(nnz)) >= 0,
            nrow >= 0, ncol >= 0, nnz <= nrow * ncol)
  spMatrix(nrow, ncol,
           i = sample(nrow, nnz, replace = TRUE),
           j = sample(ncol, nnz, replace = TRUE),
           x = rand.x(nnz))
}

M1 <- rSpMatrix(100000, 20, nnz = 200)
summary(M1)
```

Description

Methods for "[<-", i.e., extraction or subsetting mostly of matrices, in package **Matrix**.

Note: Contrary to standard `matrix` assignment in base R, in `x[. .] <- val` it is typically an **error** (see `stop`) when the `type` or `class` of `val` would require the class of `x` to be changed, e.g., when `x` is logical, say `"lsparseMatrix"`, and `val` is numeric. In other cases, e.g., when `x` is a `"nsparseMatrix"` and `val` is not `TRUE` or `FALSE`, a warning is signalled, and `val` is "interpreted" as `logical`, and (logical) `NA` is interpreted as `TRUE`.

Methods

There are *many many* more than these:

`x = "Matrix", i = "missing", j = "missing", value = "ANY"` is currently a simple fallback method implementation which ensures "readable" error messages.

`x = "Matrix", i = "ANY", j = "ANY", value = "ANY"` currently gives an error

`x = "denseMatrix", i = "index", j = "missing", value = "numeric" ...`

`x = "denseMatrix", i = "index", j = "index", value = "numeric" ...`

`x = "denseMatrix", i = "missing", j = "index", value = "numeric" ...`

See Also

[\[-methods](#) for subsetting "Matrix" objects; the [index](#) class; [Extract](#) about the standard subset assignment (and extraction).

Examples

```
set.seed(101)
(a <- m <- Matrix(round(rnorm(7*4),2), nrow = 7))

a[] <- 2.2 # <<- replaces **every** entry
a
## as do these:
a[,] <- 3 ; a[TRUE,] <- 4

m[2, 3] <- 3.14 # simple number
m[3, 3:4] <- 3:4 # simple numeric of length 2

## sub matrix assignment:
m[-(4:7), 3:4] <- cbind(1,2:4) #-> upper right corner of 'm'
m[3:5, 2:3] <- 0
m[6:7, 1:2] <- Diagonal(2)
m

## rows or columns only:
m[1,] <- 10
m[,2] <- 1:7
m[-(1:6), ] <- 3:0 # not the first 6 rows, i.e. only the 7th
as(m, "sparseMatrix")
```

subscript-methods *Methods for "[": Extraction or Subsetting in Package 'Matrix'*

Description

Methods for "[", i.e., extraction or subsetting mostly of matrices, in package **Matrix**.

Methods

There are more than these:

```
x = "Matrix", i = "missing", j = "missing", drop = "ANY" ...
x = "Matrix", i = "numeric", j = "missing", drop = "missing" ...
x = "Matrix", i = "missing", j = "numeric", drop = "missing" ...
x = "dsparseMatrix", i = "missing", j = "numeric", drop = "logical" ...
x = "dsparseMatrix", i = "numeric", j = "missing", drop = "logical" ...
x = "dsparseMatrix", i = "numeric", j = "numeric", drop = "logical" ...
```

See Also

[\[<--methods](#) for subassignment to "Matrix" objects. [Extract](#) about the standard extraction.

Examples

```
str(m <- Matrix(round(rnorm(7*4),2), nrow = 7))
stopifnot(identical(m, m[]))
m[2, 3] # simple number
m[2, 3:4] # simple numeric of length 2
m[2, 3:4, drop=FALSE] # sub matrix of class 'dgeMatrix'
## rows or columns only:
m[1,] # first row, as simple numeric vector
m[,1:2] # sub matrix of first two columns

showMethods("[", inherited = FALSE)
```

symmetricMatrix-class *Virtual Class of Symmetric Matrices in Package Matrix*

Description

The virtual class of symmetric matrices, "symmetricMatrix", from the package **Matrix** contains numeric and logical, dense and sparse matrices, e.g., see the examples with the "actual" subclasses.

The main use is in methods (and C functions) that can deal with all symmetric matrices, and in `as(*, "symmetricMatrix")`.

Slots

Dim, **Dimnames** inherited from virtual class [Matrix](#). See comments below about symmetry of **Dimnames**.

factors a list of [MatrixFactorization](#) objects caching factorizations of the matrix. Typically, it is initialized as an empty list and updated “automagically” whenever a factorization is computed.

uplo a character string, either “U” or “L” indicating that only entries in the upper or lower triangle are referenced.

Extends

Class “Matrix”, directly.

Methods

dimnames signature(object = “symmetricMatrix”): returns *symmetric dimnames*, even when the **Dimnames** slot only has row or column names. This allows to save storage for large (typically sparse) symmetric matrices.

isSymmetric signature(object = “symmetricMatrix”): returns TRUE trivially.

There’s a C function `symmetricMatrix_validate()` called by the internal validity checking functions, and also from `getValidity(getClass(“symmetricMatrix”))`.

Validity and dimnames

The validity checks do not require a symmetric **Dimnames** slot, so it can be `list(NULL, <character>)`, e.g., for efficiency. However, `dimnames()` and other functions and methods should behave as if the **dimnames** were symmetric, i.e., with both list components identical.

See Also

[isSymmetric](#) which has efficient methods ([isSymmetric-methods](#)) for the **Matrix** classes. Classes [triangularMatrix](#), and, e.g., [dsyMatrix](#) for numeric *dense* matrices, or [lsCMatrix](#) for a logical *sparse* matrix class.

Examples

```
## An example about the symmetric Dimnames:
sy <- sparseMatrix(i= c(2,4,3:5), j= c(4,7:5,5), x = 1:5, dims = c(7,7),
                  symmetric=TRUE, dimnames = list(NULL, letters[1:7]))
sy # shows symmetrical dimnames
sy@Dimnames # internally only one part is stored
dimnames(sy) # both parts - as sy *is* symmetrical

showClass(“symmetricMatrix”)

## The names of direct subclasses:
scl <- getClass(“symmetricMatrix”)@subclasses
directly <- sapply(lapply(scl, slot, “by”), length) == 0
names(scl)[directly]
```

```
## Methods -- applicable to all subclasses above:
showMethods(classes = "symmetricMatrix")
```

 symmpart-methods

Symmetric Part and Skew(symmetric) Part of a Matrix

Description

`symmpart(x)` computes the symmetric part $(x + t(x))/2$ and `skewpart(x)` the skew symmetric part $(x - t(x))/2$ of a square matrix `x`, more efficiently for specific Matrix classes.

Note that $x == \text{symmpart}(x) + \text{skewpart}(x)$ for all square matrices – apart from extraneous NA values in the RHS.

Usage

```
symmpart(x)
skewpart(x)
```

Arguments

`x` a *square* matrix; either “traditional” of class “matrix”, or typically, inheriting from the `Matrix` class.

Details

These are generic functions with several methods for different matrix classes, use e.g., `showMethods(symmpart)` to see them.

If the row and column names differ, the result will use the column names unless they are (partly) NULL where the row names are non-NULL (see also the examples).

Value

`symmpart(x)` returns a symmetric matrix, inheriting from `symmetricMatrix` or `diagonalMatrix` if `x` inherits from `Matrix`.

`skewpart(x)` returns a skew-symmetric matrix, inheriting from `generalMatrix`, `symmetricMatrix` or `diagonalMatrix` if `x` inherits from `Matrix`.

See Also

`isSymmetric`.

Examples

```

m <- Matrix(1:4, 2,2)
symmpart(m)
skewpart(m)

stopifnot(all(m == symmpart(m) + skewpart(m)))

dn <- dimnames(m) <- list(row = c("r1", "r2"), col = c("var.1", "var.2"))
stopifnot(all(m == symmpart(m) + skewpart(m)))
colnames(m) <- NULL
stopifnot(all(m == symmpart(m) + skewpart(m)))
dimnames(m) <- unname(dn)
stopifnot(all(m == symmpart(m) + skewpart(m)))

## investigate the current methods:
showMethods(skewpart, include = TRUE)

```

triangularMatrix-class

Virtual Class of Triangular Matrices in Package Matrix

Description

The virtual class of triangular matrices, "triangularMatrix", the package **Matrix** contains *square* (`nrow == ncol`) numeric and logical, dense and sparse matrices, e.g., see the examples. A main use of the virtual class is in methods (and C functions) that can deal with all triangular matrices.

Slots

uplo: String (of class "character"). Must be either "U", for upper triangular, and "L", for lower triangular.

diag: String (of class "character"). Must be either "U", for unit triangular (diagonal is all ones), or "N" for non-unit. The diagonal elements are not accessed internally when `diag` is "U". For [denseMatrix](#) classes, they need to be allocated though, such that the length of the x slot does not depend on `diag`.

Dim, Dimnames: The dimension (a length-2 "integer") and corresponding names (or NULL), inherited from the [Matrix](#), see there.

Extends

Class "Matrix", directly.

Methods

There's a C function `triangularMatrix_validity()` called by the internal validity checking functions.

Currently, [Schur](#), [isSymmetric](#) and `as()` (i.e. [coerce](#)) have methods with `triangularMatrix` in their signature.

See Also

`isTriangular()` for testing any matrix for triangularity; classes `symmetricMatrix`, and, e.g., `dtrMatrix` for numeric *dense* matrices, or `ltcMatrix` for a logical *sparse* matrix subclass of `"triangularMatrix"`.

Examples

```
showClass("triangularMatrix")

## The names of direct subclasses:
scl <- getClass("triangularMatrix")@subclasses
directly <- sapply(lapply(scl, slot, "by"), length) == 0
names(scl)[directly]

(m <- matrix(c(5,1,0,3), 2))
as(m, "triangularMatrix")
```

TsparseMatrix-class *Class "TsparseMatrix" of Sparse Matrices in Triplet Form*

Description

The `"TsparseMatrix"` class is the virtual class of all sparse matrices coded in triplet form. Since it is a virtual class, no objects may be created from it. See `showClass("TsparseMatrix")` for its subclasses.

Slots

`Dim, Dimnames`: from the `"Matrix"` class,

`i`: Object of class `"integer"` - the row indices of non-zero entries *in 0-base*, i.e., must be in $0:(nrow(.)-1)$.

`j`: Object of class `"integer"` - the column indices of non-zero entries. Must be the same length as slot `i` and *0-based* as well, i.e., in $0:(ncol(.)-1)$. For numeric `Tsparse` matrices, (i, j) pairs can occur more than once, see `dgTMatrix`.

Extends

Class `"sparseMatrix"`, directly. Class `"Matrix"`, by class `"sparseMatrix"`.

Methods

Extraction (`"["`) methods, see `[-methods`.

Note

Most operations with sparse matrices are performed using the compressed, column-oriented or [CsparseMatrix](#) representation. The triplet representation is convenient for creating a sparse matrix or for reading and writing such matrices. Once it is created, however, the matrix is generally coerced to a [CsparseMatrix](#) for further operations.

Note that all `new()`, `spMatrix` and `sparseMatrix(*, repr="T")` constructors for "TsparseMatrix" classes implicitly add (i.e., "sum up") x_k 's that belong to identical (i_k, j_k) pairs, see, the example below, or also "[dgTMatrix](#)".

For convenience, methods for some operations such as `%%` and `crossprod` are defined for [TsparseMatrix](#) objects. These methods simply coerce the [TsparseMatrix](#) object to a [CsparseMatrix](#) object then perform the operation.

See Also

its superclass, [sparseMatrix](#), and the [dgTMatrix](#) class, for the links to other classes.

Examples

```
showClass("TsparseMatrix")
## or just the subclasses' names
names(getClass("TsparseMatrix")@subclasses)

T3 <- spMatrix(3,4, i=c(1,3:1), j=c(2,4:2), x=1:4)
T3 # only 3 non-zero entries, 5 = 1+4 !
```

unpackedMatrix-class *Virtual Class "unpackedMatrix" of Unpacked Dense Matrices*

Description

Class "unpackedMatrix" is the *virtual* class of dense matrices in "unpacked" format, storing all $m \times n$ elements of an m -by- n matrix. It is used to define common methods for efficient subsetting, transposing, etc. of its *proper* subclasses: currently "[dln]geMatrix" (unpacked general), "[dln]syMatrix" (unpacked symmetric), "[dln]trMatrix" (unpacked triangular), and subclasses of these, such as "[dpoMatrix](#)".

Slots

Dim, Dimnames: as all [Matrix](#) objects.

Extends

Class "[denseMatrix](#)", directly. Class "[Matrix](#)", by class "[denseMatrix](#)", distance 2.

Methods

pack signature(x = "unpackedMatrix"): ...
unpack signature(x = "unpackedMatrix"): ...
isSymmetric signature(object = "unpackedMatrix"): ...
isTriangular signature(object = "unpackedMatrix"): ...
isDiagonal signature(object = "unpackedMatrix"): ...
t signature(x = "unpackedMatrix"): ...
diag signature(x = "unpackedMatrix"): ...
diag<- signature(x = "unpackedMatrix"): ...

Author(s)

Mikael Jagan

See Also

[pack](#) and [unpack](#); its virtual "complement" "[packedMatrix](#)"; its proper subclasses "[dsyMatrix](#)", "[ltrMatrix](#)", etc.

Examples

```
showClass("unpackedMatrix")
showMethods(classes = "unpackedMatrix")
```

updown-methods

Updating and Downdating Sparse Cholesky Factorizations

Description

Computes a rank- k update or downdate of a sparse Cholesky factorization

$$P_1 A P_1' = L_1 D L_1' = L L'$$

which for some k -column matrix C is the factorization

$$P_1 (A + s C C') P_1' = \tilde{L}_1 \tilde{D} \tilde{L}_1' = \tilde{L} \tilde{L}'$$

Here, $s = 1$ for an update and $s = -1$ for a downdate.

Usage

```
updown(update, C, L)
```

Arguments

update	a logical (TRUE or FALSE) or character ("+" or "-") indicating if L should be updated (or otherwise downdated).
C	a finite matrix or Matrix such that <code>tcrossprod(C)</code> has the dimensions of L.
L	an object of class dCHMsimpl or dCHMsuper specifying a sparse Cholesky factorization.

Value

A sparse Cholesky factorization with dimensions matching L, typically of class [dCHMsimpl](#).

Author(s)

Initial implementation by Nicholas Nagle, University of Tennessee.

References

Davis, T. A., Hager, W. W. (2001). Multiple-rank modifications of a sparse Cholesky factorization. *SIAM Journal on Matrix Analysis and Applications*, 22(4), 997-1013. doi:10.1137/S0895479899357346

See Also

Classes [dCHMsimpl](#) and [dCHMsuper](#) and their methods, notably for generic function [update](#), which is *not* equivalent to `updown(update = TRUE)`.

Generic function [Cholesky](#).

Examples

```
m <- sparseMatrix(i = c(3, 1, 3:2, 2:1), p = c(0:2, 4, 4, 6), x = 1:6,
  dimnames = list(LETTERS[1:3], letters[1:5]))
uc0 <- Cholesky(A <- crossprod(m) + Diagonal(5))
uc1 <- updown("+", Diagonal(5, 1), uc0)
uc2 <- updown("-", Diagonal(5, 1), uc1)
stopifnot(all.equal(uc0, uc2))
```

USCounties

Contiguity Matrix of U.S. Counties

Description

This matrix gives the contiguities of 3111 U.S. counties, using the queen criterion of at least one shared vertex or edge.

Usage

```
data(USCounties)
```

Format

A 3111×3111 sparse, symmetric matrix of class `dsCMatrix`, with 9101 nonzero entries.

Source

GAL lattice file ‘usc_q.GAL’ (retrieved in 2008 from ‘<http://sal.uiuc.edu/weights/zips/usc.zip>’ with permission from Luc Anselin for use and distribution) was read into R using function `read.gal` from package **spdep**.

Neighbour lists were augmented with row-standardized (and then symmetrized) spatial weights, using functions `nb2listw` and `similar.listw` from packages **spdep** and **spatialreg**. The resulting `listw` object was coerced to class `dsTMatrix` using `as_dsTMatrix_listw` from **spatialreg**, and subsequently to class `dsCMatrix`.

References

Ord, J. K. (1975). Estimation methods for models of spatial interaction. *Journal of the American Statistical Association*, 70(349), 120-126. doi:10.2307/2285387

Examples

```
data(USCounties, package = "Matrix")
(n <- ncol(USCounties))
I <- .symDiagonal(n)

set.seed(1)
r <- 50L
rho <- 1 / runif(r, 0, 0.5)

system.time(MJ0 <- sapply(rho, function(mult)
  determinant(USCounties + mult * I, logarithm = TRUE)$modulus))

## Can be done faster by updating the Cholesky factor:

C1 <- Cholesky(USCounties, Imult = 2)
system.time(MJ1 <- sapply(rho, function(mult)
  determinant(update(C1, USCounties, mult), sqrt = FALSE)$modulus))
stopifnot(all.equal(MJ0, MJ1))

C2 <- Cholesky(USCounties, super = TRUE, Imult = 2)
system.time(MJ2 <- sapply(rho, function(mult)
  determinant(update(C2, USCounties, mult), sqrt = FALSE)$modulus))
stopifnot(all.equal(MJ0, MJ2))
```

Description

This matrix gives the contiguities of 15260 one-degree grid cells of world land areas, using a criterion based on the great-circle distance between centers.

Usage

```
data(wrld_1deg)
```

Format

A 15260×15260 sparse, symmetric matrix of class `dsCMatrix`, with 55973 nonzero entries.

Source

Shoreline data were read into R from the GSHHS database using function `Rgshhs` from package `maptools`. Antarctica was excluded. An approximately one-degree grid was generated using function `Sobj_SpatialGrid`, also from `maptools`. Grid cells with centers on land were identified using the `over` method for classes `SpatialPolygons` and `SpatialGrid`, defined in package `sp`. Neighbours of these were identified by passing the resulting `SpatialPixels` object to function `dnearneigh` from package `spdep`, using as a cut-off a great-circle distance of $\sqrt{2}$ kilometers between centers.

Neighbour lists were augmented with row-standardized (and then symmetrized) spatial weights, using functions `nb2listw` and `similar.listw` from packages `spdep` and `spatialreg`. The resulting `listw` object was coerced to class `dsTMatrix` using `as_dsTMatrix_listw` from `spatialreg`, and subsequently to class `dsCMatrix`.

References

Ord, J. K. (1975). Estimation methods for models of spatial interaction. *Journal of the American Statistical Association*, 70(349), 120-126. doi:10.2307/2285387

Examples

```
data(wrld_1deg, package = "Matrix")
(n <- ncol(wrld_1deg))
I <- .symDiagonal(n)

doExtras <- interactive() || nzchar(Sys.getenv("R_MATRIX_CHECK_EXTRA"))
set.seed(1)
r <- if(doExtras) 20L else 3L
rho <- 1 / runif(r, 0, 0.5)

system.time(MJ0 <- sapply(rho, function(mult)
  determinant(wrld_1deg + mult * I, logarithm = TRUE)$modulus))

## Can be done faster by updating the Cholesky factor:

C1 <- Cholesky(wrld_1deg, Imult = 2)
system.time(MJ1 <- sapply(rho, function(mult)
  determinant(update(C1, wrld_1deg, mult), sqrt = FALSE)$modulus))
```

```
stopifnot(all.equal(MJ0, MJ1))

C2 <- Cholesky(wrld_1deg, super = TRUE, Imult = 2)
system.time(MJ2 <- sapply(rho, function(mult)
  determinant(update(C2, wrld_1deg, mult), sqrt = FALSE)$modulus))
stopifnot(all.equal(MJ0, MJ2))
```

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